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2008

## Three dimensional sensing by digital video fringe projection

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# **Three Dimensional Sensing by Digital Video Fringe Projection**

Matthew J. Baker

B.E. Telecommunications (Hons),  
University of Wollongong



A Thesis presented for the degree of  
Doctor of Philosophy

School of Electrical, Computer and Telecommunications Engineering,  
University of Wollongong,  
Australia,  
April 2008

Thesis supervisors: A/Prof. Jiangtao Xi and Prof. Joe F. Chicharo

This thesis is dedicated to my family and friends.

## **Abstract**

Fast, high precision and automated optical noncontact surface profile and shape measurement has been an extensively studied research area due to the diversity of potential application which extends to a variety of fields including but not limited to industrial monitoring, computer vision, virtual reality and medicine. Among others, structured light Fringe Projection approaches have proven to be one of the most promising techniques. Traditionally, the typical approach to Fringe Projection 3D sensing involves generating fringe images via interferometric procedures, however, more recent developments in the area of digital display have seen researchers adopting Digital Video Projection (DVP) technology for the task of fringe manufacture. The ongoing and extensive exploitation of DVP for Fringe Projection 3D sensing is derived from a number of key incentives the projection technology presents relative to the more traditional forms of projection. More specifically, DVP allows for the ability to accurately control various attributes of the projected fringe image at high speed in software, along with the capabilities to develop multi-channel techniques via colour projection. Furthermore, considering the typical DVP source is capable of projecting a standard 24 bit bitmap computer generated image, when interfaced to a personal computer, DVP makes for a very affordable projection source. However, despite the aforementioned incentives, in contrast to the more traditional methods of generating fringe images, the digitally projected fringe signal presents a number of shortcomings which ultimately hinder the effective application of the technology for Fringe Projection 3D sensing.

This thesis aims to improve the effectiveness of the deployment of DVP technology for Fringe Projection 3D sensing approaches. The proposed initiative is facilitated through extensive analysis of the application of DVP technology for fringe processing, and furthermore by the proposal of new digital fringe calibration procedures.

Firstly, this work demonstrates a comprehensive survey of current Fringe Projection 3D sensing approaches including an introductory review of the rudimentary notion of projecting fringes for 3D data acquisition. The survey also provides a thorough description of the evolution of the three major forms of fringe processing i.e. Fringe Phase Stepping,

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Fourier Fringe analysis and Direct Detection.

The limitations of DVP for Fringe Projection are demonstrated through the development of a novel fringe phase emulation approach. The phase emulation approach is subsequently employed to establish empirical insight into the application of DVP technology for Fringe Projection. More specifically, the preliminary empirical analysis is used to test the veracity of the application of the two chief DVP technologies (Liquid Crystal Display, LCD and Digital Light Processing, DLP, Texas Instruments) for Fringe Projection. Through this study the camera / projector non-linear intensity response is shown to be the single most significant shortcoming inherent to DVP based Fringe Projection implementations.

Following the findings of the preliminary empirical analysis the influence of the Display Gamma attributes of the projection system is extensively investigated. The harmonic structure of a typical digitally projected fringe signal is examined and an approximate analysis framework proposed. The framework is subsequently utilised to form a set of equations defining the true  $\gamma$  sensitivity of a range of highly exploited fringe processing techniques. The approximate analysis is later verified and the practical significance of the findings demonstrated. Through this study the true nature of the Display Gamma related phase measuring residual error is revealed.

With the aid of a verified framework, investigations into additional Display Gamma related Fringe Projection phenomena is undertaken. More specifically, the optimisation of digitally projected fringes by fringe parameter manipulation is demonstrated. The temporal nature of digitally projected fringe images is studied for the well exploited single shot Fourier Transform Profilometry technique and the digital fringe harmonic dependence on the projector optical modulation transfer function is revealed. Subsequently, the elimination of Display Gamma related Fringe Projection phase measuring residual error for phase stepping techniques by projector defocus optimisation is shown.

Finally, a novel digital fringe calibration approach ideal for minimum shot fringe processing techniques is proposed. The calibration procedure is centered on the application of Artificial Neural Networks (ANNs) to correct the non-linear intensity distortion associated with the camera / projector system. Unlike previously proposed gamma correction techniques, the neural fringe calibration technique requires no additional data acquisi-

tion with effective calibration requiring no more than a single cross-section of a reference fringe. The neural network fringe calibration approach is also shown to significantly outperform simple filter based techniques of similar computational complexity. Given the reduced data requirements for the neural approach its application for multi-channel fringe calibration is also considered.



# Certification

I, Matthew John Baker, declare that this thesis, submitted in fulfilment of the requirements for the award of Doctor of Philosophy, in the School of Electrical, Computer and Telecommunications Engineering, University of Wollongong, is wholly my own work unless otherwise referenced or acknowledged. The document has not been submitted for qualifications at any other academic institution.

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Matthew John Baker

17th February 2008

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# List of Publications

## Journal publications:

1. Matthew J. Baker, Jiangtao Xi, Joe Chicharo, “A Neural Network Digital Fringe Calibration Technique for Structured Light Profilometers”, *Applied Optics* 46, March 2007, pp 1233-1243.
2. Matthew J. Baker, Joe Chicharo and Jiangtao Xi, “Accuracy Limitations in Profilometric Metrology Schemes using Digital Structured Light”, *Accepted subject to revisions, IEEE Transactions on Instrumentation and Measurement*
3. Matthew J. Baker, Jiangtao Xi and Joe Chicharo “The Implications of Display Gamma for Fringe Projection 3D sensing using Digital Video Projection”, *To be submitted to Applied Optics*

## Conference publications:

4. Matthew. J. Baker, J. F. Chicharo J. Xi, and E. Li, “Accuracy limitations introduced by digital projection sources in profilometric optical metrology systems”, *IEEE Conference on Optoelectronic and Microelectronic Materials and Devices, COMMAD 2004*, Brisbane, Australia, 8-10 December 2004, pp.261-264 2005IEEE
5. Matthew. J. Baker, J. Xi, E. Li and J. F. Chicharo, “A contrast between DLP and LCD digital projection technology for triangulation based optical profilometry”, *Optics East: Sensors and Photonics for Applications in Industry, Life Sciences and Communica-*

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tions, Boston, Massachusetts, USA, October 25-26, 2005, (EI: 06109749730).

6. Matthew J. Baker, Jiangtao Xi, Joe Chicharo, "Fringe Calibration using Neural Network Signal Mapping for Structured Light Profilometers", *International Symposium on Intelligent Signal Processing and Communication Systems, ISPACS 2006*, Tottori, Japan, December 12-15, 2006.
7. Matthew J. Baker, Jiangtao Xi, Joe Chicharo, "Multi-channel Digital Fringe Calibration for Structured Light Profilometers using Neural Networks", *IEEE Instrumentation and Measurement Technology Conference, IMTC 2007*, Warsaw, Poland, May 1-3, 2007.
8. Matthew J. Baker, Joe Chicharo, Jiangtao Xi, "An Investigation into Temporal Gamma Luminance for Digital Fringe Fourier Transform Profilometers", *IEEE International Symposium on Intelligent Signal Processing, WISP 2007*, Madrid, Spain, October 3-5, 2007.
9. Matthew J. Baker, Jiangtao Xi, Joe Chicharo, "Elimination of  $\gamma$  Non-linear Luminance Effects for Digital Video Projection Phase Measuring Profilometers" *4th International Symposium on Electronic Design, Test and Applications, DELTA 2008*, Hong Kong, January 23-25 2008.

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# List of Abbreviations

3D	Three-Dimensional
2DFTP	Two-Dimensional Fourier Transform Profilometry
Am-Si	Amorphous Silicon
ANN	Artificial Neural Network
AOM	Acousto-Optic Modulator
CCD	Charged Couple Device
DC	Direct Component
DFP	Digital Fringe Projection
DFT	Discrete Fourier Transform
DLP	Digital Light Processing
DMD	Digital Micromirror Device
DPD	Direct Phase Detection
DVP	Digital Video Projection
FIR	Finite Impulse Response
FTP	Fourier Transform Profilometry
I3PSP	Improved Three Step Phase Stepping Profilometry
IFTP	Improved Fourier Transform Profilometry
IIR	Infinite Impulse Response
LCD	Liquid Crystal Display
LCOS	Liquid Crystal on Silicon
MEMS	MircroElectroMechanical System
MFTP	Modified Fourier Transform Profilometry
MMP	Modulation Measurement Profilometry
OPD	Optical Path Difference

PC	Personal Computer
PLL	Phase Locked Loop
PMP	Phase Measuring Profilometry
Poly-Si	Polycrystalline Silicon
PSD	Position Sensitive Detector
PSI	Phase Shifting Interferometry
PSP	Phase Stepping Profilometry
SLM	Spatial Light Modulator
SNR	Signal to Noise Ratio
SPD	Spatial Phase Detection
TFT	Thin Film Transistor
TI	Texas Instruments
TN	Twisted Nematic

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