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Strengthening square reinforced concrete columns by circularisation and FRP confinement

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Keywords
confinement, circularisation, columns, concrete, reinforced, frp, square, strengthening

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Strengthening Square Reinforced Concrete Columns by Circularization and FRP Confinement

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Abstract

A technique called circularization where segmental circular concrete covers made of different concrete strengths (40 MPa, 80 MPa and 100 MPa) was used to change a square column to a circular column. The applicability of the circularization method was experimentally studied for a wide range of concrete strengths (from 40 MPa to 100 MPa). The behaviour of the strengthened specimens under different loading conditions including concentric loading, eccentric loading (25 mm and 50 mm) and flexural bending is investigated. The experimental results demonstrate that using high strength concrete (HSC) for the additional covers to strengthen existing square reinforced concrete (RC) columns provides higher load-carrying capacity than covers made of normal strength concrete. The HSC covers and the concrete cores worked as a composite material to failure. The FRP strain at peak load was observed for the purpose of estimating the specimens’ capacity. The distribution of FRP strain around the circumference of the column section is also reported.

Keywords: Fibre reinforced polymer; Eccentric load; Strengthening; Strain distribution; Shape modification; Square columns.

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1. **Introduction**

Using fibre reinforced polymer (FRP) to strengthen existing reinforced concrete (RC) columns has been proven to increase the strength, stiffness and ductility of the strengthened columns. Most of the existing columns are square or rectangular in cross sections, which reduce the effectiveness of FRP confinement. Thus, it is believed that shape modification technique in which a square column is changed to a circular column before wrapping with FRP improves the confinement effect. This shape modification idea had been explored by Priestley and Seible [1].

In their approach, precast concrete bolsters were bonded to obtain a circular or elliptical section before wrapping with FRP sheets. Using fast-cured cement inside FRP straps was also utilized to modify cross sections of columns by Saadatmanesh et al. [2] while post-tensioned FRP shells were carried out as another shape modification technique by Yan and Pantelides [3]. The shear strength, flexural ductility and lap-slice performance of the retrofitted columns under seismic loads were investigated in the studies by Priestley and Seible [1] and Saadatmanesh et al. [2].

No axial load capacity was investigated in the above papers. Hadi et al. [4] proposed a new technique for strengthening an existing square column by circularizing with four precast segmental circular concrete covers and then wrapping them with FRP. The columns were tested under concentric loading, eccentric loading and flexural bending. The results indicated that this technique significantly improves the strength and ductility of the strengthened columns.

As a result, there are two ways to strengthen a square RC column by wrapping with FRP. The first common method is to round the corners of the column and then wrap it with FRP. The second method is to use the proposed method, which does not need to round the corners. So, the
proposed technique reduces labour-works by not rounding the corners, which must be conducted on site in real structures. On contrast, casting the segmental covers is constructed in a factory which may reduce the labour cost and increase the quality control. Therefore, the method proposed by Hadi et al. [4] is promising for the practical engineering.

Sequentially, the studies above have shown that a combination of shape modification and FRP has been used to successfully strengthen existing square RC columns. Hadi et al. [4] made the same concrete strength for both the column core and the precast segmental covers. This study uses high strength concrete (HSC) in the covers to increase the load carrying capacity of columns. However, using HSC leads to different behaviours between the concrete core and the segmental concrete covers. Also, HSC was found to achieve lower effective confinement than normal strength concrete [5]. Therefore, this study investigates the applicability of the proposed method for existing square RC concrete columns strengthened by HSC segments and FRP. The compressive concrete strength of the column cores was 40 MPa while the segmental covers had compressive design strength of 40 MPa, 80 MPa to 100 MPa. The capacity, ductility and failure modes of the columns were investigated. In addition, load – deflection response and strain distribution of FRP around the tested columns were also studied.

2. Confined Concrete and Interaction Diagrams

2.1. Confined Concrete

The confinement model was firstly reported based on tri-axial tests of small plain concrete cylinders. Richart et al. [6] proposed the following linear relationship between the confined concrete strength and the confining pressure:
where $f'_{cc}$ is the strength of confined concrete, $f'_{co}$ is the strength of unconfined concrete, $f_l$ is the confining pressure, and $k_1$ is a coefficient that is a function of lateral pressure and cross sections, which was taken as 4.1. This model is based on active confinement to calculate the strength of confined concrete. Richart et al. [7] also found that the confined concrete strength with passive confinement pressure was same as the strength of concrete with active confinement from lateral hydraulic pressure. Mander et al. [8] suggested the following nonlinear relationship based on the ultimate strength surface:

$$f'_{cc} = f'_{co} \left( -1.254 + 2.254 \sqrt{1 + \frac{7.94f_l}{f_{co}} - 2 \frac{f_l}{f_{co}}} \right)$$

Mander et al. [8] proposed the above model based on the experiments of steel confined concrete. This model was adopted by ACI 440.2R-02 [9] to design externally bonded FRP systems for strengthening concrete structures. However, using this model to calculate the strength of FRP confined concrete was inappropriate [10]. As a result, several studies proposed confinement models, which exhibited a reasonable agreement with experimental results, for FRP confined concrete [11-15]. Lam and Teng’s model [11] was adopted herein to calculate the strength of the specimens, as follows:

$$\frac{f'_{cc}}{f_{co}} = 1 + 3.3 \frac{f_{l,a}}{f_{co}}$$

where is the effective confining pressure, which can be estimated by:

$$f_{l,a} = k_e \frac{2f_{fe}t}{d}$$
where and \( t \) are respectively the rupture stress and the thickness of FRP, \( d \) is the diameter of a column, and \( k_e \) is the FRP strain efficiency factor which was defined by Harries and Carey [16] and then taken as 0.586 by Lam and Teng [11].

Unfortunately, Lam and Teng’s model [11] is applicable for concrete having unconfined compressive strength less than 55 MPa while this study used concrete with compressive strengths ranging between 40 MPa and 100 MPa. A model for FRP confined HSC is necessary for estimating the strength of confined concrete made of HSC. Models for FRP confined HSC do not show a significant difference from models for normal strength concrete. Thus, the model proposed by Lam and Teng [11] was used to calculate the confined concrete strength of all tested columns.

The confinement mechanism of the tested columns is very complicated when NSC is used in column cores and HSC in the segmental covers. This combination may cause different confinement efficiency [5]. The concrete of the column cores and the segmental covers has differences in the axial concrete stiffness and the axial strain at peak load. These differences lead to inconsistency in transferring the applied load to the core and the covers. The different behaviours of the tested columns are investigated experimentally and the nominal confined concrete strength was calculated as follows:

\[
f'_{cc} = \frac{f'_{cc1}A_1}{A_1 + A_2} + \frac{f'_{cc2}A_2}{A_1 + A_2}
\]

where \( f'_{cc1} \) and \( f'_{cc2} \) are respectively the confined concrete strength of the column core and the segmental covers, and \( A_1 \) and \( A_2 \) are the cross sectional area of the column core and the total cross sectional area of the segmental covers.
2.2. Interaction diagrams

ACI-440.2R [17] suggested that interaction diagrams for FRP confined concrete columns could be established using simple sectional analysis procedures developed for RC concrete columns. Such diagrams must satisfy strain compatibility and force equilibrium. The only difference for establishing interaction diagrams for FRP confined concrete columns is the use of a FRP confined concrete stress–strain curve instead of the stress–strain curve for unconfined concrete. Two methods were adopted to analyse the interaction diagrams as suggested by Hadi et al. [4]. However, this study only reports the “equivalent method”, which provides a closer estimation with the experiments, to verify the experimental results.

A theoretical axial load – bending moment interaction diagram includes four points: (a) the pure axial condition; (b) the condition where the strain at the extreme compression fibre is equal to the ultimate confined concrete strain and the strain at the extreme tension fibre is zero; (c) the balanced condition where the strain at the extreme compression fibre is equal to the ultimate confined concrete strain and the steel bar nearest to the tensile face has just yielded in tension; and (d) the pure flexural condition.

The axial load \((P)\) proposed by ACI-440.2R [17] was calculated as follows:

\[
P = 0.85f_{cc}'(A_g - A_s) + f_y A_s
\]

where \(A_g\) and \(A_s\) are respectively the cross sectional area of the column and the longitudinal reinforcement, and \(f_y\) is the yield stress of the longitudinal reinforcement.
For combining the axial compressive and flexural behaviour, this procedure adopted the Whitney stress block assumptions to make the force equilibrium in the FRP confined concrete columns. The Whitney stress block was used to transfer non-uniform compressive confined concrete stresses to rectangular distribution of stresses in accordance with AS 3600 [18].

3. Experimental Program

3.1. Design of Specimens

Sixteen identical square RC specimens were cast to have a cross-section with 150 mm in sides and 800 mm in height. All specimens had identical internal steel reinforcement and were designed according to AS 3600 [18]. Each specimen was reinforced with four N12 (12 mm diameter deformed bars) as longitudinal bars and R6 (6 mm diameter plain bars) ties at 60 mm spacing. The columns were made of normal strength concrete with a design compressive strength of 40 MPa, which was supplied by a local supplier. The high strength concrete (80 MPa and 100 MPa) was designed and mixed at the University of Wollongong. Concrete cover was maintained at 20 mm on all sides including the top and bottom of the specimens. CFRP used as a confinement material was 75 mm in width with a uni-directional fibre density of 340 g/m². The nominal tensile strength of the materials was not specified by the suppliers and therefore preliminary tests were carried out to investigate the mechanical properties of CFRP and reinforcement as explained below.
3.2. Test Configuration

All tests were carried out at the laboratories of the School of Civil, Mining and Environmental Engineering, University of Wollongong. The specimens were subdivided into four groups. The first group (Group R) was set as a reference group with no further modification and strengthening. The columns of the other three groups were bonded with four segmental circular concrete covers to modify the cross section from square to circle. The concrete strength of the additional segments of these groups was unique for each other. Based on the strength (in MPa) of the additional segments, these groups were named as Groups C40, C80 and C100 indicating covers have design compressive strengths of 40, 80 and 100 MPa, respectively. It is noticed that the compressive concrete strengths reported in Table 1 are the actual values. The modified columns were then wrapped with three CFRP layers.

From each group, the first specimen was subjected to an axial concentric load and the next two specimens were tested with 25 mm or 50 mm eccentric loading. The last specimen was tested under a four-point loading regime. The specimens were labelled based on the compressive strength of the covers followed by the loading condition. For examples, Specimen C80-50 had an 80 MPa compressive strength of the covers and was tested under 50 mm eccentricity. Table 1 shows the test matrix used in this study and the details of the specimens are shown in Fig. 1.

3.3. Specimen Fabrication

Two plywood formworks were used to construct the column cores and the segmental circular concrete covers. For the segmental circular concrete covers, a box of 34 rectangular
segments having a dimension of 51x170 mm² was built. A section mould of foam was added to each rectangular segment in order to create a mould for the concrete covers. Each segmental circular concrete cover had a chord of 150 mm (equal to the side length of the column core) and the height of the segment was 31 mm.

3.3.1. Circularisation Process

The segmental circular concrete covers were taken out of the formwork after 28 days. The foams on the covers were first removed and the surface of the segments was ground and cleaned to be smooth. Before bonding the segments, the column surface was cleaned and any dust was removed. The adhesive was a mix of epoxy resin, slow hardener and silica microsphere with a ratio of 5:1:10. The adhesive was evenly spread onto the segment surface, which were then bonded onto the column surface. The epoxy resin had 54 MPa tensile strength, 2.8 GPa tensile modulus, and 3.4% tensile elongation [19].

Four segmental circular concrete covers were bonded on the surface of a column to modify the shape of the cross section from square to circle. After the segments were bonded, adjustable steel straps were used to hold them. The modified specimens were then left to dry for three days before they were externally confined. Fig. 2 illustrates details of the circularisation process. In practice, the surface of the column cores and the segments may not fit together because of construction errors. As a result, any effort of bonding the segments to the column core causes cracking of the segments. Fiber reinforced segments should be used in such cases to provide ductile structural elements.
3.3.2. Construction of External Confinement

Wet-layup method was used to wrap the specimens with CFRP using epoxy resin. The specimens were confined with separate CFRP rings. Firstly, epoxy resin was spread onto the specimen surface and the first CFRP layer was attached. Next, epoxy resin was spread again on the surface of the first CFRP layer and the second layer was attached. The same procedure was followed until three CFRP layers were bonded with a notice that 100 mm overlap was maintained at the third layer. An additional layer of CFRP was wrapped at both ends of the specimens to prevent premature damage at the ends. The specimens were then left to dry for three days as specified by the supplier.

3.4. Preliminary Tests

The compressive concrete strength was recorded at 28 days, 56 days and at the testing time. Since the specimens were tested at different ages, three cylinders were tested on the same day of testing the specimen to determine the compressive concrete strength at that time. Table 1 summarizes the average compressive concrete strength of the tested columns during testing time. To determine the mechanical properties of CFRP, CFRP flat coupon tests were conducted according to ASTM D7565 [20]. The average width of the coupons was 25.6 mm and the average maximum tensile force per unit width was 2089 N/mm. The strain at the average maximum tensile force and the average elastic modulus were 0.0174 mm/mm and 121 kN/mm, respectively. The average tensile strength of N12 and R6 was respectively 568 MPa and 478 MPa.
3.5. Instrumentation and Test Procedure

Strain gauges were horizontally attached onto the CFRP surface to investigate the actual strain of CFRP at the critical locations around the circumference of the column sections. Four strain gauges were symmetrically bonded in all concentrically loaded columns while each beam specimen had two strain gauges, one at the compression and one at the tension regions. Meanwhile, each eccentrically loaded column had ten strain gauges which were used to observe the strain distribution at the middle CFRP ring. Because of the significance of the FRP strain in the compression region, more strain gauges were concentrated in this region. The strain gauges were then connected to a data logger and a control computer. Details of the positions of strain gauges are shown in Fig. 3.

A specific loading system was used to conduct eccentric loading tests. Detailed description of the loading system could be found in Hadi and Widiarsa [21]. For flexural tests, two four-point loading frames were used. The “square” four-point loading frame introduced by Hadi and Widiarsa [21] was used for Specimen R-F while the “circular” four-point loading frame used by Yazici and Hadi [22] was used for Specimens C40-F, C80-F and C100-F.

Axial deflection of the columns was monitored by a Linear Variable Differential Transformer (LVDT) attached to the lower moving plate of the compression machine. In order to measure the lateral deflection of the eccentrically loaded columns and midspan deflection of the flexural tests, a laser triangulation sensor was used and connected to the data logger as well. For the column tests, the laser triangulation sensor was set up at mid-height of the columns. For the beam tests, the laser triangulation sensor was placed on a hole located at midspan of the beam.
bottom loading plate. The Denison 5000 kN testing machine was used for testing all of the specimens. The tests were conducted as deflection controlled with a rate of 0.3 mm/min. All columns were capped at both ends by using high strength plaster to ensure even distribution of forces. Calibration was carried out to ensure the specimens were placed at the centre of the machine.

**Experimental El t an i on**

All Specimens were tested to failure. The load and displacement data were collected using the data logger connected to the compression machine.

*4.1. Failure Modes*

For concentrically loaded columns, Column R-0 failed by dedonding of concrete cover and buckling of the longitudinal steels at midheight of the columns. Three confined columns failed in a brittle manner with rupture of FRP and crushing of the concrete covers. FRP ruptured at midheight of the columns with a loud sound. The concrete cover including the segmental circular concrete covers and the concrete cover of the original columns crushed while the concrete core inside the longitudinal steels was still confined as shown in Fig. 4. The columns made of higher concrete strength were observed to fail rather suddenly than the others.

For eccentrically loaded columns, tension cracks in concrete occurred between two FRP rings located at midheight of the columns were found at early stage of the loading. FRP confined concrete columns under eccentric loading failed by FRP rupture followed by concrete crushed at the compression side. The rupture of FRP was always observed at midheight. In this
study, half of the tested columns had two types of concrete having different strengths. These
differences may lead to debonding at the interface between the two types of concrete. Thus, the
tested columns were unwrapped to observe the connection between the additional segments and
the column core. As expected, the bonding between the additional segments and the column
core was good for all columns. Fig. 4 shows Specimen C80-25 after being tested and FRP
peeled off.

Specimens under flexural tests failed by the fracture of longitudinal steels in the tension
side and crushing of the concrete in the compression side. No FRP rupture was observed in the
tests. For Specimen R-F, two types of cracks were observed. Vertical cracks occurred first due
to flexural stresses. These cracks started at mid-span and bottom of the beam and then new
cracks moved to near the ends of the beam. These cracks rapidly opened when the applied load
was reaching the peak load. The inclined cracks near the ends of the beams were observed later
due to shear effect. For Specimens C40-F, C80-F and C100-F, the same cracking pattern was
observed after unwrapping the tested beams as shown in Fig. 5. Additionally, arch action was
found and detailed below in the following sections.

4.2. Load – Deflection Responses

The first column of each group was tested under concentric loading. Fig. 6 shows axial
load versus axial deflection of the columns. The axial load of Specimen R-0 increased to the
peak load at which the longitudinal steel yielded, and then the load decreased to failure. The
shape of the axial load – deflection diagrams of the confined columns shown in Fig. 6 is
identical to each other, which is a bi-linear increase. The first portion of the diagrams quickly

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increased to the yield load before gradually increasing to the peak load. Then, the specimens
suddenly failed by a very loud sound caused by FRP rupture. Fig. 6 also shows that slopes of the
tested columns (specimen stiffness) are approximately identical in each corresponding stage.
The similarity in slope shows that effects of the additional segment strength on the specimen
stiffness could be negligible. In addition, the higher concrete strength of the segmental covers,
the higher yield load and peak load were obtained. As compared to Specimen R-0, the increase
of the peak load of Specimens C40-0, C80-0 and C100-0 was respectively 261%, 268%, and
286%. The increase of yield load of 16% and 15% was achieved for Specimens C80-0 and
C100-0 compared to Specimen C40-0, respectively. It is commonly assumed that the
confinement effect caused by FRP is negligible at yield load. Thus, the increase of the yield
load of Specimens C80-0 and C100-0 proved that the contribution of the high strength concrete
of the segments. Meanwhile, the increase of the peak load of Specimens C80-0 and C100-0 was
respectively 2% and 7% compared to Specimen C40-0. The increase of the axial load at the
peak load being smaller than at the yield load confirmed that FRP confinement on HSC is less
efficient than normal strength concrete.

The axial load - deflection diagrams of the columns under eccentric loads are plotted in
Figs. 7-8. The shape of the load – deflection diagrams of the eccentrically loaded columns was
different from those of the columns under concentric load. The load – deflection diagrams of
the confined columns under 25 mm eccentric load steadily increased to the peak load, and then
sustained a load before failing by rupturing FRP at the compression side. The increase of the
peak load of Specimens C40-25, C80-25 and C100-25 compared to Specimen R-25 was 129%,
155% and 162%, respectively. As shown in Fig. 7, the increase of the axial deflection and
lateral deflection is quite similar before reaching the peak load. The lateral deflection then increased much faster than the axial deflection as the axial load was sustained.

The axial load - deflection diagrams of the specimens under 50 mm eccentric load are shown in Fig. 8. The increase of the peak load of Specimens C40-50, C80-50 and C100-50 compared to Specimen R-50 was 139%, 178% and 175%, respectively. It is confirmed that the efficiency of FRP confined concrete decreases when eccentricity was introduced. Additionally, the axial load of Specimens C80-50 and C100-50 fluctuated after the peak load, which resulted from redistribution and rearrangement of the micro structures inside the columns. This phenomenon did not occur in Specimen C40-50 having the same concrete strength between the column core and the segmental circular concrete covers. In terms of deflection, unlike the specimens tested under 25 mm eccentric load, the increase of the lateral deflection of specimens under 50 mm eccentricity was higher than that of the corresponding axial deflection at all stages.

Fig. 9 shows the load – midspan deflection diagrams of the tested beams under flexure. The beams wrapped with FRP exhibit a large increase in their load-carrying capacity compared to the reference beam. The load – midspan deflection diagrams of the beams confined with FRP exhibit an ascending branch after yielding.

4.3. Strain Distribution of FRP

FRP rupture was observed at two potential locations: the extreme compression fibre for the eccentrically loaded columns, and the positions close to the corners of the column core and out of the overlap region for the concentrically loaded columns.
For columns under concentric loads, the FRP strain at the yield load was approximately 0.0014, which was an average reading of the strain gauges out of the overlap zone, while the FRP strain at the peak load was 0.012. Those strains confirmed an assumption that FRP effect at the yield load could be negligible as the FRP strain at that stage was 8% of the ultimate strain of FRP from flat coupon tests. The FRP strain efficiency factor, defined as the ratio of the actual rupture strain and the ultimate strain of FRP from flat coupon tests, of the tested columns was 0.7. The axial load - FRP strain diagrams of the concentrically loaded columns are plotted in Fig. 10. The FRP of the concentrically loaded columns always ruptured at the peak load.

Conversely, the FRP of eccentrically loaded columns did not rupture at the peak load. Fig. 11 shows the axial load – FRP strain diagrams at the extreme compression region, which is Position 1 (S1) in Fig. 3b. The peak load occurred at very early stage as observed in Specimen C100-50, where the FRP strain was 0.0014 at the peak load and 0.0116 at the ultimate load. Otherwise, the FRP strain of Specimen C100-25 was 0.0098 at the peak load and 0.0144 at the ultimate load. As shown in Fig. 11, the FRP strain at the peak loads varied from 12% to 68% of the FRP strain at rupture. In this study, the FRP strain efficiency factor of specimens under eccentric load was 0.72, in which the actual rupture strain of FRP was the strain reading at Position 1 (S1) as shown in Fig. 3b.

Fig. 12 shows the distribution of FRP strain around the circumference of Column C80-25. The FRP strain of Column C80-25 illustrates a pattern of strain distribution for eccentrically loaded columns. The FRP strain was the highest at Position 1 (S1) and then regularly declined till Position 6 (S6). It is believed that no confinement effect resulted from FRP is available at the
tension region in a column. Interestingly, the FRP strain was not negligible at Location 6 as shown on the “ultimate load” line in Fig. 1. Thus, the FRP strain at Position 6 could not result from confinement effect, but caused by stretching the FRP from the compression region in the column section.

4.4. Ductility

Ductility of the tested specimens was calculated as the ratio of the deflection at 85% post-peak load ($\delta_u$) and the yield load ($\delta_y$) as described in Eq. 7 and summarised in Tables 2-3.

$$\lambda = \frac{\delta_u}{\delta_y} \quad (7)$$

The deflection at 85% post-peak load was determined by the deflection corresponding to the axial load dropping to 85% of the peak load. The definition of the yield load was adopted from Pessiki and Pieroni [23], which was obtained as follows. A best-fit line to the linear portion of the load – deflection diagram for each specimen was implemented. This line was then extrapolated to intersect with the maximum load sustained by the column. The load corresponding to this intersection is the yield load. In addition, the axial load – deflection graphs of the concentrically loaded columns had the ascending branch after yielding. Thus this approach was inappropriate in these cases. Determining the yield loads of such specimens was modified. Two best-fit lines for the two linear portions of the diagrams were made, and then the yield load was determined by an intersection of the two above lines.

Tables 2 - 3 show that the confined columns exhibited higher ductility relative to the reference columns. The concrete strength of Groups C80 and C100 was designed to have
different strengths. However, the concrete strength of these groups was quite similar, thus their
behaviours were very similar. The ductility of the columns tested by the same condition of
Groups C40, C80 and C100 was quite similar. This behaviour demonstrates that the influence
of the concrete strength of the segments on ductility of FRP confined columns is negligible.

4.5. Interaction Diagram

The experimental interaction diagrams in this study were drawn based on four points: (1) a pure axial load of the columns under concentric loads, (2) two points of eccentric loads of 25
mm and 50 mm, where the axial loads were recorded from the testing machine and the bending
moments were calculated by Eq. 8, and (3) a pure bending moment observed from the
four-point loading tests. The experimental interaction diagrams are shown in Fig. 13.

\[ M = P_{\text{max}} (e + \delta) \]  

(8)

where \( P_{\text{max}} \) is the peak axial load, \( e \) is the original eccentricity, and \( \delta \) is the lateral deflection at
the peak load.

The theoretical interaction diagrams were established to describe the axial load and
bending moment capacity of the tested columns. The actual rupture strain of FRP on the tested
columns was different than the value suggested by ACI-440.2R (2008). As mentioned above,
the columns under eccentric loads reached the peak load as the FRP strain was much lower than
the rupture strain observed at the ultimate load. In this study, the FRP strain was set as 0.7 for
concentrically loaded columns and 0.34 for columns under eccentric loads. Fig. 14 shows the
experimental - theoretical interaction diagrams of the tested columns.
Fig. 14 demonstrates that using the proposed procedure to calculate the interaction diagrams provides good agreement with the experimental results. The differences between the theoretical and experimental results were 7.25% and 3.05% for concentrically and eccentrically loaded columns, respectively. In order words, the estimation of the bending moment did not show good agreement with the experimental results because of the following reasons.

Specimen R-F failed with flexural behaviour evidenced by vertical cracks. Thus, the experimental bending moment of this beam is close to the calculation as shown in Fig. 14. Meanwhile, the specimens wrapped with FRP under flexural tests failed in a manner of a combination of flexure and shear as shown in Fig. 5 showing the vertical and inclined cracks. The inclined cracks were resulted from the arch action which resulted in the increase of the beam capacity. The availability of the arch action was confirmed by the FRP strain. When the vertical cracks, which were signs of flexural behaviour, occurred and opened quite large, the FRP strain was still negligible at the compression region. However, when the vertical cracks stopped developing, the FRP strain increased quickly to the value of 0.006 at such zone. To maintain equilibrium, it is assumed that a strut resulted from the arch action carried the increased load.

The proposed strengthening technique was used to modify a square section to a circular section before wrapping with FRP. This technique could be utilized to improve significantly the capacity of a square column. Two concrete components including the original concrete core and the additional concrete covers worked as a composite material to failure under pure axial load,
flexure, and eccentric loads. The bonding of two components observed after testing was perfect bond. Thus, it is concluded that the proposed technique is able to improve the capacity of a noncircular column.

The ductility of the strengthened columns significantly increased compared to the reference columns since FRP has the same full confinement effect on the tested columns as on a conventional original circular column.

This study also verified the application of the proposed technique for a variety of concrete strength up to 100 MPa. The experiments demonstrated that this technique could be used not only for normal strength concrete but for high strength concrete. Bonding high strength concrete covers to the column core with low concrete strength was successfully verified.

The FRP strain was recorded during the loading process. The rupture strain of FRP on the concentrically loaded columns was around 0.7 of the ultimate strain from flat coupon tests. The FRP strain at the peak load of the eccentrically loaded columns was much smaller than the rupture strain at the ultimate load. The measured FRP strain at the peak load was approximately 0.34 of the ultimate strain from flat coupon tests. This value should be used to estimate the capacity of a FRP confined concrete column under eccentric loads. In addition, distribution of FRP strain around the tested columns was also investigated. The distribution describes a decrease of FRP strain from the extreme compression fibre to the tension side of a column.

Finally, the proposed method proved to be effective in increasing the load-carrying capacity of FRP confined square column with normal strength concrete by Hadi et al. [4].
study verifies this method with HSC and proposes the actual FRP strain to calculate the
capacity of FRP confined columns under both concentric and eccentric loads.

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1. **Figure 1.** Cross section of specimens (units in mm)

2. **Figure 2.** Circularization process (a) Removal of the segments from the formworks; (b) Removal of foams attached on the covers; (c) Bonding of segments; and (d) Bonded specimens

3. **Figure 3.** Details of strain gauge locations

4. **Figure 4.** Failure modes of the tested columns

5. **Figure 5.** Failure patterns of the tested beams

6. **Figure 6.** Axial load – deflection diagrams of the concentrically loaded columns

7. **Figure 7.** Axial load – deflection diagrams of the eccentrically loaded columns (e = 25 mm)

8. **Figure 8.** Axial load – deflection diagrams of the eccentrically loaded columns (e = 50 mm)

9. **Figure 9.** Load – deflection diagrams of the beams

10. **Figure 10.** Axial load – FRP strain diagrams of the concentrically loaded columns

11. **Figure 11.** Axial load – FRP strain at the extreme compression fibre diagrams

12. **Figure 12.** Strain distribution around the circumference of Column C80-25

13. **Figure 13.** Experimental interaction diagrams for the tested columns

14. **Figure 14.** Experimental and theoretical interaction diagrams for the tested columns
Table 1. Test matrix

Table 2. Summary of the tested columns under concentric loads

Table 3. Summary of the tested columns under eccentric loads
Table 1. Test matrix

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Concrete Core Strength at test time (MPa)</th>
<th>Concrete Cover Strength at test time (MPa)</th>
<th>External Confinement</th>
<th>Test Eccentricity</th>
</tr>
</thead>
<tbody>
<tr>
<td>R-0</td>
<td>44</td>
<td>-</td>
<td>-</td>
<td>0</td>
</tr>
<tr>
<td>R-25</td>
<td>44</td>
<td>-</td>
<td>-</td>
<td>25</td>
</tr>
<tr>
<td>R-50</td>
<td>44</td>
<td>-</td>
<td>-</td>
<td>50</td>
</tr>
<tr>
<td>R-F</td>
<td>44</td>
<td>-</td>
<td>-</td>
<td>Flexural</td>
</tr>
<tr>
<td>C40-0</td>
<td>58</td>
<td>58</td>
<td>3 CFRP layers</td>
<td>0</td>
</tr>
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<td>C40-25</td>
<td>58</td>
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<td>3 CFRP layers</td>
<td>25</td>
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<tr>
<td>C40-50</td>
<td>58</td>
<td>58</td>
<td>3 CFRP layers</td>
<td>50</td>
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<tr>
<td>C40-F</td>
<td>58</td>
<td>58</td>
<td>3 CFRP layers</td>
<td>Flexural</td>
</tr>
<tr>
<td>C80-0</td>
<td>59</td>
<td>98</td>
<td>3 CFRP layers</td>
<td>0</td>
</tr>
<tr>
<td>C80-25</td>
<td>59</td>
<td>98</td>
<td>3 CFRP layers</td>
<td>25</td>
</tr>
<tr>
<td>C80-50</td>
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<tr>
<td>C80-F</td>
<td>59</td>
<td>98</td>
<td>3 CFRP layers</td>
<td>Flexural</td>
</tr>
<tr>
<td>C100-0</td>
<td>63</td>
<td>101</td>
<td>3 CFRP layers</td>
<td>0</td>
</tr>
<tr>
<td>C100-25</td>
<td>63</td>
<td>101</td>
<td>3 CFRP layers</td>
<td>25</td>
</tr>
<tr>
<td>C100-50</td>
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<td>63</td>
<td>101</td>
<td>3 CFRP layers</td>
<td>Flexural</td>
</tr>
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</table>
Table 2. Summary of the tested columns under concentric loads

<table>
<thead>
<tr>
<th>Specimens</th>
<th>R-0</th>
<th>C40-0</th>
<th>C80-0</th>
<th>C100-0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Yield load (kN)</td>
<td>892</td>
<td>2109</td>
<td>2452</td>
<td>2418</td>
</tr>
<tr>
<td>Corres. Axial Def. (mm)</td>
<td>3.88</td>
<td>2.57</td>
<td>3.39</td>
<td>3.85</td>
</tr>
<tr>
<td>Ultimate load (kN)</td>
<td>942</td>
<td>3400</td>
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<td>3634</td>
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<tr>
<td>Corres. Axial Def. (mm)</td>
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<td>13.75</td>
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<td>17.99</td>
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<tr>
<td>Ductility</td>
<td>1.48</td>
<td>5.45</td>
<td>4.05</td>
<td>5.03</td>
</tr>
<tr>
<td>Specimens</td>
<td>R-25</td>
<td>C40-25</td>
<td>C80-25</td>
<td>C100-25</td>
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<tr>
<td>--------------------</td>
<td>------</td>
<td>--------</td>
<td>--------</td>
<td>---------</td>
</tr>
<tr>
<td>Yield load (kN)</td>
<td>600</td>
<td>1423</td>
<td>1558</td>
<td>1585</td>
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<tr>
<td>Corres. Axial Def. (mm)</td>
<td>2.47</td>
<td>3.47</td>
<td>2.57</td>
<td>2.79</td>
</tr>
<tr>
<td>Ultimate load (kN)</td>
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<td>1513</td>
<td>1762</td>
<td>1741</td>
</tr>
<tr>
<td>Corres. Axial Def. (mm)</td>
<td>2.88</td>
<td>5.93</td>
<td>5.52</td>
<td>4.79</td>
</tr>
<tr>
<td>Corres. Lateral Def. (mm)</td>
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<td>7.76</td>
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<tr>
<td>Ductility</td>
<td>1.22</td>
<td>3.92</td>
<td>3.55</td>
<td>3.27</td>
</tr>
</tbody>
</table>
Figure 1

Group R
(Reference Group)

Group C40
(Circularization + CFRP)

Group C80
(Circularization + CFRP)

Group C100
(Circularization + CFRP)

4N12
R6@60

$\sigma_{co}$
40 MPa

Concrete covers

$\sigma_{co}$
80 MPa

$\sigma_{co}$
100 MPa

$\varnothing$ 212

CFRP

CFRP

Concrete covers
(a) Concentrically Loaded Column

(b) Eccentrically Loaded Column

(c) Beam specimen
Specimen C40-0

Specimen C80-25

Specimen C80-25
After peeling off the FRP

Bonding between the additional segments and the column core
Figure 7
Figure
The flax flat coupon tests (1.74%) and strain of FRP (%)

Figure
Figure
Figure 12

(a) Strain Gage Positions

(b) FRP Strain

(c) Distribution of FRP strain of Specimen C80-25

- Yield load
- Peak load
- Ultimate load

Strain of FRP

Position of strain gages
Figure 1