

1-1-2008

## Feature based stereo correspondence using moment invariant

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### Recommended Citation

Premaratne, Prashan and Safaei, Farzad: Feature based stereo correspondence using moment invariant 2008, 104-108.

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### Abstract

Autonomous navigation is seen as a vital tool in harnessing the enormous potential of Unmanned Aerial Vehicles (UAV) and small robotic vehicles for both military and civilian use. Even though, laser based scanning solutions for Simultaneous Location And Mapping (SLAM) is considered as the most reliable for depth estimation, they are not feasible for use in UAV and land-based small vehicles due to their physical size and weight. Stereovision is considered as the best approach for any autonomous navigation solution as stereo rigs are considered to be lightweight and inexpensive. However, stereoscopy which estimates the depth information through pairs of stereo images can still be computationally expensive and unreliable. This is mainly due to some of the algorithms used in successful stereovision solutions require high computational requirements that cannot be met by small robotic vehicles. In our research, we implement a feature-based stereovision solution using moment invariants as a metric to find corresponding regions in image pairs that will reduce the computational complexity and improve the accuracy of the disparity measures that will be significant for the use in UAVs and in small robotic vehicles.

### Keywords

Feature, based, stereo, correspondence, using, moment, invariant

### Disciplines

Physical Sciences and Mathematics

### Publication Details

Premaratne, P. & Safaei, F. 2008, "Feature based stereo correspondence using moment invariant", 4th International Conference on Information and Automation for Sustainability. Sustainable Development Through Effective Man-Machine Co-Existence, IEEE Region 10 and ICIAFS, Colombo, Sri Lanka, pp. 104-108.

# Feature based Stereo Correspondence using Moment Invariant

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**Abstract**—Autonomous navigation is seen as a vital tool in harnessing the enormous potential of Unmanned Aerial Vehicles (UAV) and small robotic vehicles for both military and civilian use. Even though, laser based scanning solutions for Simultaneous Location And Mapping (SLAM) is considered as the most reliable for depth estimation, they are not feasible for use in UAV and land-based small vehicles due to their physical size and weight. Stereovision is considered as the best approach for any autonomous navigation solution as stereo rigs are considered to be lightweight and inexpensive. However, stereoscopy which estimates the depth information through pairs of stereo images can still be computationally expensive and unreliable. This is mainly due to some of the algorithms used in successful stereovision solutions require high computational requirements that cannot be met by small robotic vehicles. In our research, we implement a feature-based stereovision solution using moment invariants as a metric to find corresponding regions in image pairs that will reduce the computational complexity and improve the accuracy of the disparity measures that will be significant for the use in UAVs and in small robotic vehicles.

**Keywords**—moment invariants, feature-based stereo correspondence, sum of squared difference (SSD)

## I. INTRODUCTION

Stereo vision is a mechanism for obtaining depth information from digital images. The challenge in stereovision is how to find corresponding points in the left image and the right image, known as the correspondence problem. Once a pair of corresponding points is found the depth can be computed using triangulation. There are two prominent approaches to finding such corresponding pairs namely, area-based and feature-based techniques. In the area based techniques, every pixel in a designated area of one image is compared with the pixels in the same row of the other image. This is done with few constraints such as maximum disparity to avert any false matches. Some of the well-known techniques in this approach are Hierarchical Block Matching [1], Census [2], Correlation Matching [3-4] and Zitnick-Kanade (Cooperative Algorithm for Stereo Matching and Occlusion Detection) [5-6] algorithms. The feature-based methods rely on finding special features in corresponding pairs and may result in fewer depth values lowering the computational complexity.

Our approach is very much aimed at controlling small robotic vehicles using stereovision for depth calculation. This depth information will be used in control algorithms to detect and avoid obstacles. If this depth information is to be useful, they need to be estimated in realtime which requires any stereovision algorithm to be less computationally expensive.

With our great success in using moment invariants for recognizing hand gestures, moment invariants can be of great use in finding corresponding matching regions in stereo pairs [7-8]. Moment invariants are invariant to rotation, scale and shift and the rotation invariant property is especially beneficial to the stereo correspondence problem as any misalignment or non-flat ground conditions can create slightly rotated versions of any scene in any one of the cameras. In our approach, we rely on edge-corner detection algorithms such as Harris corner detection [8] to produce reliable feature points. This will result in fewer points of interest compared to area-based techniques [9-18]. An image can be separated to a collection of blocks and can be marked as candidates or not depending on whether they occupy corners (or edges). These blocks can be matched with the help of moment invariants and disparity of the identified features can be simply calculated.

In this paper, section II details the general stereo matching approaches and the moment invariant based technique is presented in detail in section III. This is followed by our experimental results and the conclusion.

## II. STEREO MATCHING APPROACHES

In area based stereo matching, for a given pair of stereo images, the corresponding points are supposed to lie on the epipolar lines [19]. Area based techniques rely on the assumption of surface continuity, and often involve some correlation-measure to construct a disparity map with an estimate of disparity for each point visible in the stereo pair. Area based techniques produce much denser disparity maps, which is critical in obstacle detection and avoidance.

Since corresponding points are the same real point in the captured scene projected into left and right images, we can assume that their surroundings in both pictures would be quite similar. Area-based methods use this similarity for corresponding points detection [9-13]. It is computed from the difference in local neighborhoods (usually a constant size

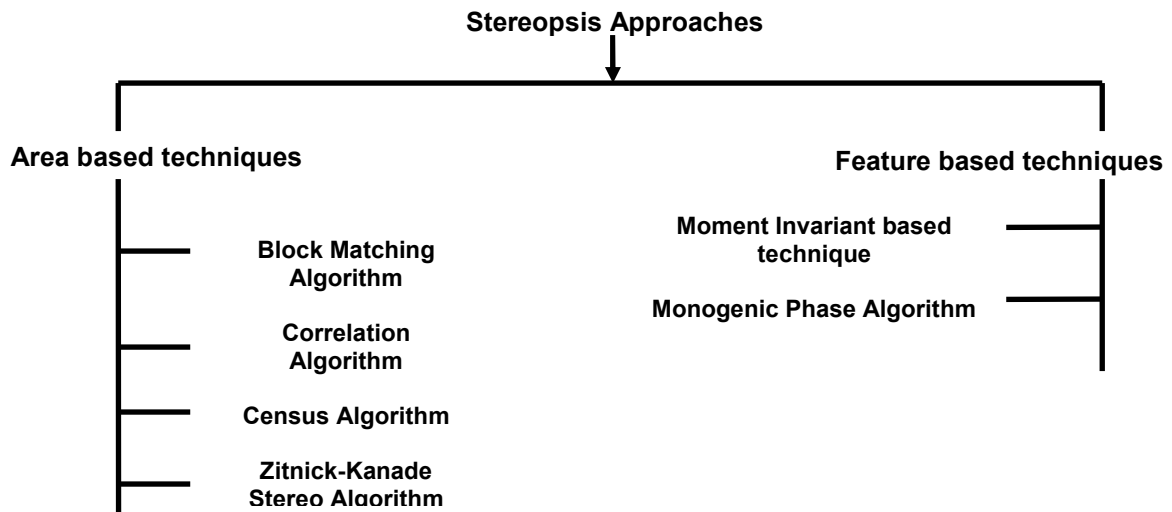


Figure 1. Stereopsis Approaches

square) of the points. Computing the similarity of two points is the elementary step in the method and cannot be accelerated. The main problem is to look for the corresponding point in the picture. The naive area-based algorithm chooses a point from the first image, and run through all the points in the second image to find its corresponding point. This inefficient process can be accelerated by restraining the search area to a specific region around the corresponding pixel by specifying a maximum disparity. The most efficient method is adapted from Epipolar Geometry known as epipolar constraint.

Area based methods are considered to be computationally expensive due to the exhaustive nature of the metrics being used. Sum of Squared Difference (SSD), Sum of Absolute Difference, Sum of Sum of Squared Difference (SSSD) and Cross Correlation based metrics use every pixel to calculate these metrics making them exhaustive.

Feature-based stereo matching techniques focus on local intensity variations and generate depth information only at points where features are detected. In general, feature-based techniques provide more accurate information in terms of locating depth discontinuities and thus achieve fast and robust matching. However they yield very sparse range maps and may have to undergo expensive feature extraction process. Edge elements, corners, line segments, and curve segments are features that are robust against the change of perspective, and they have been widely used in many stereovision work. Features such as edge elements and corners are easy to detect however, they may suffer from occlusion whereas line and curve segments require extra computation time, but are more robust against occlusion. Higher level image features such as circles, ellipses, and polygonal regions have also been used as features for stereo matching. These features are, however, restricted to images of indoor scenes. Nevertheless, feature based techniques are associated with computation of conjugate

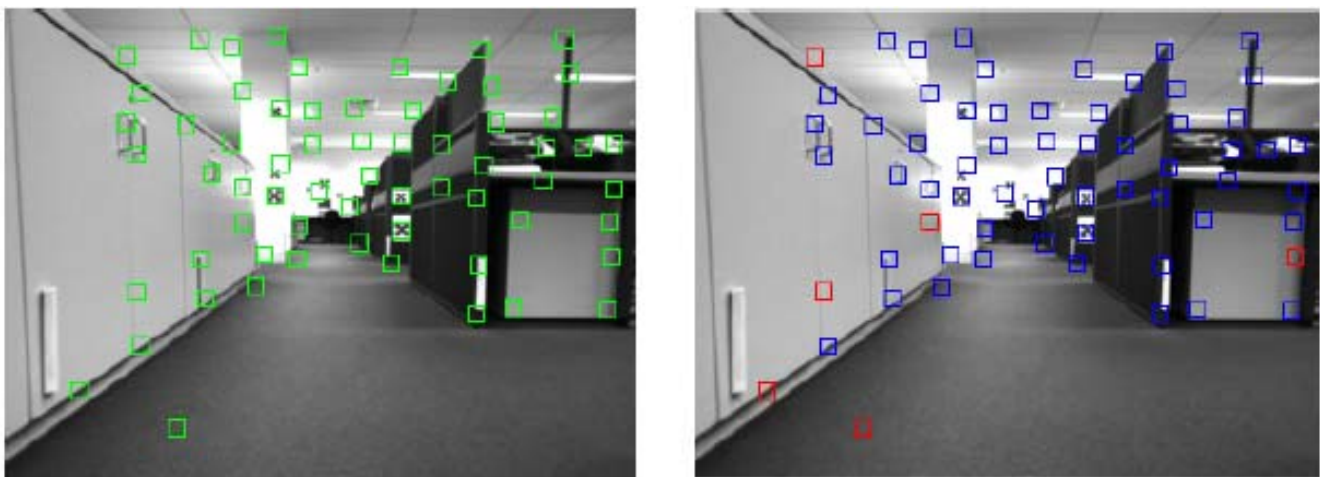


Figure 2. Left and Right stereo images with 'corners' marked using Harris corner detection

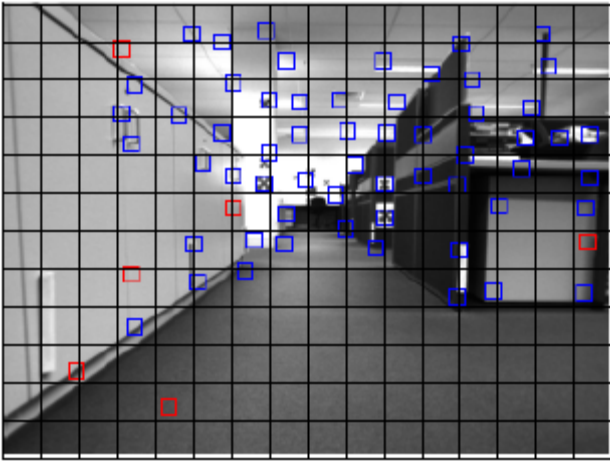


Figure 3. Left image is divided into blocks of size 20x20 pixels

pairs with subpixel accuracy. They will also include object-dependent constraints in the solution of the correspondence problem such as ‘corners’ when using Harris corner detection algorithm.

### III. MOMENT INVARIANT BASED STEREO MATCHING

Using invariant moments to locate corresponding features in stereo pairs will be less computationally intensive as the number of block comparisons will depend on the disparity constraint as well as number of features. In our approach, ‘corners’ will be used as features as shown in Fig. 2. Then the left image is divided into 20x20 pixel blocks and will be marked with occupying features (Fig. 3). Then the blocks containing features will be used to calculate the first 4 moments using equations 3 to 6. Even though the moment invariants can calculate upto 7 such moments, 4 moments will be adequate to uniquely represent a square. Using epipolar and disparity constraints, we can now evaluate the adjoining 20x20 pixel blocks in the Right image for matches for the blocks containing the features. The ‘closeness’ of these moments will be decided using a threshold that is dependent on the image scenery. When such blocks are identified, the simple depth calculation formula can be used to calculate the depth to the identified feature as follows:

$$d = b \frac{f}{D}$$

Where  $d$  is the depth the object from the camera plane,  $f$  being the focus of the camera,  $D$  the disparity  $a$   $b$  is the baseline distance. Here the underlying assumption is that the epipolar lines run parallel to the image lines, so that corresponding points lie on the same image lines.

#### A. Moment Invariants

Moment invariants algorithm has been known as one of the most effective methods to extract descriptive feature for object recognition applications. The algorithm has been widely applied in classification of aircrafts, ships, ground targets, etc

[20, 21]. Essentially, the algorithm derives a number of self-characteristic properties from a binary image of an object. These properties are invariant to rotation, scale and translation. Let  $f(i,j)$  be a point of a digital image of size  $M \times N$  ( $i = 1, 2, \dots, M$  and  $j = 1, 2, \dots, N$ ). The two dimensional moments and central moments of order  $(p + q)$  of  $f(i,j)$ , are defined as:

$$m_{pq} = \sum_{i=1}^M \sum_{j=1}^N i^p j^q f(i, j) \quad (1)$$

$$U_{pq} = \sum_{i=1}^M \sum_{j=1}^N (i - \bar{i})^p (j - \bar{j})^q f(i, j) \quad (2)$$

Where  $\bar{i} = \frac{m_{10}}{m_{00}}$  and  $\bar{j} = \frac{m_{01}}{m_{00}}$

$$\phi_1 = \eta_{20} + \eta_{02} \quad (3)$$

$$\phi_2 = (\eta_{20} - \eta_{02})^2 + 4\eta_{11}^2 \quad (4)$$

$$\phi_3 = (\eta_{30} - 3\eta_{12})^2 + (3\eta_{21} - \eta_{03})^2 \quad (5)$$

$$\phi_4 = (\eta_{30} + \eta_{12})^2 + (\eta_{21} + \eta_{03})^2 \quad (6)$$

Where  $\eta_{pq}$  is the normalized central moments defined by:

$$\eta_{pq} = \frac{U_{pq}}{U_{00}^r}$$

#### B. Example of Invariant Properties

Fig. 4 shows an image containing letter ‘A’, rotated and scaled, translated and noisy versions of it. There respective moment invariants calculated using formulas using Equations (1) to (6) and 3 other equations not defined in this paper are shown in Table 1.

It is obvious from Table 1 that the algorithm produces the same result for the first three orientations of letter ‘A’ despite the different transformations applied upon them. There is only one value, i.e.  $\Phi_1$ , displays a small discrepancy of 5.7% due to the difference in scale. The other values of the three figures are effectively the same for  $\Phi_2$ ,  $\Phi_3$ ,  $\Phi_4$ ,  $\Phi_5$ ,  $\Phi_6$  and  $\Phi_7$ . The last letter, however, reveals the drawback of the algorithm: it is susceptible to noise. Specifically, the added noisy spot in the letter has changed the entire moment invariants set. This drawback suggests that moment invariants can only be applied on noise-free images in order to achieve the best results. Since the algorithm is firmly effective against transformations, a simple classifier can exploit these moment invariants values to differentiate as well as recognize the letter ‘A’ from other letters. In this paper, we have used these first 4 moment invariants to compare similar regions rather than calculating similarity between every pixel using correlation.

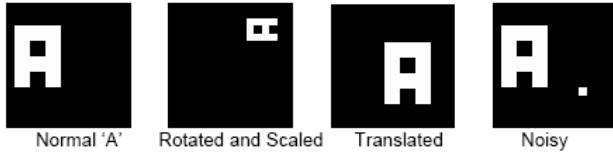


Figure 4. Letter 'A' in different orientations

TABLE I. MOMENT INVARIANT VALUES FOR 'A'

	A1	A2	A3	A4
$\Phi_1$	0.2165	0.2165	0.204	0.25153
$\Phi_2$	0.001936	0.001936	0.001936	0.002161
$\Phi_3$	3.69E-05	3.69E-05	3.69E-05	0.004549
$\Phi_4$	1.64E-05	1.64E-05	1.64E-05	0.002358
$\Phi_5$	-4.03E-10	-4.03E-10	-4.03E-10	7.59E-06
$\Phi_6$	7.21E-07	7.21E-07	7.21E-07	7.11E-05
$\Phi_7$	0	0	0	1.43E-06

In the algorithm, each block containing at least one 'feature' will be compared with the other blocks in the same horizontal region of the other image. Since only 4 values are compared per block against 400 such comparisons in the case of correlation, the computational saving will be immense and will lead to faster depth computations. The algorithm is moderately easy to implement and requires only a moderate computational effort from the CPU. Feature extraction, as a result, can be progressed rapidly and efficiently. The summary of the proposed technique is presented in Figure 5.

If certain blocks do not contain any features, the search area in the other image (Right) can be restricted using maximum disparity constraint. This will further cut down the computational requirements as opposed to area-based correlation techniques.

#### IV. EXPERIMENTAL RESULTS

We ran the proposed algorithm on 100 stereo pairs generated using a BumbleBee™ stereo rig mounted on a mobile robot producing 320x240 pixel frames. The path the robot covered had special markers to provide feature points as most of the cubicles of the indoor setup had monotonous flat featureless walls and partitions. This was followed by running correlation based stereo matching algorithm using SSD and SAD metrics. The results are shown in Fig. 6. The processing system comprised of a Pentium 4 system running at 2GHz with 2GB of RAM. The system was capable of processing 10 frames per second for both moment invariant based approach and correlation based technique using SAD metric however, it only managed 5 frames per second using SSD. This was expected as the SSD involved more computational complexity compared to SAD. However, it should be pointed out that the proposed approach computed handful of disparity values. We also used the Zitnick-Kanade algorithm to estimate the disparity even though the results are not presented due to the inability of the algorithm to run anywhere near realtime with our modest processing power. Since this algorithm expects multiple iterations to refine its estimates, it is simply not useful for

realtime applications that we are interested in. Fig. 5 summarizes the major steps in the proposed algorithm.

The major advantage of local approaches presented here is speed and suitability for hardware implementation. Global optimization algorithms commonly require 2 to 3 orders of magnitude more time than even the software implementations of local methods.

#### V. SUMMARY

In many respects feature based algorithms are established as the most robust way to implement stereo vision algorithms for the industrial-type stereo problems. The advantages offered by using features are that feature-based representations contain desirable statistical properties and provide algorithmic flexibility to the programmer. The flexibility being that algorithmic constraints can be applied explicitly to the data structures rather than implicitly as with area based correlation techniques. In particular the use of 'corners' leads to algorithms which are as locally accurate as the precision to which the edges can be extracted.

Even though, feature-based techniques do not produce denser disparity map, their values are more accurate than the area-based techniques. Some of the reasons for this is that presence of shadows produce erroneous results; some surfaces were non-uniformly reflecting light from; backgrounds are usually flat single-colored surfaces and some parts of the first image were occluded in one of the images .

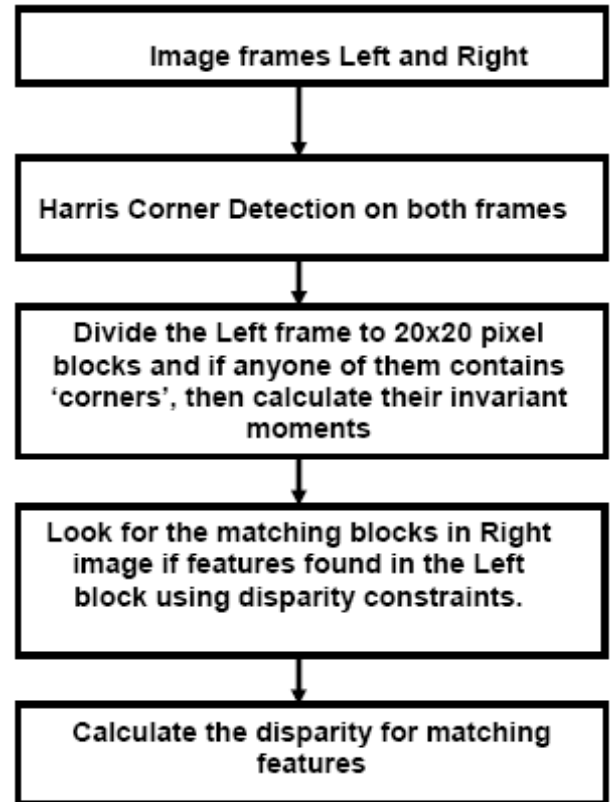


Figure 5. Summary of the proposed technique

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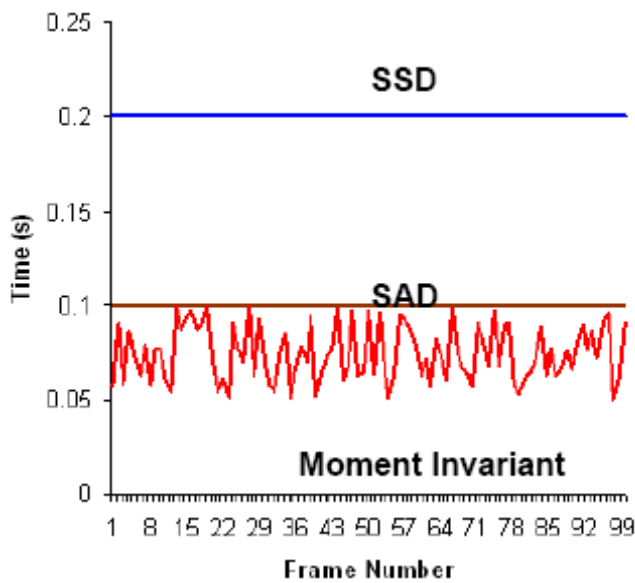


Figure 6. Comparison of Moment Invariant technique with correlation method using SSD and SAD metrics

We managed to demonstrate that feature-based techniques relying on moment invariants for matching can process a frame in the order of tenths of seconds in software implementations. This implies that the algorithm can comfortably reach higher video rates using DSP and FPGA implementations [22]. At the moment, there is no technique for achieving simultaneously the high quality range obtained from global optimization with the fast run-times of local schemes.

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