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A Generic Construction of Identity-Based Online/Offline Signcryption

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Abstract

Signcryption has clear advantage over traditional sign-then-encrypt schemes. However, the computational overhead for signcryption is still too heavy when it is applied to resource-constraint systems. In this paper, we propose a generic construction of the identity-based online/offline signcryption, where most of computations are carried out when the associated message is still unavailable and the online part of our scheme does not require any exponent computations and therefore is very efficient. Our scheme is generic and identity-based, in the sense it is independent of the selection of signature and encryption algorithms. Our scheme possesses the properties of ciphertext indistinguishability (IND-gCCA2) and existentially unforgeability (UF-CMA).

1. Introduction

Signcryption is a cryptographic primitive introduced by Zheng [13] in 1997. The main idea of this primitive is to carry out encryption and signature computations in a single logical step to obtain confidentiality and authentication more efficiently than the simple composition of encryption and signature. Since Zheng’s seminal work, many efficient signcryption schemes have been proposed.

The notion of identity-based cryptography was introduced by Shamir in 1984 [10]. The system is realized by introducing a trusted third party named Private Key Generator (PKG) to produce a user’s private key corresponding to the user’s identity. Shamir proposed an identity-based signature scheme, but for many years identity-based encryption remained an open problem. In 2001, Boneh and Franklin [3] proposed a fully practical and functional identity-based encryption scheme with security proof.

Identity-based notion was introduced to signcryption in 2002. Malone-Lee proposed an identity-based signcryption solution [9]. However, it is not semantically secure. Libert and Quisquater [8] proposed a solution to remedy the problem. Unfortunately, the properties of public verifiability and forward security are mutually exclusive in their scheme. Boyen [4] proposed a Multipurpose Identity-Based Signcryption and gave the security notions for signcryption as: message confidentiality, signature non-repudiation, ciphertext unlinkability, ciphertext authentication, and ciphertext anonymity. Chen and Malone-Lee proposed a more efficient scheme [5] and their scheme provides a full security analysis in the model of [4].

To extend the applicability of signcryption to low-power devices, online/offline signcryption was introduced by An, Dodis, and Rabin [1]. The online/offline notion can be tracked to the earlier work due to online/offline signatures. Even, Goldreich, and Micali [7] proposed the first online/offline signature which is a generic scheme to convert any signature scheme into an online/offline counterpart. Their scheme increases the size of each signature by a quadratic factor, hence, it only makes sense in theoretical aspect. Another generic method to achieve online/offline signing was proposed by Shamir and Tauman [11] in 2001. The main advantage of the latter is that the length of the key and signature are significantly reduced which is much better than the former in practical sense. After that, a much more efficient generic online/offline signature scheme was proposed by Chen et al [6].

The work of online/offline signcryption due to An, Dodis, and Rabin [1] mainly concentrates on the security analysis of general combination of signature and encryption scheme in asymmetric settings. No concrete scheme was provided in [1]. Zhang, Mu, and Susilo [12] proposed the first concrete online/offline signcryption scheme in 2005. In their scheme, the online part does not require any expensive computations so it is very efficient, and moreover, the size of a signature is short since they use the notion of short signature.

Motivation and Contribution

Identity-based online/offline signcryption has potential applicability to low-power devices. The reason is threefold.
Let $P$ be a generator of $G_1$. Assume that there is a bilinear mapping $e : G_1 \times G_1 \rightarrow G_2$. Let an attacker $B$ solve the following problem: Given $(P, aP, bP, cP)$, compute a Bilinear Diffie-Hellman key $e(P, P)^{abc}$ with the help of the Decisional Bilinear Diffie-Hellman (DBDH) oracle, which given $(P, aP, bP, cP, d)$, outputs true if $d = e(P, P)^{abc}$ and false otherwise.

We define $B$’s advantage $\text{Adv}^{\text{GBDH}}_{G_1}(B) = \Pr[B(P, aP, bP, cP) = e(P, P)^{abc}]$. We say an algorithm $B$ $(t, q_b, \epsilon)$ breaks GBDH in $(G_1, G_2)$ if it makes $q_b$ queries in time $t$, $B$ has advantage greater than $\epsilon$ in solving GBDH.

2.3. Chameleon Hash Family

Definition 2. [11] (chameleon hash family) A chameleon hash family consists of a pair $(\mathcal{L}, \mathcal{H})$:

- Assume $\mathcal{L}$ is a probabilistic polynomial-time key generation algorithm that on input $1^k$, outputs a pair $(HK, TK)$ such that the sizes of $HK, TK$ are polynomially related to $k$.
- Assume $\mathcal{H}$ is a family of randomized hash functions. Every hash function in $\mathcal{H}$ is associated with a hash key $HK$, and is applied to a message from a space $M$ and a random element from a finite space $R$. The output of hash function $HK$ does not depend on $TK$.

A chameleon hash family $(\mathcal{L}, \mathcal{H})$ has the following properties:

1. Efficiency: Given a hash key $HK$ and a pair $(m, r) \in M \times R$, $HK(m, r)$ can be computed in polynomial time.
2. Collision resistance: There is no probabilistic polynomial-time algorithm $A$ that on input $HK$ outputs, with a non-negligible probability, two pairs $(m_1, r_1), (m_2, r_2) \in M \times R$ that satisfy $HK(m_1, r_1) = HK(m_2, r_2)$ and $m_1 \neq m_2$.
3. Trapdoor collisions: There is a probabilistic polynomial time algorithm that given a pair $(HK, TK) \leftarrow \mathcal{L}(1^k)$, a pair $(m_1, r_1) \in M \times R$, and an additional message $m_2 \in M$, outputs a value $r_2 \in R$ such that:
   - $HK(m_1, r_1) = HK(m_2, r_2)$.
   - If $r_1$ is uniformly distributed in $R$ then the distribution of $r_2$ is computationally indistinguishable from uniform in $R$.

We now present a construction of chameleon hash family [11] with the elliptic curve analogue. The chameleon hash function is based on discrete logarithm assumption.

(1) Identity-based system avoids distribution of public keys. (2) It allows expensive computation to be carried out in an offline phase. (3) Signcryption achieves encryption and signature in a single logical step to obtain confidentiality and authentication more efficiently than the sign-then-encrypt approach. In this paper, we propose a generic scheme of identity-based online/offline signcryption, where the signing part and encryption part are generic.

Our contributions of this paper are as follows. We first formally define the generic identity-based online/offline signcryption and related security models. We then propose a generic construction of identity-based online/offline signcryption. Our construction is based on chameleon hash function and pairing over elliptic curves. It can achieve authenticity and confidentiality simultaneously in an efficient manner. We also provide a proof that the resultant scheme is indistinguishable against adaptive chosen-ciphertext attacks (IND-gCCA2) and is existentially unforgeable against adaptive chosen-message attacks (UF-CMA). Finally, we present a new generic online/offline broadcast signcryption as an extension.

The rest of this paper is organized as follows. In Section 2, we briefly review the preliminaries required in this paper. In Section 3, we formally define the generic identity-based online/offline signcryption. We present our scheme and prove its security in our model in Section 4 and Section 5. In Section 6, we describe an extension of our scheme to broadcast signcryption. We conclude this paper in Section 7.

2. Preliminaries

2.1. Bilinear Mapping

Let $k$ be a security parameter and $q$ be a $k$-bit prime number. Let $G_1$ and $G_2$ be groups of the same prime order $q$. There is a bilinear map $e : G_1 \times G_1 \rightarrow G_2$ with the following properties:

1. Bilinearity: for all $P, Q \in G_1$ and $a, b \in Z_q^*$, $e(aP, bQ) = e(P, Q)^{ab}$.
2. Non-degeneracy: for any generator $P \in G_1$, $e(P, P) \neq 1$.
3. Computability: there is an efficient algorithm to compute $e(P, Q)$, for $P, Q \in G_1$.

2.2. Security Assumptions

The security of our scheme is based on the intractability of the following problem.

Definition 1. Gap-Bilinear Diffie-Hellman Problem (GBDH) Let $G_1$ and $G_2$ be two groups of the same order $q$. We define $B$’s advantage $\text{Adv}^{\text{GBDH}}_{G_1}(B) = \Pr[B(P, aP, bP, cP) = e(P, P)^{abc}]$. We say an algorithm $B$ $(t, q_b, \epsilon)$ breaks GBDH in $(G_1, G_2)$ if it makes $q_b$ queries in time $t$, $B$ has advantage greater than $\epsilon$ in solving GBDH.
• **System Parameters Generation Algorithm** $\mathcal{L}$: Let $t$ be a prime power, and $E(\mathbb{F}_t)$ an elliptic curve over finite field $\mathbb{F}_t$. Let $\#E(\mathbb{F}_t)$ be the number of points of $E(\mathbb{F}_t)$, and $P$ be a point of $E(\mathbb{F}_t)$ with prime order $q$ where $q\neq \#E(\mathbb{F}_t)$. Denote $\mathbb{G}$ the subgroup generated by $P$. Choose a random element $x \in_R \mathbb{Z}_q^*$, and compute $Y = xP$. The public hash key is $HK = (P, Y)$, and the private trapdoor key is $TK = x$.

• **The Hash Family** $\mathcal{H}$: Given the hash key $HK$, the proposed chameleon hash function $H_{HK} : \mathbb{Z}_q \times \mathbb{Z}_q \to \mathbb{G}$ is defined as follows: $H_{HK}(m, r) \overset{\text{def}}{=} mP + rY$.

3. **Definition and Security Models of Generic Identity-based Online/Offline Signcryption**

3.1. **Definition of Generic Identity-based Online/Offline Signcryption**

**Definition 3.** The generic identity-based online/offline signcryption scheme is comprised of five algorithms: System Parameters Generation, Key Generation, OffSigncrypt, OnSigncrypt, and UnSigncrypt.

1. **System Parameters Generation.** Given a security parameter $k$ as input, the private key generator PKG generates the system’s public parameters $\text{params}$, the master secret key $s$, a chameleon hash family $(\mathcal{L}, \mathcal{H})$ and an identity-based signature scheme $(\mathcal{G}, S, V)$, where $\text{params}$ and $(\mathcal{G}, S, V)$ are published in the system, $s$ is kept as secret by PKG and the chameleon hash family $(\mathcal{L}, \mathcal{H})$ is sent to the designated user.

2. **Key Generation.**
   - Given an identity $ID$ and the master secret key $s$ as input, output $d_{ID}$.
   - On input $1^k$, run the key generation algorithm of the trapdoor hash family $(\mathcal{L}, \mathcal{H})$ to obtain the hash/trapdoor key pair $(HK, TK)$.

3. **OffSigncrypt.** Given $\text{params}$, $ID_S$’s private key $d_{d_{ID_S}}$, hash key $HK_S$ and the receiver’s identity $ID_R$ as input, this algorithm outputs an offline signature $\sigma'$.

4. **OnSigncrypt.** Given a message $m$, receiver’s identity $ID_R$, hash/trapdoor key pair $(HK_S, TK_S)$ and an offline signature $\sigma'$ as input, this algorithm outputs the ciphertext $C$.

5. **UnSigncrypt.** Given $\text{params}$, a ciphertext $C$, the sender’s identity $ID_S$ and the receiver’s private key $d_{ID_R}$ as input, this algorithm outputs the plaintext $m$ or the symbol “⊥”. “⊥” denotes that $C$ is an invalid ciphertext between $ID_S$ and $ID_R$.

**Correctness.** The algorithm UnSigncrypt will output a plaintext if the ciphertext and the offline signature are generated as defined above.

$m \leftarrow \text{UnSigncrypt}(\text{params}, \text{OnSigncrypt}(\text{params}, m, ID_R, HK_S, TK_S, \text{OffSign}(\text{params}, ID_R, d_{ID_S}, HK_S)), ID_S, ID_R, d_{ID_R})$

3.2. **Security Models of Generic Identity-based Online/Offline Signcryption**

An, Dodis, and Rabin [1] generalized IND-CCA2 notion slightly, by introducing an equivalence relation $\mathcal{R}$ with property: $\mathcal{R}(c_1, c_2) = \text{true} \Rightarrow \text{Dec}(c_1) = \text{Dec}(c_2)$ ($c_1$ and $c_2$ are ciphertexts). $\mathcal{R}$ is called decryption-respecting. We may use it to restrict the attacker from decrypting other encryptions of the target message. We say that the encryption scheme $\mathcal{E}$ is ciphertext indistinguishable against generalized CCA2 (or gCCA2) if there exists some efficient decryption-respecting relation $\mathcal{R}$ with respect to which it is CCA2-secure.

Our scheme is based on the $\text{CtE&B}$ which is called “commit-then-encrypt-and-sign” paradigm [1]. Before presenting our scheme, we revisit some theorems and issues addressed in [1] as follows:

**Theorem 1.** [1] Assume that $\mathcal{E}$ is IND-gCCA2-secure, $S$ is UF-CMA-secure and $C$ satisfies the syntactic properties of a commitment scheme. Then, in the insider-security model, we have:

- $\text{CtE&B} \iff C$ satisfies the hiding property.
- $\text{CtE&B} \iff C$ satisfies the relaxed binding property.

Thus, $\text{CtE&B}$ preserves security of $\mathcal{E}$ and $S$ if $C$ is a secure relaxed commitment. In particular, any secure regular commitment $C$ yields secure signcryption $\text{CtE&B}$.

The chameleon hash function can be regarded as a commitment. It should be noted that since chameleon hash functions $C$ are information-theoretically hiding, it is safe for the receiver when the sender chooses a bad commitment key (the hiding property is satisfied for all $HK$’s, and it is in sender’s interest to choose $HK$ so that the binding is satisfied as well). It is easy to determine that our proposed chameleon hash function satisfies both properties.

We can find from the next Section that our scheme is similar to $\text{CtE&B}$ except that we move the expensive signature part to offline phase. We also modified the encryption part to be more suitable in identity-based system. Hence, if our encryption part is IND-gCCA2-secure and we choose some UF-CMA secure identity-based signature
scheme combined with the chameleon hash function, we can construct an IND-gCCA2 secure and UF-CMA secure identity-based online/offline signcryption scheme. A proof for the encryption part can be found in Section 5.

4. Our Generic Identity-Based Online/Offline Signcryption Scheme

System Parameters Generation: Let \( t \) be a prime power, and \( E(\mathbb{F}_t) \) an elliptic curve over finite field \( \mathbb{F}_t \). Let \( \# E(\mathbb{F}_t) \) be the number of points of \( E(\mathbb{F}_t) \), and \( P \) be a point of \( E(\mathbb{F}_t) \) with prime order \( q \) where \( q \neq \# E(\mathbb{F}_t) \). \( \mathbb{G}_1 \) is the subgroup generated by \( P \). \( \mathbb{G}_2 \) is a finite group of order \( q \). Choose cryptographic hash function \( H_1: \mathbb{G}_2 \rightarrow \{0,1\}^n \). Let \( (\mathcal{L}, \mathcal{H}) \) be the chameleon hash family, which will be sent to the designated user on request, based on the discrete logarithm assumption and \((\mathcal{G}, S, \mathcal{V})\) be any identity-based signature scheme. The system parameters are \( SP = \{ E(\mathbb{F}_t), t, q, P, \mathbb{G}_1, \mathbb{G}_2, (\mathcal{G}, S, \mathcal{V}), H_1 \} \).

Key Generation:

- Given an identity \( ID \), run the key extract algorithm of the original identity-based signature scheme to obtain the private/public key pair \((d_{ID}, Q_{ID})\).

- On input \(1^k\), the sender runs the key generation algorithm of the trapdoor hash family \((\mathcal{L}, \mathcal{H})\) to obtain the hash/trapdoor key pair \((Y = xP, x)\).

Assume Alice sends \( m \) to Bob. Alice obtains private key and hash/trapdoor key \( \{d_{ID_A}, Y, x\} \). Bob obtains private key \( d_{ID_B} \). \( \{Q_{ID_A}, Q_{ID_B}\} \) are public to both of them.

OffSigncrypt:

- Choose at random \((m', r') \in R \mathcal{M} \times \mathcal{R} \), where \( \mathcal{M} \) is a message space and \( \mathcal{R} \) is a finite space, and compute the chameleon hash value \( h = H_Y(m', r') = m'P + r'Y \).

- Run the signing algorithm \( S \) with the signing key \( d_{ID_A}^{-1} \) to sign the hash value \( h \). Let the output be \( \sigma = S_{d_{ID_A}}(h||H_Y) \), where \( H_Y \) is the description of the chameleon hash.

- Choose at random \( y \in R Z_q^* \) and compute \( X = yP \), then compute \( \omega = e(y^{P_{pub}}, Q_{ID_B}) \). Finally set \( y' = H_1(\omega) \).

- Store the pair \((m', r')\) and \( y'\) for future use.

OnSigncrypt:

- For a given message \( m \), retrieve from the memory \( x^{-1} \) and the pair \((m', r')\).

- Compute \( r = x^{-1}(m' - m) + r' \mod q \).

- The message encryption is done with \( y' \) and a symmetric-key encryption algorithm such as AES. The ciphertext is \( c = Enc_{y'}(\sigma||ID_A||m||r||H_Y) \).

- Final ciphertext is \((c, X)\).

UnSigncrypt:

- Given ciphertext \((c, X)\), compute \( \omega = e(X, d_{ID_B}) \) and \( y' = H_1(\omega) \).

- Decrypt \( c \) as \( \sigma||ID_A||m||r||H_Y = Dec_{y'}(c) \).

- Compute \( h = H_Y(m, r) = mP + rY \).

- Verify that \( \sigma \) is indeed a signature of the value \( h||H_Y \) with respect to the verification key \( Q_{ID_A} \).

Correctness: The consistancy is easy to verify as follows:
\[ e(y^{P_{pub}}, Q_{ID_B}) = e(yP, d_{ID_B}) = e(X, d_{ID_B}). \]

Performance: The proposed scheme satisfies the requirement of online/offline signcryption as all expensive computations are done in the offline phase. The offline phase of our signcryption mainly consists of one evaluation of the trapdoor hash function, one invocation of the original signing algorithm and one pairing computation. The online phase consists of only a single collision finding computation and a symmetric-key encryption. The UnSigncrypt algorithm consists of one evaluation of the trapdoor hash function, one invocation of the original verification algorithm, one pairing computation and a symmetric-key decryption.

5. Security Proof

We can choose most of UF-CMA secure identity-based signatures as long as the key extraction algorithm is the same as in the encryption scheme below. We prove the encryption scheme is IND-gCCA2 secure to complete our proof.

Setup: Given security parameters \( k, n \) and \( \mathbb{G}_1, \mathbb{G}_2 \) of order \( q \) and generator \( P \) of \( \mathbb{G}_1 \), pick a random \( s \in Z_q^* \), and set \( P_{pub} = sP \). Chose cryptographic hash functions \( H_0: \{0,1\}^* \rightarrow \mathbb{G}_1, H_1: \mathbb{G}_2 \rightarrow \{0,1\}^n \). \( \mathcal{R} \) is decryption-respecting mentioned before. The system parameters are \((P, P_{pub}, H_0, H_1)\). The master key is \( s \). \( H_0 \) and \( H_1 \) will be regarded as random oracles in security analysis.

Extract: Given an identity \( ID \), compute \( d_{ID} = sH_0(ID) \) and output it as the private key related to \( ID \) corresponding to \( Q_{ID} = H_0(ID) \).

Encrypt: Given a message \( m \), choose at random \( y \in R Z_q^* \) and compute \( X = yP \), then compute \( \omega = (y^{P_{pub}}, Q_{ID_B}) \).
finally set \( y' = H_1(\omega) \). The message encryption is done with \( y' \) and a symmetric-key encryption algorithm such as AES. The ciphertext is \((e, X)\), where \( c = Enc_{y'}(m) \).

**Decrypt:** Given a ciphertext \((e, X)\), Compute \( \omega = e(X, a_{1D_B}) \) and Set \( y' = H_1(\omega) \), then decrypt the message \( Dec_{y'}(c) = m \).

**Theorem 2.** In the random oracle model, assume we have an IND-\( \sigma \)-CCA2 adversary called \( A \) that is able to distinguish ciphertexts that succeeds with probability \( \epsilon \) and asking \( H_0, H_1 \) and decryption oracle \( q_{0}, q_{1} \) and \( q_{4} \) times respectively. Then, there exists a simulator \( B \) that can solve the GBDH problem with the probability at least \( \epsilon \cdot \frac{1}{q_{0}} \cdot \frac{1}{q_{1}} \cdot \left( 1 - \frac{1}{q_{4}} \right) \).

**Proof.** Let \((P, aP, bP, cP)\) be the instance of the GBDH problem to be solved, the aim is to compute \( e(P, P)^{abc} \) where \( a, b, c \) are chosen at random from \( Z_q^\ast \) and \( P \) generates \( G_1 \), \( B \) will run \( A \) as a subroutine and act as \( A \)'s challenger in the IND-\( \sigma \)-CCA2 game. \( B \) needs to maintain lists \( L_0 \) and \( L_1 \) that are initially empty and are used to keep track of answers to queries asked by \( A \) to oracles \( H_0, H_1 \). \( B \) gives \( A \) the system parameters with \( P_{pub} = bP \).

We describe how the requests are treated below.

**H0 requests:** At the beginning of the simulation, choose \( i_{\beta} \) uniformly at random from \( \{1, \ldots, q_{0}\} \). If \( i = i_{\beta} \) then respond with \( H_0(ID_U) = aP \) and set \( ID_\beta = ID_U \), else choose \( x \) uniformly at random from \( Z_q^\ast \); compute \( Q_U = xP \); compute \( d_U = xP_{pub} \); store \((ID_U, Q_U, d_U, x)\) in \( L_0 \) and respond with \( Q_U \).

**H1 requests:** For a query \( H_1(\omega) \), \( B \) first ensures the list \( L_1 \) does not contain a tuple \((\omega, y')\). If such a tuple is found, \( B \) answers \( y' \), otherwise he chooses \( y' \in Z_q^\ast \), gives it as an answer to the query and puts the tuple \((\omega, y')\) into \( L_1 \).

**Key extraction requests:** We assume that \( A \) makes the query \( H_0(ID_U) \) before it makes the extraction query for \( ID_U \). When \( A \) asks a query \( Extract(ID_U) \), if \( ID_U = ID_\beta \), then abort the simulation, otherwise \( B \) searches \( L_0 \) for the entry \((ID_U, Q_U, d_U, x)\) corresponding to \( ID_U \) and returns \( d_U \).

**Decryption requests:** When receiving an decryption query for a ciphertext \((e, X)\) for identities \( ID_U \) that are not \( ID_\beta \), find the entry \((ID_U, Q_U, d_U, x)\) in \( L_0 \) and compute \( \omega = e(X, d_U) \), then run the \( H_1 \) simulation algorithm to find \( y' = H_1(\omega) \), finally decrypt the ciphertext \( Dec_{y'}(c) = m \).

When receiving an decryption query for a ciphertext \((e, X)\) for identities \( ID_U = ID_\beta \), \( B \) steps through the list \( L_1 \) with entries \((\omega, y')\). For each pair in \( L_1 \), \( B \) submits the tuple \((P, H_0(ID_\beta), P_{pub}, X, \omega)\) to DBDH oracle. The DBDH oracle returns 1 if \( \omega = e(X, d_{ID_\beta}) \) and 0 otherwise. If the returned value is 1, \( B \) will use the corresponding \( y' \) to decrypt the ciphertext \( Dec_{y'}(c) = m \). Otherwise \( B \) takes a random pair \((\omega, y')\) such that no \((\omega, \omega')\) already exists in \( L_1 \), then decrypt the message \( Dec_{y'}(c) = m \) and put the tuple \((\omega, y')\) into \( L_1 \).

After a polynomially bounded number of queries, \( A \) chooses an identity \( ID_B \) on which he wishes to be challenged and produces his two plaintexts \( m_0 \) and \( m_1 \). The restriction is that \( A \) cannot have chosen \( ID_B \) as one of key extraction requests. If \( ID_B \neq ID_\beta \), \( B \) aborts the simulation. Otherwise \( B \) chooses \( e^* \in R \{0,1\}^\ast \) and sets \( X^* = cP \). It returns the challenge ciphertext \((e^*, X^*)\) to \( A \). \( A \) then performs a second series of queries which is treated in the same way as the first one. This time, he can not make a key extraction request on \( ID_B \) and he can not make an decrypt query of \((e', X')\) equivalent to \((e^*, X^*)\), i.e. \( R((e', X'), (e^*, X^*)) = true \).

At the end of the simulation, \( A \) produces a bit \( b \). The simulator ignores this bit. It chooses some \( \omega \) at random from \( L_1 \) and returns \( \omega \) as its guess at the solution to the GBDH problem for \((P, aP, bP, cP)\).

Let us now consider how our simulation could fail, i.e. describe events that could cause \( A \)'s view to differ when run by \( B \) from its view in a real attack. It is clear that the simulations for \( H_0, H_1 \) and Decryption oracle are indistinguishable from real random oracles. \( B \) will abort the key extraction oracle, if \( d_{ID_\beta} \) was asked. The probability for the oracle to abort is at most \( 1/q_0 \). With a probability exactly \( 1/q_0 \), \( A \) chooses to be challenged on \( ID_\beta \). If \( A \) queries the \( H_1 \) oracle for \( \omega = e(P, P)^{abc} \), the simulation would fail. However, if \( A \) has any advantage it must make this query, and once it has done so we have trapped it into leaving enough information in \( L_1 \) to solve the GBDH problem with probability \( 1/q_1 \).

We conclude from the above that \( B \) succeeds with probability as follows:

\[
Adv[B] > \epsilon \cdot \frac{1}{q_0} \cdot \frac{1}{q_1} \cdot \left( 1 - \frac{1}{q_4} \right).
\]

\[\square\]

**6. Application to Broadcast Signcryption**

We now present a generic identity-based online/offline broadcast signcryption scheme based on the work in [2].

**System Parameters Generation, Key Generation:** As in our proposed scheme.

Assume user 1 broadcasts message \( m \) to a group of \( N \) users.

**Initialization:** Let \( Q_{1D_1} \) be the public key of the user 1, and \( K_{1N} \in R Z_q^\ast \) be the broadcast secret of user 1 for a group of \( N \) users. User 1 will compute the broadcast parameter \( P_{1-brdcst} \) as: \( P_{1-brdcst} = K_{1N}Q_{1D_1} \). User 1 will
deliver the parameter $P_{1-brcdst}$ to other users in the group by encrypting in each group-member’s pairwise shared key $(k = e(d_{ID_i}, Q_{ID_i}) \; i \in N)$ with user 1.

**OffSigncryption:**

- Choose at random $(m', r') \in_R M \times R$, where $M$ is a message space and $R$ is a finite space, and compute the chameleon hash value $h = H_Y(m', r') = m'P + r'Y$.
- Run the signing algorithm $S$ with the signing key $d_{ID_1}$ to sign the hash value $h$. Let the output be $\sigma = S_{d_{ID_1}}(h||H_Y)$, where $H_Y$ is the description of the chameleon hash.
- Choose at random $y \in_R Z_q^*$ and compute $\omega = e(Q_{ID_1}, P)^y$, then compute $X = yK_{1N}^{-1}P$. Finally Set $y' = H_1(\omega)$.
- Store the pair $(m', r')$ and $y'$ for future use.

**OnSigncryption:**

- For a given message $m$, retrieve from the memory $x^{-1}$ and the pair $(m', r')$.
- Compute $r = x^{-1}(m' - m) + r' \mod q$.
- The message encryption is done with $y'$ and a symmetric-key encryption algorithm such as AES. The ciphertext is $c = E_{\sigma||m||r}(H_Y)$. Finally Set $c' = H_1(\omega)$.
- Final ciphertext is $(c', X)$.

**UnSigncryption:**

Given a ciphertext $(c, X)$, the authorized receivers (i.e., members of the group provided with broadcast parameter $P_{1-brcdst} = K_{1N}Q_{ID_1}$) will compute the key $y'$.

- Given ciphertext $(c, X)$, compute $\omega = e(P_{1-brcdst}, X)$ and $y' = H_1(\omega)$.
- Decrypt $c$ as $\sigma||m||r||H_Y = Dec_{y'}(c)$.
- Compute $h = H_Y(m, r) = mP + rY$.
- Verify that $\sigma$ is indeed a signature of the hash value $h||H_Y$ with respect to the verification key $Q_{ID_1}$.

7. Conclusion

In this paper, we have proposed a generic identity-based online/offline signcryption scheme. In our scheme, the online computation is very efficient and all the expensive computation is performed offline. Our scheme is generic and does not require specific identity-based signatures and symmetric-key encryption schemes. Our scheme is secure against adaptive chosen-ciphertext attacks (IND-gCCA2) and is existentially unforgeable against adaptive chosen-message attacks (UF-CMA) provided that the signature part is UF-CMA secure. We also present a broadcast signcryption scheme as an application of the scheme.

**References**