Model-based correction for scatter and tailing effects in simultaneous 99mTc and 123I imaging for a CdZnTe cardiac SPECT camera

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Keywords
imaging, cdznTe, cardiac, spect, camera, scatter, model, tailing, correction, effects, simultaneous, $^{123}$I, $^{99m}$Tc

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Model-based correction for scatter and tailing effects in simultaneous $^{99m}\text{Tc}$ and $^{123}\text{I}$ imaging for a CdZnTe cardiac SPECT camera

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Abstract
An advantage of semiconductor-based dedicated cardiac single photon emission computed tomography (SPECT) cameras when compared to conventional Anger cameras is superior energy resolution. This provides the potential for improved separation of the photopeaks in dual radionuclide imaging, such as combined use of $^{99m}\text{Tc}$ and $^{123}\text{I}$. There is, however, the added complexity of tailing effects in the detectors that must be accounted for. In this paper we present a model-based correction algorithm which extracts the useful primary counts of $^{99m}\text{Tc}$ and $^{123}\text{I}$ from projection data. Equations describing the in-patient scatter and tailing effects in the detectors are iteratively solved for both radionuclides simultaneously using a maximum a posteriori probability algorithm with one-step-late evaluation. Energy window-dependent parameters for the equations describing in-patient scatter are estimated using Monte Carlo simulations. Parameters for the equations describing tailing effects are estimated using virtually scatter-free experimental measurements on a dedicated cardiac SPECT camera with CdZnTe-detectors. When applied to a phantom study with both $^{99m}\text{Tc}$ and $^{123}\text{I}$, results show that the estimated spatial distribution of events from $^{99m}\text{Tc}$ in the $^{99m}\text{Tc}$ photopeak energy window is very similar to that measured in a
single $^{99m}$Tc phantom study. The extracted images of primary events display increased cold lesion contrasts for both $^{99m}$Tc and $^{123}$I.

Keywords: CdZnTe, tailing effects, incomplete charge collection, dual radionuclide imaging, D-SPECT

(Some figures may appear in colour only in the online journal)

1. Introduction

Simultaneous imaging of $^{123}$I- and $^{99m}$Tc-labelled radiopharmaceuticals can be useful in a number of situations. The $^{99m}$Tc-labelled radiopharmaceuticals sestamibi (MIBI) and tetrofosmin are commonly used for myocardial perfusion imaging (Baggish and Boucher 2008). The $^{123}$I-labelled agents metaiodobenzylguanidine (MIBG) and iodophenylpentadecanoic acid (IPPA) can be used to image myocardial sympathetic innervation and fatty acid metabolism respectively (Verani et al 2000, Chirumamilla and Travin 2011). The use of combinations of these or other $^{99m}$Tc- and $^{123}$I-labelled agents can be advantageous as differences in uptake can assist in patient diagnosis. One example is imaging using the fatty acid analogue β-methyl-iodo-phenyl pentadecanoic acid (BMIPP) in conjunction with $^{99m}$Tc-sestamibi perfusion imaging, where a mismatch is frequent in areas with acute myocardial infarction (De Geeter et al 1994, Kumita et al 2000). Another example is imaging using $^{99m}$Tc-MIBI in conjunction with $^{123}$I-MIBG where regions of mismatch were identified extending beyond perfusion defects (Ben-Haim et al 2014). $^{123}$I-MIBG has been used sequential to $^{99m}$Tc-tetrofosmin to assess transmyocardial laser revascularization (Muxi et al 2003). Studies of other parts of the body include parathyroid imaging employing simultaneous use of $^{123}$I and $^{99m}$Tc-sestamibi (Hindié et al 1998) and brain imaging employing simultaneous use of $^{99m}$Tc-ECD and $^{123}$I-FP-CIT (El Fakhri et al 2006).

Simultaneous imaging in these cases is preferable to sequential imaging as it reduces time spent on the camera which is beneficial to both the patient and the clinic. Simultaneously acquired images will also automatically be perfectly registered as opposed to ones acquired sequentially where image registration may be necessary. With a typical energy resolution of 10% for an Anger camera with a sodium iodide crystal, the close proximity of the two photo-peaks of $^{99m}$Tc and $^{123}$I, at 140.5 keV and 159 keV respectively, results in cross-contamination between the photo-peaks (also known as cross-talk between photo-peaks). Suggested methods for simultaneous imaging in these cases include using an asymmetrical energy window for the $^{123}$I photopeak (Devous et al 1992). This, however, reduces the counting efficiency for $^{123}$I compared to using a symmetrical energy window (Ivanovic and Weber 1994). Other suggested methods for cross-contamination correction in dual radionuclide imaging using Anger cameras include model-based compensation (Kadmas et al 1999), a rotation-based Monte Carlo simulation method (de Jong and Beekman 2000), constrained spectral factor analysis (El Fakhri et al 2000), the use of artificial neural networks (El Fakhri et al 2000, 2001, 2002, Zheng et al 2004), iterative generalised spectral factor analysis (Hapdey et al 2006), generalised five-dimensional dynamic and spectral factor analysis (El Fakhri et al 2006b), the Monte Carlo based joint iterative reconstruction algorithm (Ouyang et al 2007, 2009) and the analytical photon distribution algorithm (Shcherbinin et al 2009).

Two dedicated cardiac cameras based on CdZnTe semiconductor technology have now been made available by manufacturers: the D-SPECT (Spectrum Dynamics, Caesarea, Israel) and Discovery NM 530c (GE Healthcare, Milwaukee, US). When semiconductor detectors...
are considered, one of the benefits is the superior energy resolution which assists in better separation of the two photopeaks. An additional benefit is that of superior sensitivity, allowing for dynamic tracer studies or low dose imaging protocols (Gimelli et al 2012, Ben-Haim et al 2013, Nakazato et al 2013). There is, however, a characteristic ‘tailing effect’ in the energy spectrum towards lower energies due to incomplete charge collection (Leo 1994). This effect and the pixelated design of dedicated cardiac cameras need to be considered when in-patient scatter and cross-contamination between the photopeaks is to be corrected for. Kacperski et al (2011) has proposed and validated a model-based correction algorithm for dual radionuclide imaging using $^{99m}$Tc and $^{201}$Tl for the D-SPECT dedicated cardiac camera with pixelated CdZnTe-detectors. The method employs multiple energy windows and model equations describing the tailing effects and scatter. The useful primary counts of the photopeaks are estimated by iteratively solving the equations using the acquired images in the energy windows. Monte Carlo simulations of point sources are employed to estimate the parameters for scatter modelling and experimental measurements using rod sources are employed to estimate the parameters for modelling of tailing effects.

In this paper we modify the model-based correction algorithm proposed by Kacperski et al (2011) and apply it to the new case of dual radionuclide imaging with $^{99m}$Tc and $^{123}$I. Monte Carlo simulations of digital chest phantoms are used in combination with experimental measurement using capillary tubes to estimate the appropriate parameters to be implemented in the algorithm. The equations are iteratively solved to extract the primary events from $^{99m}$Tc- and $^{123}$I-images acquired simultaneously.

2. Methods

The proposed correction algorithm seeks to iteratively estimate the primary and scatter components of $^{99m}$Tc and $^{123}$I by solving a set of equations, utilising models describing both tailing effects and scatter. The method employs multiple energy windows which are defined in section 2.1.1. The modelling of tailing effects which utilises parameters estimated using scatter-free experimental measurements is described in section 2.2. The modelling of photopeak scatter which utilises parameters estimated using Monte Carlo simulations is described in section 2.3. Scattered events from higher energy emissions of $^{123}$I are treated separately which is described in section 2.3.2 and the full set of equations to be solved is presented in section 2.4. A priori knowledge regarding the scatter fractions of $^{99m}$Tc and $^{123}$I used to aid convergence is described in section 2.4.1. Three experimental phantom studies, described in section 2.5, were performed in order to evaluate the proposed correction algorithm.

2.1. Simultaneous imaging using $^{123}$I and $^{99m}$Tc on the D-SPECT

A schematic drawing of the D-SPECT geometry can be seen in figure 1. Nine detectors are arranged in an arc around the chest of the patient. Each detector is composed of a $16 \times 64$ CdZnTe pixel array (16 in the transaxial direction and 64 in the axial direction) with a pixel pitch of 2.46 mm. Each detector is equipped with a parallel square hole tungsten collimator with a hole centre separation of 2.46 mm, centred over the individual pixels, and a septal thickness of 0.2 mm. During a SPECT scan the detectors rotate around their own individual central axes (sweep mode) and are translated to ensure complete tomographic sampling. Additional time is spent on the region of the heart which is determined in a scout scan prior to the full SPECT acquisition (Erlandsson et al 2009). All D-SPECT scans are acquired in list mode which allows for images to be generated for any number of energy windows post acquisition.
Two energy spectra experimentally measured on the D-SPECT system using capillary tubes filled with $^{99m}$Tc and $^{123}$I are presented in figure 2(a) and (b) respectively. The capillary tubes result in virtually scatter-free sources. The energy windows covering the photopeaks can be seen in the figure: W2 covers the $^{99m}$Tc photopeak at 140.5 keV (133–148 keV) and W3 covers the $^{123}$I photopeak at 159 keV (150–168 keV). It can be observed from these energy spectra that the contribution from $^{99m}$Tc counts in W3 is negligible. The tailing effect of incomplete charge collection at energies below the photopeak is evident.

2.1.1. Energy windows. Two energy spectra experimentally measured on the D-SPECT system using capillary tubes filled with $^{99m}$Tc and $^{123}$I are presented in figure 2(a) and (b) respectively. The capillary tubes result in virtually scatter-free sources. The energy windows covering the photopeaks can be seen in the figure: W2 covers the $^{99m}$Tc photopeak at 140.5 keV (133–148 keV) and W3 covers the $^{123}$I photopeak at 159 keV (150–168 keV). It can be observed from these energy spectra that the contribution from $^{99m}$Tc counts in W3 is negligible. The tailing effect of incomplete charge collection at energies below the photopeak, evident in these figures, is discussed in section 2.2. Figure 3 shows two energy spectra in units of counts per
3049 second per MBq separately measured using $^{99m}$Tc and $^{123}$I in the anthropomorphic phantom with scattering material shown in figure 4. The activity distribution in the phantom is specified in section 2.5. The summed energy spectrum of the two is shown as are two additional energy windows. W1 (105–130 keV) is situated below both photopeaks and is used in the count model as a window receiving scattered events and tailing effects from both photopeaks. W4 (173–196 keV) is situated above both photopeaks and is used to estimate the scattered events from $^{123}$I-emissions with energies higher than 159 keV (NNDC 2000).

Figure 3. Two separately measured energy spectra using an anthropomorphic phantom with a cardiac insert filled with $^{123}$I and $^{99m}$Tc. The summed energy spectrum and the energy windows used in this study are also shown.

Figure 4. A transaxial slice from a CT scan of the anthropomorphic phantom (a), vertical long axis of the cardiac insert (b) and short axis of the cardiac insert (c). The two lesions in the cardiac insert are indicated.
2.2. Modelling of tailing effects

A characteristic effect of impurities in irregularities in the CdZnTe-crystal lattice is that of trapping of electrons or holes (Leo 1994). When the trapping time is longer than the charge collection time this results in incomplete charge collection of photon detection. Tailing effects can also occur when a fraction of the photopeak signal is detected in one pixel and another fraction in a neighbouring pixel due to either charge cloud overlap (also known as cross-talk between pixels) or Compton and/or x-ray fluorescent scattering (Wagenaar 2004). The characteristic tailing effect of incomplete charge collection is evident in figure 2.

The model which describes the distribution of tailing photopeak events in an energy window below the photopeak energy window \((P_{\text{ph} \rightarrow \text{lo}})\) can be described by equation (1) (Kacperski et al 2011)

\[
P_{\text{ph} \rightarrow \text{lo}} = w_{\text{ph} \rightarrow \text{lo}} \cdot P_{\text{ph}} \otimes K_{\text{ph} \rightarrow \text{lo}}^P
\]

where \(w_{\text{ph} \rightarrow \text{lo}}\) indicates the photopeak energy window, \(l_0\) indicates the lower energy window, \(w_{\text{ph} \rightarrow \text{lo}}\) is a window-dependent weight factor and \(P_{\text{ph}}\) is the image of the primary events in the photopeak energy window. \(K_{\text{ph} \rightarrow \text{lo}}^P\) is a Gaussian kernel characterised by the window-dependent value of \(\sigma_{\text{ph} \rightarrow \text{lo}}\). The values of \(w_{\text{ph} \rightarrow \text{lo}}\) and \(\sigma_{\text{ph} \rightarrow \text{lo}}\) were estimated for all coupled energy windows using experimentally acquired projection images of capillary tubes filled with \(^{99m}\text{Tc}\) and \(^{123}\text{I}\) separately. The capillary sources were placed at the centre of the gantry (marked with a cross in figure 1) on a polystyrene block. The experimental setup is assumed to be scatter free and hence it is assumed that all events detected in \(\text{ph}\) are primary events and all events detected in \(\text{lo}\) are events from tailing effects. \(w_{\text{ph} \rightarrow \text{lo}}\) was calculated as \(N_{\text{lo}}/N_{\text{ph}}\) where \(N_{\text{lo}}\) and \(N_{\text{ph}}\) are the total number of counts in the photopeak and lower energy windows respectively. As the line-spread in the lower window is modelled as the line-spread in the photo-peak convolved with a Gaussian, it follow that:

\[
K_{\text{ph} \rightarrow \text{lo}} = e^{-\lambda_{\text{ph} \rightarrow \text{lo}} r}
\]

where \(C_{\text{ph} \rightarrow \text{lo}}\) and \(\alpha_{\text{ph} \rightarrow \text{lo}}\) are window-dependent weight factors and \(S_{\text{ph}}\) is the image of the photopeak scatter events. The kernel \(K_{\text{ph} \rightarrow \text{lo}}^S\) expressed in equation (3), is described by a mono-exponential function characterised by the window-dependent value of \(\lambda_{\text{ph} \rightarrow \text{lo}}\) (\(r\) is the radial distance). This is similar to other models in the literature (e.g. Meikle et al (1991)). The values of \(C_{\text{ph} \rightarrow \text{lo}}\) and \(\alpha_{\text{ph} \rightarrow \text{lo}}\) and \(\lambda_{\text{ph} \rightarrow \text{lo}}\) were estimated using Monte Carlo simulations as described in section 2.3.1.

2.3. Modelling of scatter

The model which describes the scatter in an energy window below the photopeak energy window \((S_{\text{ph} \rightarrow \text{lo}})\) can be described by equation (2) (Kacperski et al 2011)

\[
S_{\text{ph} \rightarrow \text{lo}} = C_{\text{ph} \rightarrow \text{lo}} \cdot \left( S_{\text{ph}} + \alpha_{\text{ph} \rightarrow \text{lo}} \cdot S_{\text{ph}} \otimes K_{\text{ph} \rightarrow \text{lo}}^S \right)
\]

where \(C_{\text{ph} \rightarrow \text{lo}}\) and \(\alpha_{\text{ph} \rightarrow \text{lo}}\) are window-dependent weight factors and \(S_{\text{ph}}\) is the image of the photopeak scatter events. The kernel \(K_{\text{ph} \rightarrow \text{lo}}^S\) expressed in equation (3), is described by a mono-exponential function characterised by the window-dependent value of \(\lambda_{\text{ph} \rightarrow \text{lo}}\) (\(r\) is the radial distance). This is similar to other models in the literature (e.g. Meikle et al (1991)). The values of \(C_{\text{ph} \rightarrow \text{lo}}\) and \(\alpha_{\text{ph} \rightarrow \text{lo}}\) and \(\lambda_{\text{ph} \rightarrow \text{lo}}\) were estimated using Monte Carlo simulations as described in section 2.3.1.

2.3.1. Monte Carlo modelling of photopeak scatter. The contribution from scattered events in a photopeak window to energy windows below was modelled using the Monte Carlo software SIMIND (Ljungberg and Strand 1989). The software XCAT (Segars et al 2010) was used to
generate digital chest phantoms of the adult male with a uniform activity distribution in the heart muscle. The linear attenuation coefficient maps were generated for both 140.5 keV and 159 keV and simulated separately. A transaxial slice of the phantom can be seen in figure 1. The phantom matrices were of size 128 × 128 × 128 with pixels of size 2.75 mm.

Nine simulations, representing the nine detectors of the D-SPECT, were set up for each radionuclide. The photons emitted from the heart will have been subjected to different tissue paths depending on which detectors they reach as seen in figure 1. Hence the fraction of scattered events detected will vary between the detectors. An in-house written MATLAB script was used to position the phantom in the D-SPECT geometry and the detectors were set to point to the centre of the left ventricle. A batch of nine simulations in total (one projection per detector head) was generated with the appropriate angle and distance between the phantom and each detector. A continuous detector was used in combination with a tungsten collimator with square holes of the same size as that of the D-SPECT and the appropriate values for the energy resolution of the CdZnTe-detector at 140.5 keV and 159 keV were used. More complex physics such as tailing effects in the detector were not included in order to isolate the relative effects of in-patient scatter in different energy windows. It should be noted that Monte Carlo modelling of CdZnTe-detectors in cardiac SPECT systems in SIMIND is in development (Ljunberg et al 2014) but not yet fully validated and was not available for this study. The higher energy emissions of $^{123}$I were not included in the simulations as those are treated separately as explained in section 2.3.2. Image matrices of size 256 × 256 with pixels of size 2.46 mm were acquired in the energy windows W1, W2 and W3.

The resulting scatter images were used in an in-house written MATLAB script to estimate the parameters in equation (2). The scatter distribution in the photopeak window, $S_{ph}$, was assumed constant and estimated using equation (4)

$$S_{W4\to lo} = S_{W4} \cdot \frac{\Delta E_{lo}}{\Delta E_{W4}}.$$  \hspace{1cm} (4)

where $S_{W4}$ is the directly measured image in energy window W4. This window is assumed to only contain scattered events from higher energy emissions of $^{123}$I. $\Delta E_{W4}$ and $\Delta E_{lo}$ are the widths of energy window W4 and the lower energy window respectively. This is a very similar approach to the two-window method applied by Kobayashi et al (2003).

### 2.3.2. Scatter from higher energy emissions.

In addition to the scatter originating from the photopeak at 159 keV when imaging $^{123}$I there is also a low level contribution from multiple high energy emissions. The contribution from these events to lower energy windows ($S_{W4\to lo}$) was assumed constant and estimated using equation (4)

$$S_{W4\to lo} = S_{W4} \cdot \frac{\Delta E_{lo}}{\Delta E_{W4}}.$$  \hspace{1cm} (4)

where $S_{W4}$ is the directly measured image in energy window W4. This window is assumed to only contain scattered events from higher energy emissions of $^{123}$I. $\Delta E_{W4}$ and $\Delta E_{lo}$ are the widths of energy window W4 and the lower energy window respectively. This is a very similar approach to the two-window method applied by Kobayashi et al (2003).

### 2.4. Equations to Be solved

The images of all events in energy windows W1, W2 and W3 are denoted $A_{W1}$, $A_{W2}$ and $A_{W3}$ respectively and are given by equations (5a)–(5e).

$$A_{W1} = P_{W2\to w1} + S_{W2\to w1} + P_{W3\to w1} + S_{W3\to w1} + S_{W4\to w1}$$  \hspace{1cm} (5a)

$$A_{W2} = P_{W2} + S_{W2} + P_{W3\to w2} + S_{W3\to w2} + S_{W4\to w2}$$  \hspace{1cm} (5b)

$$A_{W3} = P_{W3} + S_{W3} + S_{W4\to w3}$$  \hspace{1cm} (5c)
We seek to extract the unknown primary components for the two photopeaks: $P_{W2}$ for $^{99m}$Tc and $P_{W3}$ for $^{123}$I. These images represent the activity distribution in the patient or phantom free from scattered events and tailing effects. In order to do so we need to also estimate the unknown self-scatter (the scatter from the photopeak in its own energy window) for the two photopeaks ($S_{W2}$ and $S_{W3}$) and solve the linear problems described by equations (1) and (2) as we take the forward models described by equations (4) and (5a)–(5c) into consideration. The equations could in principle be solved using the maximum-likelihood expectation-maximisation (ML-EM) algorithm, as in Kacperski et al (2011). However, we found that, in this case, it was necessary to utilise a priori knowledge regarding the scatter fractions of $^{99m}$Tc and $^{123}$I, in order to aid convergence. Therefore, we opted for a maximum a posteriori probability (MAP) algorithm with one-step-late (OSL) evaluation (Green 1990). This approach is described in section 2.4.1. Note that in the approach presented by Kacperski et al (2011) the estimation of the scatter components was used in combination with the triple energy window scatter correction approach (Ogawa et al 1991). The approach presented here directly estimates the scatter components in each energy window.

The algorithm was initialised with the guesses that $P_{W3}$ and $S_{W3}$ were 80% and 20% respectively of the measured data in W3 and $P_{W2}$ and $S_{W2}$ were 40% and 10% respectively of the measured data in W2. The final converged solution is not sensitive to these starting values. However, the number of iterations required to reach the convergence do differ depending on the initial estimates.

At the stage in the algorithm where equation (2) is applied the estimates of $S_{ph}$ are rebinned to obtain conventional planar projections before convolution with $K_{ph \rightarrow kr}^E$. The D-SPECT design consists of nine smaller detectors that are exposed to in-patient scatter from activity outside their direct field of view which this approach accounts for (Kacperski et al 2011). After the convolution step inverse rebinning is applied to obtain the original projection composition.

Due to imperfections in the crystal-growing process there is a variation in uniformity of response between pixels in cameras with CdZnTe-detectors which is easily corrected for using uniformity correction maps (Wagenaar 2004). In order to account for non-uniformity of the detectors, each component in equations (5a)–(5c) were multiplied by an appropriate experimentally measured uniformity map. This was a necessary step before comparison of the estimated and the measured images.

### 2.4.1. Constraint

To aid convergence a constraint was incorporated in the algorithm. A Monte Carlo study was performed to investigate the relationship between the detection of $^{99m}$Tc and $^{123}$I activity in the heart muscle. In a clinical study, the relative activity levels of $^{99m}$Tc and $^{123}$I are unknown. Also, the fraction of primary events will be dependent on the size of the patient. However, the photopeak emissions of the two radionuclides should be affected to similar degrees regardless of their relative activity levels in the heart muscle. Digital chest phantoms of the adult female with a uniform activity distribution in the heart muscle were generated using the XCAT software. Four different sizes of breast tissue were generated to simulate different size patients. The distances between the apex of the heart and the chest surface of the phantoms were 4 cm, 5 cm, 7 cm and 9 cm respectively. The phantom sizes are denoted 1–4 respectively with 1 being the smallest and 4 being the largest. The linear attenuation coefficient maps were generated for both 140.5 keV and 159 keV and simulated separately. The high energy emissions of $^{123}$I were omitted in the simulations as only the photopeak scatter was to be taken into consideration. The phantom matrices were of size $128 \times 128 \times 128$ with pixels of size 2.75 mm. SIMIND was set up in the same way as described in section 2.3.1 and the detector was placed anterior to the phantoms at 17.6 cm distance from the centre of the
phantoms. Image matrices of size 256 × 256 with pixels of size 2.46 mm were acquired in the energy windows W2 and W3.

The scatter-to-total-ratio values were extracted from the result files from the simulation outputs and the primary-to-scatter-ratio (PTS) values were calculated. The values are presented in table 1. The results show that the PTS values vary greatly with patient size. The 99mTc-to-123I-ratio for PTS, however, varies only slightly with patient size. The average radionuclide ratio for PTS is 0.91 ± 0.01. A penalty term based on this constraint was incorporated into the algorithm. Note that the scatter in this context is the self-scatter from the photopeak in the corresponding photopeak energy window.

The basic ML-EM formula for the problem can be expressed according to equation (6):

$$f_{jb}^{n+1} = \sum_{ia} a_{ia,jb} \left( \sum_{kc} d_{ia} a_{ia,kc} f_{kc}^{nb} \right) f_{jb}^n,$$

where $n$ is the iteration number. In the context of this work, $d_{ia}$ is the measured counts in the $i$th energy window of the $a$th pixel. The quantity $f_{jb}^n$ is the $n$th estimate of the underlying primary or scatter component in a window (depending on $j$) for the $b$th pixel. In the dual-radionuclide problem there are four unknowns to be found for each pixel. Components $j = 1$ and 2 refer to $P_W$ and $S_W$ and components $j = 3$ and 4 refer to $P_{W3}$ and $S_{W3}$. The matrix $a_{ia,jb}$ is the system matrix, which couples the $j$th underlying value in pixel $b$ to the $i$th measured value in pixel $a$. Enforcing a prior of the Gibbs-form by the OSL approximation (Green 1990) leads to the following MAP update equation:

$$f_{jb}^{n+1} = \sum_{ia} a_{ia,jb} + \beta \frac{\partial U(f)}{\partial f_{jb}} \sum_{ia} a_{ia,jb} \sum_{kc} d_{ia} a_{ia,kc} f_{kc}^{nb},$$

where $\beta$ is the strength with which the prior is enforced and $U(f)$ is the ‘energy-function’. A convenient form for the latter quantity, enforcing the observed relationship between the underlying primary and scatter components in the 99mTc and 123I energy windows, was found to be:

$$U(f) = \frac{d_{sum}}{2} \left( \frac{\sum_{b} f_{1b}}{\sum_{b} f_{2b}} - c \frac{\sum_{b} f_{3b}}{\sum_{b} f_{4b}} \right)^2 = \frac{d_{sum}}{2} \left( \frac{\sum_{b} P_{W2}}{\sum_{b} S_{W2}} - c \frac{\sum_{b} P_{W3}}{\sum_{b} S_{W3}} \right)^2,$$

where $d_{sum} = \sum_{ia} d_{ia}$ is the total number of measured counts summed over all four energy windows and pixels. Based on the simulations and analysis described above, we have found that to a good approximation $c = 0.91$ (independent of patient size). The final step is to derive the necessary derivatives. These are:

<table>
<thead>
<tr>
<th>Phantom size</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>PTS 99mTc (W2)</td>
<td>4.52</td>
<td>4.02</td>
<td>3.06</td>
<td>2.51</td>
</tr>
<tr>
<td>PTS 123I (W3)</td>
<td>4.95</td>
<td>4.37</td>
<td>3.40</td>
<td>2.80</td>
</tr>
<tr>
<td>99mTc-to-123I-ratio for PTS</td>
<td>0.91</td>
<td>0.92</td>
<td>0.90</td>
<td>0.90</td>
</tr>
</tbody>
</table>
The purpose of the normalization factor of $d_{\text{sum}}$ is now apparent: it removes the scaling of the derivatives with the total number of measured counts. In our numerical studies, a value of $\beta = 0.0045$ has proved successful.

\[ \frac{\partial U(f)}{\partial f_{lb}} = d_{\text{sum}} \sum_{b} \frac{P_{W2}}{S_{W2}} - c \frac{\sum_{b} P_{W3}}{\sum_{b} S_{W3}} \]  

\[ \frac{\partial U(f)}{\partial f_{lb}} = -d_{\text{sum}} \sum_{b} \frac{P_{W2}}{S_{W2}} \left( \sum_{b} P_{W2} - c \frac{\sum_{b} P_{W3}}{\sum_{b} S_{W3}} \right) \]  

\[ \frac{\partial U(f)}{\partial f_{lb}} = -c \cdot d_{\text{sum}} \sum_{b} \frac{P_{W3}}{S_{W3}} \left( \sum_{b} P_{W3} - c \frac{\sum_{b} P_{W3}}{\sum_{b} S_{W3}} \right) \]  

\[ \frac{\partial U(f)}{\partial f_{lb}} = c \cdot d_{\text{sum}} \sum_{b} \frac{P_{W3}}{S_{W3}} \left( \sum_{b} P_{W3} - c \frac{\sum_{b} P_{W3}}{\sum_{b} S_{W3}} \right). \]  

\[ \text{(9a) \quad (9b) \quad (9c) \quad (9d)} \]

The purpose of the normalization factor of $d_{\text{sum}}$ is now apparent: it removes the scaling of the derivatives with the total number of measured counts. In our numerical studies, a value of $\beta = 0.0045$ has proved successful.

**2.5. Phantom studies**

Three experimental phantom studies were performed in order to evaluate the obtained images after processing with the proposed algorithm. A thorax phantom (Data Spectrum Corporation, Hillsborough, NC, USA) with a cardiac insert as well as spine- and lung compartments were used. A transaxial slice of a CT-scan of the phantom can be seen in figure 4(a). Figures 4(b) and (c) show the cardiac insert orientated in the vertical long axis and the short axis respectively. Two lesions, as seen in the figures, were included in all three studies. Lesion 1 is fillable and lesion 2 is entirely made of Perspex. In study 1 the myocardium compartment was filled with $^{99m}$Tc whilst lesion 1 was filled with non-radioactive water. In study 2 the myocardium compartment and lesion 1 were filled with equal activity concentrations of $^{123}$I. In study 3, the dual radionuclide study, the compartments were filled with both $^{99m}$Tc and $^{123}$I as in studies 1 and 2 (i.e. no $^{99m}$Tc in lesion 1). In each study the phantom was scanned ten times in order to estimate the uncertainty on the calculations of lesion contrast. For each scan the acquisition time was increased to account for the decay of $^{99m}$Tc.

The count statistics in the phantom study was similar to that of a clinical scan. In the study protocol employed by Ben-Haim et al (2014) a 300 MBq injection of $^{99m}$Tc-MIBI was followed by a 150 MBq injection of $^{123}$I-MIBG approximately 75 min later. The dual radionuclide scan started approximately 15 min later with an acquisition time of 20 min. An equivalent $^{99m}$Tc activity level of 2.7 MBq for a 20 min scan was used in the experimental studies 1 and 3. With an estimated myocardial uptake of 1.2% for MIBI (Crawford and Husain 2010) this closely corresponds to the $^{99m}$Tc activity in the clinical protocol at the time of scan. The equivalent of 2.8 MBq of $^{123}$I for a 20 min scan was used in studies 2 and 3. With an estimate of 0.8% for MIBG uptake (Kline et al 1981) the level of $^{123}$I is elevated compared to the
protocol of Ben-Haim et al. This poses a worst-case situation with more pollution from $^{123}$I to the $^{99m}$Tc energy window than in the clinical situation.

The D-SPECT list mode data were used to generate projection images for energy windows W1, W2, W3 and W4. The ten scans from study 3 were then processed to extract the primary components ($P_{W2}$ and $P_{W3}$) using the method described above. Fifteen iterations were used and there was no smoothing applied to the data in the algorithm. The final projection images were normalised by the total expected number of counts in each window and saved. In order to directly compare the results with the images acquired in studies 1 and 2 the following images were also created:

- Contributions from $^{99m}$Tc in W2 ($P_{W2} + S_{W2}$)
- Contributions from $^{123}$I in W2 ($P_{W3} \rightarrow W2 + S_{W3} \rightarrow W2 + S_{W4} \rightarrow W2$)

Tomographic images were reconstructed using an ordered subsets expectation-maximisation (OS-EM) algorithm including collimator response modelling (Spectrum Dynamics). The lesion contrasts in the reconstructed data were calculated using volumes of interest delineated with help from the aligned CT-scan of the phantom as $(a_m - a_l)/a_m$, where $a_m$ and $a_l$ are the average counts in the myocardial and lesion volumes of interest respectively. The coefficient of variation (CV) was calculated for the myocardial volume in the $^{99m}$Tc and $^{99m}$Tc + $^{123}$I studies for energy window W2 in order to investigate the level of noise.

The count rates (number of detected counts per unit activity per unit time) in the images in W2 from studies 1 and 2 were used to calculate the expected fraction of $^{99m}$Tc and $^{123}$I in W2 in study 3. The results were compared to the fractions obtained after processing using the algorithm.

### 3. Results

#### 3.1. Parameters for modelling of trapping and Monte Carlo scatter

The values for $w_{ph \rightarrow lo}$ and $\sigma_{ph \rightarrow lo}$ used in equation (1) for modelling of tailing effects are presented in table 2 together with the values for $C_{ph \rightarrow lo}$, $\alpha_{ph \rightarrow lo}$ and $\lambda_{ph \rightarrow lo}$ used in equation (2) for modelling of scatter. Figure 5 shows normalised line profiles across the images of the capillary tubes for the photopeak energy window as well as the lower energy windows.

Figure 6 shows line profiles across images of the photopeak scatter, the ‘true’ scatter in the lower window (obtained from the Monte Carlo simulations) and the estimated scatter in the lower window using equation (2). Line profiles are presented for all coupled windows for detector positions 5((a)–(c)) and 1((d)–(f)) (with positions and projection angles as presented in figure 1). For illustrative purposes figures 6(g) and (h) show digitally reconstructed radio-raphs of the XCAT phantom as seen by these two detectors, with an overlay of the activity

### Table 2

<table>
<thead>
<tr>
<th>Photopeak window</th>
<th>Lower window</th>
<th>Tailing parameters</th>
<th>Scatter parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>($ph$)</td>
<td>($lo$)</td>
<td>$w_{ph \rightarrow lo}$</td>
<td>$\sigma_{ph \rightarrow lo}$ (cm)</td>
</tr>
<tr>
<td>W2</td>
<td>W1</td>
<td>0.422</td>
<td>0.586</td>
</tr>
<tr>
<td>W3</td>
<td>W2</td>
<td>0.367</td>
<td>0.588</td>
</tr>
<tr>
<td>W3</td>
<td>W1</td>
<td>0.332</td>
<td>0.752</td>
</tr>
</tbody>
</table>
distribution. These images were generated by rotating the XCAT attenuation coefficient phantom as well as the activity distribution phantom along the central axis and summing up the 3D-volumes to a planar projection. Figures 6(i) and (j) show the scatter images in W1 (from $^{99m}$Tc) for these two detectors illustrating the positions of the line profiles.

3.2. Phantom study

Figure 7 shows the convergence of estimations of $^{99m}$Tc and $^{123}$I contributions to W2 as a function of iteration number in the correction algorithm for the first scan of the phantom filled with both radionuclides. Figure 8 shows short axis and vertical long axis views of reconstructed images (with the lesions being oriented in the same way as presented in figure 4) as well as bull’s eye plots from all three phantom studies. The images show the mean of the ten scans of each study. Figure 9 shows circular line profiles from the W2 images. The line profiles start at the top of the short axis images (lesion 2) and go all the way around the myocardium.

The obtained lesion contrasts in the three phantom studies are presented in table 3. The distribution of $P_{W2} + S_{W2}$ from the dual radionuclide study (study 3) should be similar to that measured in the single $^{99m}$Tc study (study 1) in W2. Note the close corresponding contrasts between these images in table 3. It was also found that the difference in CV within the myocardium volume between these two image datasets was very small. This illustrates that no mid-iteration smoothing was necessary to suppress noise at the activity levels investigated.

4. Discussion

The work presented in this study is a continuation on the work by Kacperski et al (2011) which was developed for dual radionuclide imaging using $^{99m}$Tc and $^{201}$Tl. One of the differences is that the estimation of the scatter components in the forward problem in the previous study was used in combination with the triple energy window scatter correction approach. The algorithm presented here directly estimates the scatter components in each energy window and therefore could be considered a more straightforward approach. Another difference is that the parameters for the scatter model were estimated using simulated point sources at various depths in water in the previous study. In this study the parameters were estimated using a digital chest
phantom imaged from the various angles of the D-SPECT detectors. A constraint was incor-
porated into the ML-EM algorithm to assist convergence in this $^{99m}$Tc- and $^{123}$I-study.

The line profiles shown in figure 6 show that there is good agreement between the ‘true’
scatter in a lower energy window (as estimated by Monte Carlo simulations) and that esti-
mated using equation (2) with the parameters presented in table 2. The agreement gets worse
towards the edge of the patient as the convolution results in scattered events being placed
outside the border of the body outline. This is particularly noticeable in the example shown for
detector position 1 from which angle the activity distribution appears near the outline of the
body. However, for areas over and near the heart region the agreement is good.

--- Photopeak scatter, --- ‘True’ scatter in lower window, -- Estimated scatter in lower window

Figure 6. Line profiles across the images of photopeak scatter and lower window
scatter obtained from Monte Carlo simulations together with line profiles as estimated
in the scatter model for detector 5: (a) W3 to W2, (b) W3 to W1, (c) W2 to W1 and
detector 1: (d) W3 to W2, (e) W3 to W1 and (f) W2 to W1. Intensity projections with
enhanced heart as seen by detector positions 5 (g) and 1 (h) and images of the scatter in
W1 from $^{99m}$Tc with positions of the line profiles for detector positions 5 (i) and 1 (j).
It can be seen in figure 8 that there is good spatial agreement in the measured contribution from $^{99m}$Tc in W2 in the single radionuclide study (a) and that estimated for $^{99m}$Tc in W2 in the dual radionuclide study (f). There is also good spatial agreement in the measured contribution from $^{123}$I in W2 in the single radionuclide study (b) and that estimated for $^{123}$I in W2 in the dual radionuclide study (g). These agreements can also be seen in the line profiles in figure 9, where the magnitude of the correction also can be seen.

The contrast in the estimated contribution from $^{99m}$Tc ($P_{W2} + S_{W2}$) in the dual radionuclide study agrees well with that measured in the single $^{99m}$Tc study (0.64 ± 0.02 compared to 0.64 ± 0.03 for lesion 1 and 0.75 ± 0.02 compared to 0.80 ± 0.01 for lesion 2). The contrast in the dataset comprised of primary $^{99m}$Tc events only, extracted from study 3, has a 20% and 8% improvement in lesion contrast for lesions 1 and 2 respectively compared to the uncorrected dataset. The greatest contrast recovery for $^{99m}$Tc is achieved by removing the contributions from $^{123}$I. The contrast degradation due to self-scatter for $^{99m}$Tc in W2 is only marginal (0.66 ± 0.02 compared to 0.64 ± 0.02 for lesion 1 and 0.78 ± 0.02 compared to 0.75 ± 0.02 for lesion 2). The contrast in the dataset comprised of primary $^{123}$I events has a 5% improvement for lesion 2 compared to the uncorrected dataset in W3. Only a small improvement in this energy window (W3) is expected as it is less polluted by extraneous components. The obtained count rates per unit activity in studies 1 and 2 predicted that the fraction of events in W2 originating from $^{99m}$Tc and $^{123}$I in the first scan of study 3 should be 0.60 and 0.40 respectively. The fractions obtained after processing were found to be 0.71 and 0.29 respectively. This moderate discrepancy would warrant further investigation in future work.

The level of noise in the extracted image $P_{W2} + S_{W2}$ was at the same level as that for the uncorrected image measured in W2 in the single $^{99m}$Tc-study. Mid-iteration smoothing of the images was not applied in this study but can be applied to suppress noise (Kacperski et al 2011).

The estimation of parameters for the scatter modelling in this study was performed based on a default adult male digital phantom, which is believed to be representative of a typical patient. Whether these parameter fits are sufficiently accurate for unusually large or small patients is worth future investigation. Another subject for future investigation is the impact of excessive extra-cardiac activity on the performance of the proposed correction algorithm.

The obtained images of the primary photopeak counts, which do not have Poisson noise statistics, should strictly speaking not be reconstructed using an ML-EM algorithm, or as in this case, an OS-EM algorithm (Hutton et al 2006). However, these initial encouraging results provide a good foundation for future implementation of the model-based correction in the
reconstruction software via the use of the extracted projections of primary counts. An alternative approach, preserving Poisson statistics, would be to explore the addition of the estimated

**Figure 8.** The obtained images in the reconstructed data from the uncorrected images from studies 1 (99mTc), 2 (123I) and 3 (99mTc and 123I) as well as the reconstructed data from the estimated contributions after processing study 3.
Figure 9. Circular line profiles from short axis slices of the obtained data from the uncorrected images in W2 from studies 1 ($^{99m}$Tc), 2 ($^{123}$I) and 3 ($^{99m}$Tc and $^{123}$I) as well as the estimated contributions after processing study 3.

Table 3. The obtained lesion contrasts in the reconstructed data from the uncorrected images from studies 1 ($^{99m}$Tc), 2 ($^{123}$I) and 3 ($^{99m}$Tc and $^{123}$I) as well as the estimated contributions after processing study 3.

<table>
<thead>
<tr>
<th>Study</th>
<th>Window</th>
<th>Data</th>
<th>Lesion 1</th>
<th>Lesion 2</th>
<th>CV $^{d,e}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 ($^{99m}$Tc)</td>
<td>W2</td>
<td>uncorrected (a)</td>
<td>0.64 ± 0.02</td>
<td>0.80 ± 0.01</td>
<td>52% ± 1%</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2 ($^{123}$I)</td>
<td>W2</td>
<td>uncorrected (b)</td>
<td>0.21 ± 0.06</td>
<td>0.50 ± 0.04</td>
<td>35% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W3</td>
<td>uncorrected (c)</td>
<td>—</td>
<td>0.76 ± 0.02</td>
<td>49% ± 1%</td>
</tr>
<tr>
<td>3 ($^{99m}$Tc &amp; $^{123}$I)</td>
<td>W2</td>
<td>uncorrected (d)</td>
<td>0.55 ± 0.01</td>
<td>0.72 ± 0.01</td>
<td>43% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W2</td>
<td>$P_{w2} + S_{w2}(f)$</td>
<td>0.64 ± 0.02</td>
<td>0.75 ± 0.02</td>
<td>50% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W2</td>
<td>$P_{w2}(h)$</td>
<td>0.66 ± 0.02</td>
<td>0.78 ± 0.02</td>
<td>54% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W2</td>
<td>$P_{w1 \rightarrow w2 + S_{w3 \rightarrow w2} + S_{w4 \rightarrow w2}(g)}$</td>
<td>0.18 ± 0.02</td>
<td>0.54 ± 0.01</td>
<td>28% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W3</td>
<td>uncorrected (e)</td>
<td>—</td>
<td>0.76 ± 0.01</td>
<td>48% ± 1%</td>
</tr>
<tr>
<td></td>
<td>W3</td>
<td>$P_{w3(i)}$</td>
<td>—</td>
<td>0.80 ± 0.01</td>
<td>54% ± 1%</td>
</tr>
</tbody>
</table>

$^{a}$ The letter in parentheses indicate the position in figure 8.
$^{b}$ The values presented are mean ± standard deviation for the ten scans.
$^{c}$ Lesion 1 was only a defect (cold) for the $^{99m}$Tc-distribution.
$^{d}$ Coefficient of variation in the myocardial volume of interest.
$^{e}$ The values presented are mean ± standard deviation for the ten scans.
scatter projections to the forward projections within the iterative reconstruction, as discussed in Hutton et al (2011).

5. Conclusion

We have developed a model-based iterative algorithm to correct for in-patient scatter and tailing effects in dual radionuclide imaging with $^{99m}$Tc and $^{123}$I for a CdZnTe-detector cardiac camera. Parameters for the modelling of scatter were simulated using the Monte Carlo technique and parameters for the modelling of tailing effects were estimated using experimental measurements. The algorithm yielded improved images for both $^{99m}$Tc and $^{123}$I with increased lesion contrast.

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