Performance evaluation of railway subballast stabilised with geocell based on pull-out testing

Mohammad Mahdi Biabani  
*University of Wollongong*, mmb958@uowmail.edu.au

Ngoc Trung Ngo  
*University of Wollongong*, trung@uow.edu.au

Buddhima Indraratna  
*University of Wollongong*, indra@uow.edu.au

Follow this and additional works at: [https://ro.uow.edu.au/eispapers](https://ro.uow.edu.au/eispapers)

*Research Online* is the open access institutional repository for the University of Wollongong. For further information contact the UOW Library: research-pubs@uow.edu.au
Performance evaluation of railway subballast stabilised with geocell based on pull-out testing

Abstract
A large-scale apparatus was designed and built at the University of Wollongong to evaluate the pull-out strength of rail subballast reinforced with geocells. A series of tests were carried out to investigate the pull-out resistance, mobilised tensile strength ($t_{tensile}$) and passive strength ($t_{passive}$) of a subballast-geocell assembly under a given range of overburden pressure ($1 \text{ kPa} < q < 45 \text{ kPa}$). The interface was held in a vertical alignment to better simulate the interaction between subballast and geocell in accordance with routine track practices. The test results show that the geocell reinforcement provides a considerable degree of passive resistance, where the opening area (OA) and lateral pressure ($s_n$) over the geocell strip are found to be influential factors. A three-dimensional finite element simulation was also conducted. The numerical results show that the tensile strength mobilised in the geocell will increase as the geocell stiffness increases, but causes a reduction in $t_{passive}$. A parametric study was also developed to investigate the impact of geocell stiffness and friction coefficient on the passive resistance and mobilised tensile strength. These results indicate that the passive resistance and mobilised tensile strength increase with the increase in overburden pressure ($q$) and friction coefficient ($\mu$).

Keywords
geocell, out, performance, pull, evaluation, testing, railway, stabilised, subballast

Publication Details

This journal article is available at Research Online: https://ro.uow.edu.au/eispapers/5767
Performance evaluation of railway subballast stabilised with geocell based on pull-out testing

**M. Mahdi Biabani**, PhD, MEng, BEng

Research Assistant, Centre for Geomechanics and Railway Engineering, University of Wollongong, Wollongong City, NSW 2522, Australia; ARC Centre for Excellence for Geotechnical Science and Engineering, Australia Faculty of Engineering, Australia

**Ngoc Trung Ngo**, PhD, MEng, BEng

Lecturer, School of Civil, Mining and Environmental Engineering, University of Wollongong, Wollongong City, NSW 2522, Australia; ARC Centre for Excellence for Geotechnical Science and Engineering, Australia Faculty of Engineering, Australia

**Buddhima Indraratna**, PhD (Alberta), FTSE, FIEAust., FASCE, FGS.

Research Director, Distinguished Professor of Civil Engineering, Centre for Geomechanics and Railway Engineering, University of Wollongong, Wollongong, NSW 2522, Australia. ARC Centre for Excellence for Geotechnical Science and Engineering, Australia

Technical paper submitted to: *Geotextiles and Geomembranes*

Author for correspondence:

Distinguished Professor Buddhima Indraratna

Faculty of Engineering and Information Sciences

University of Wollongong

Wollongong, NSW 2522

Australia.

Ph: +61 2 4221 3046

Fax: +61 2 4221 3238

Email: indra@uow.edu.au
Performance evaluation of railway subballast stabilised with geocell based on pull-out testing

M. Mahdi Biabani¹, Ngoc Trung Ngo² and Buddhima Indraratna³

¹Research Assistant, Centre for Geomechanics and Railway Engineering, Faculty of Engineering, University of Wollongong, Wollongong City, NSW 2522, Australia; ARC Centre for Excellence for Geotechnical Science and Engineering, Australia Faculty of Engineering, Australia. Email: mmb958@uowmail.edu.au

²Lecturer, School of Civil, Mining and Environmental Engineering, University of Wollongong, Wollongong City, NSW 2522, Australia; ARC Centre for Excellence for Geotechnical Science and Engineering, Australia Faculty of Engineering, Australia. Email: trung@uow.edu.au, Ph: +61 2 4221 4892 Fax: +61 2 4221 3238

³Research Director, Distinguished Professor of Civil Engineering, Centre for Geomechanics and Railway Engineering, University of Wollongong, Wollongong, NSW 2522, Australia. ARC Centre for Excellence for Geotechnical Science and Engineering, Australia. Email: indra@uow.edu.au, Ph: +61 2 4221 3046 Fax: +61 2 4221 3238

ABSTRACT: A large-scale apparatus was designed and built at the University of Wollongong to evaluate the pull-out strength of rail subballast reinforced with geocells. A series of tests were carried out to investigate the pull-out resistance, mobilised tensile strength ($\tau_{\text{tensile}}$) and passive strength ($\tau_{\text{passive}}$) of a subballast-geocell assembly under a given range of overburden pressure (1 kPa $\leq q \leq$ 45 kPa). The interface was held in a vertical alignment to better simulate the interaction between subballast and geocell in accordance with routine track practices. The test results show that the geocell reinforcement provides a considerable degree of passive resistance, where the open area ($OA$) and lateral pressure ($\sigma_n$) over the geocell strip are found to be influential factors. A three-dimensional finite element simulation was also conducted. The numerical results show that the tensile strength mobilised in the geocell will increase as the geocell stiffness increases, but causes a reduction in $\tau_{\text{passive}}$. A parametric study was also developed to investigate the impact of geocell stiffness and friction...
coefficient on the passive resistance and mobilised tensile strength. These results indicate that the passive resistance and mobilised tensile strength increase with the increase in overburden pressure ($q$) and friction coefficient ($\delta$).

**KEYWORDS:** Geosynthetics, Geocell reinforcement, subballast, pull-out, numerical modelling

**1. Introduction**

In view of rapid urbanisation, the demand for appropriate ground improvement techniques is imperative, in order to construct road and rail infrastructure over subgrade deposits with low shear strength. This has intensified pressure on railway industry to find innovative solutions to maintain track stability and reduce maintenance cost. Unlike conventional rigid reinforcement (e.g. steel and timber), geosynthetics have shown a promising approach to improve the performance of granular media placed over weak and soft subgrade (Bergado et al. 1993; Indraratna et al. 2011; Bathurst and Raymond 1987; Brown et al. 2006; Tutumluer et al. 2012). Loss of track geometry that is associated with excessive differential settlements due to localized failure of formation (capping and subgrade), often results in reduced stability and longevity of tracks (Selig and Waters 1994, Indraratna et al. 2014). In this regard, planer geosynthetics (e.g. geogrids, geotextiles or geocomposites) have been effectively utilised to reduce excessive settlement and lateral displacement of tracks under cyclic loading (Indraratna et al. 2013). In addition, three-dimensional cellular reinforcement, also known as geocell mattress, has been considered for different applications. The improvement in the performance of geocell stabilised soil has been attributed to enhanced apparent cohesion between the infilled soil and the geocell (Bathurst and Rajagopal, 1993). Nevertheless, recent studies have proven that the additional confinement mobilised during cyclic loading, helps to
enhance confinement and minimize lateral spreading of the aggregates, hence maintain
stability of the infill granular material (Indraratna et al. 2015). Different types of
geosynthetics have been utilised to investigate the pull out resistance (Ezzein and Bathurst
2014, Moraci and Recalcati 2006, Sieira et al. 2009, and Bakeer et al. 1998). Also, the effects
of aperture size and shape and opening area have been investigated by employing large-scale
direct shear box and assessing the shear strength of unreinforced and reinforced soil (Biabani
and Indraratna 2015). Nevertheless, studies of pull-out testing on cellular reinforcement (i.e.
geocell pocket) of railway materials have not been conducted before to the knowledge of the
authors.

Indeed, none of the past studies were able to evaluate the exact mechanisms of shear
improvement due to: (i) disparity in the loading patterns, where the overburden stress is either
ignored or considered to be perpendicular to the sliding direction, and (ii) inappropriate
horizontal alignment of the failure plane, in conventional direct shear and pull-out tests. In
most cases, the planer geogrids are placed horizontally, so the normal stress is the vertical
stress. However, placing the geocells mattress horizontally means that their strips are in the
vertical direction, so the normal stress can be assumed as hydrostatic stress. This pattern of
normal stress distribution must be properly assessed, because this is crucial for internal
stability in the lower layers of a railway substructure, where the lateral confinement on ballast
or subballast is usually very low \( (\sigma'_v \leq 30 \text{ kPa}) \) as measured in the field. In view of this, a full-
scale laboratory pull-out apparatus was adopted to investigate the shear strength of geocell-
reinforced subballast in a more realistic manner.

2. Scope and objective of current study
In order to investigate the advantages of cellular reinforcement of geocell-reinforced subballast in the field (Fig.1), a series of pull-out tests were conducted using a new apparatus, where the overburden stress was applied parallel to the pull-out direction (shearing plane). In this condition, the load distribution over the geocell strip can be investigated and compared to a conventional direct shear or a pull-out box. The objective of this current study is to develop a new approach to measure the passive resistance ($\tau_{\text{passive}}$) of geocell reinforced granular media with respect to a typical railway condition subjected to a relatively low confining pressure exerted by sleepers and the ballast shoulder ($\sigma'_c \leq 30$ kPa) as measured in the field by Indraratna et al. (2015). In this investigation, during pull-out testing, the potential failure plane was not forced to be parallel to the pulling direction, and the mobilised shear resistance over geocell strips was measured by applying different overburden stresses on top of the geocell. A numerical analysis was also conducted to validate the experimental results and to provide greater insight into the pull-out test results, particularly considering the passive resistance ($\tau_{\text{passive}}$) attributed to the transverse ribs and mobilised tensile strength ($\tau_{\text{tensile}}$) of the longitudinal ribs. Also, a parametric study was carried out to investigate the impact of different factors, including the geocell stiffness ($E_{\text{geocell}}$), the overburden pressure ($q$), and the friction coefficient ($\delta$).

3. Material and Method of Testing

The granular medium used here was a locally available crushed basalt from a quarry near Wollongong. The particle size distribution adopted for the subballast was within the rail industry specified range ($D_{50} = 3.3$ mm, $D_{\text{max}} = 19$ mm, $D_{\text{min}} = 0.075$ mm, $C_u = 16.3$, $C_c = 1.3$, $\gamma_d = 19$ kN/m$^3$). Four types of geogrid and two types of geomembrane were used to form a geocell pocket for reinforcing the subballast and to examine the influence of the open area ($OA\%$) on the passive resistance. The geogrids and geomembranes were divided to three
types of geosynthetics (Fig. 2 a): (i) geomembrane (GC1 and GC2), (ii) triaxial geogrid with
triangular openings (GG1), and (iii) biaxial geogrid (GG2, GG3 and GG4). The
geomembranes used were made from strips of high density polyethylene, welded together at
the joints to create a cellular network with depth of 150 mm. The geogrids were made from
high density polypropylene, and they were also connected together to create a 150 mm deep
cellular pocket. It is noted that the welding of geocells was carried out by the manufacturer.
During laboratory tests, the geocell was installed exactly in the same way as in the field.
Within the scope of this study, the effect of the welded joint was not considered, although we
agree that this is a relevant point. The physical and mechanical properties of the
geosynthetics used in this study are summarised in Table 1.

The large-scale pull-out box (800 mm long, 600 mm wide, and 500 mm high) designed and
built at University of Wollongong is shown in Fig. 2b. It was large enough to accommodate a
single geocell pocket at the centre without any significant boundary effects. A total of 36 tests
under different overburden pressures were conducted. A predetermined mass of granular
material was placed inside the box in several layers and then compacted using a vibratory
hammer to achieve the desired relative density ($D_r$) of about 77%, that is representative of
subballast in the field ($\rho = 2100$ kg/m$^3$). Vertical displacement was recorded using a linear
variable differential transformer (LVDT). Four strain gauges were attached to the geocell
pocket at heights of $h = 18.75, 56.25, 93.75,$ and $131.25$ mm as illustrated in Figs. 2b-c to
measure vertical strains of longitudinal ribs in various geocell pockets. To attach the strain
gauges to the geocell strip, the surface of a geocell pocket/rib was brushed lightly with
cleaner and degreaser, and an industrial adhesive was applied before mounting the strain
gauges. The strain gauge was pressed into the adhesive with an overlying thin plastic film
with care to remove all the entrapped air. The strain gauges were then covered with flexible
sealant and water proof tape. The cable leads were encased in flexible conduits to protect them from any damage during the experiments owing to subsequent deformation of the geocell pocket. Four miniature pressure cells (10 mm thick, 50 mm diameter with a range of 500 kPa and 99.7% accuracy) were also mounted to the geocell at depths of \( h = 18.75, 56.25, 93.75 \) and 131.25 mm to measure the stress induced in the geocell strip (Figs. 2b-c). Every instrument was calibrated before connecting to an electronic data logger (DT800) and was controlled by a host computer to accurately record pull-out force, vertical displacement and stresses at predetermined time intervals during the testing. A pull-out force was applied using the tensile Instron machine at different overburden pressures varying from 1 kPa ≤ \( q \) ≤ 45 kPa. A groove was provided at the top loading plate to facilitate pull-out of the geocell while maintaining a constant overburden pressure. A single pocket of geocell was placed at the centre of the box and the subballast layer was placed and compacted in three layers surrounding the geocell to achieve the desired field density. The pull-out rate was maintained at 1 mm/min during testing, following the ASTM-D-6706-01, (2001). During these experiments, shearing continued until a maximum vertical displacement of 30 mm was reached (i.e. the maximum displacement allowed by the apparatus).

4. Results and Discussion

4.1 Pull-out force

Fig. 3a shows the results obtained by pull-out tests for reinforced subballast with a single geocell pocket (GC1) subjected to various overburden pressures, ranging from 1 kPa to 45 kPa. The pull-out force shows a non-linear variation with the axial displacement where as expected, an increased pull-out force is evident at a higher overburden pressure. For a given overburden pressure, the pull-out force reaches the peak value at an axial displacement of 4-8 mm, beyond which the pull-out force then decreases with further increase in axial
displacement. The observed stress-strain responses including volumetric strains confirm that the reduction in the pull-out force is associated with the post-peak dilation of the aggregates. The variation in volumetric change at different axial displacements is shown in Fig. 3c and it is observed that at low overburden pressure ($q$), geocell-reinforced specimen exhibits an initial contraction followed by dilation. Nevertheless, a volumetric contraction occurs at a higher level of overburden pressure ($q \geq 20$ kPa), which clearly demonstrates the role of effective cellular confinement in inhibiting dilation. The degree of contraction is increased by increasing the overburden pressure. It can be concluded that the infill granular materials tend to be in compression rather than being in dilation when reinforced by a cellular pocket.

Fig. 3b presents the corresponding pull-out force of the subballast, reinforced with different types of geosynthetics subjected to an overburden pressure of $q = 20.5$ kPa. According to the laboratory results, GG3 (having the highest open area) provides the lowest degree of pull-out force compared to other geosynthetics. This can be justified due to the large size of the aperture in geogrid GG3, compared to the subballast gradation. As a result, geogrid GG3 does not provide a considerably effective interlock with the subballast aggregates. On the other hand, the laboratory results reveal that the triax geogrid (GG1) exhibits the highest pull-out force, the highest initial modulus, and the lowest degree of dilation compared to other geosynthetics. This is possibly because of the triangular shape apertures and the optimum aperture size of the GG1 with respect to subballast gradation providing better particle interlocking and a more uniform stress distribution facilitated by the triaxial ribs (Biabani and Indraratna 2015).

4.2. Measured geosynthetics strains
It is well recognised that in pull-out testing, the strain mobilised in the geosynthetic varies according to the distance from the pull-out force (Abdi and Zandieh 2014, Moraci and Recalcati 2006, Sugimoto and Alagiyawanna 2003). During pull-out testing, the force is transferred from transverse members and friction surfaces through the longitudinal members. There will be a different mobilisation of strain, at different parts of the geocell pocket, due to different elongation of longitudinal ribs (Bergado and Chai 1994). As a result, a particular part of reinforcement will be moved during pull-out testing. Fig. 4a shows the variations of strains, mobilised in the longitudinal ribs of geogrid GG2 subjected to various overburden pressures. The experimental results show that the mobilised strain of the geocell pocket varies with the depth and that mobilised strain increases as the overburden pressures ($q$) increases. The maximum strain mobilised in the reinforcement is found to occur at a depth of about $h = 18.75$ mm. Moreover, the results also show that there is an insignificant strain mobilised at the depth of $h = 131.25$ mm, highlighting the varied mobilised strains with the geocell depth. These results are in accordance with previous studies, which were carried out using conventional pull-out testing (Bergado and Chai 1994; Alagiyawanna et al. 2001), among others. Fig. 4b shows the mobilised strain for different types of the geosynthetics subjected to an overburden pressure of $q = 29.5$ kPa. It is seen in all of these artificial inclusions that the mobilised strain decreases with an increase in the depth of the geocell pockets. However, over the longitudinal ribs, the GG2 provided the minimum strain, and GG3 provided the maximum strain. This can be explained by the fact that GG2 has the highest and GG3 has the lowest mobilised tensile strength during pull-out testing, and this is possibly associated with the level of interlocking between the subballast particles and the tested geosynthetics.

4.3. Passive resistance
It is well known that, the pull-out resistance can be determined as the sum of the frictional and bearing (passive) resistance in reinforced soil as:

\[ P_{\text{reinforced}} = P_{RF} + P_{RB} \]  

(1)

where, \( P_{RB} \) is the bearing (passive) resistance and \( P_{RF} \) is the frictional resistance. There are several models available in the literature for evaluating the bearing (passive) resistance, which are summarised in Table 2. Accordingly, the performance of geocell-reinforced subballast can be explained by determining the bearing resistance (passive strength) that develops against transverse ribs during pull-out testing. Bergado and Chai (1994) presented that the mobilised passive bearing resistance \( (\tau_{\text{passive}}) \) of geosynthetic-reinforced soil could be obtained as:

\[ \tau_p = N_q \sigma_n + CN_c \]  

(2)

where, \( Nc \) and \( N_q \) are bearing capacity parameters. The bearing capacity factor \( N_q \) is determined by (Peterson and Anderson, 1980):

\[ N_q = e^{(\pi \tan \phi)} \tan^2 \left( \frac{\pi}{4} + \frac{\phi}{2} \right) \]  

(3)

Also, the value of \( N_c \) can be determined by:

\[ N_c = (N_q - 1) \cot \phi \]  

(4)

In Eq. (2), \( \sigma_n \) is the normal stress at the soil-geocell interface, which has been measured by miniature pressure cells. The magnitude of normal stress over the geocell strip could be calculated by lateral earth pressure, as shown in Fig 5a. The passive resistance of geocell reinforced subballast determined by Eq. (2) is plotted for different overburden pressures (hence normal stresses) for various types of geosynthetics, as shown in Fig. 5b. In addition, the degree of \( \sigma_n \) over the geocell strip measured by the miniature pressure cell and calculated...
by earth lateral pressure is also shown in Fig. 5b. As expected, the passive resistance increases as the overburden pressure ($q$) increases. Notably, the value of $\sigma_n$ measured by the pressure cell is slightly greater than $\sigma_n$ calculated by the lateral earth pressure theory. Also, based on the lateral pressure measured by four miniature pressure cells, a marginal difference is observed over the relatively small height of the geocell pocket. Accordingly, it can be assumed that the shear strength was uniform through the geocell strips. The geogrids GG1 and GG3 provide the maximum and minimum $\tau_{\text{passive}}$, respectively, as shown in Fig. 5b. This can be justified due to the optimum length and thickness of the transverse ribs compared to the subballast degradation. Fig. 5b also shows that the maximum passive resistance can be obtained when the percentage of open area ($OA$) is in a range of $70\% < OA < 80\%$.

In order to compare the shear strength obtained by the new pull-out box and those measured in large-scale direct shear tests by Biabani and Indraratna (2015), the passive resistance is plotted against normal stress ($\sigma_n$) for the same subballast confined by the same geosynthetics, as shown in Fig. 5c. It is seen that the mobilised passive resistance ($\tau_{\text{passive}}$) measured by the pull-out and direct shear tests exhibits a similar trend except that the degree of mobilised passive resistance ($\tau_{\text{passive}}$) measured in the large-scale direct shear box is markedly less than that measured in the current pull-out tests. This can be related to the impact of loading mechanism on the overall behaviour of reinforced materials, where the contribution of geogrid transverse ribs has been mobilised to increase passive resistance for the case of interaction under pullout mode. It is seen from Figs. 5b-c that at the same normal stress (i.e. $\sigma_n \approx 21$ kPa), the passive resistance measured in the pull-out box (about $\tau_{\text{passive}} = 16$ kPa) is much higher than that measured in the large scale direct shear box (about $\tau_{\text{passive}} = 4$ kPa). These results clearly show that a much lower normal stress is needed to mobilise the same passive resistance as was exhibited during direct shear.
5. Finite Element Simulation

Numerical simulations have been often used to model various types of geosynthetically reinforced soils in pull-out testing using the finite element approach (Abdi and Zandieh 2014, Ezzein and Bathurst 2014, Khedkar and Mandal 2009). However, there are only a few models that have been used to investigate the bearing (passive) resistance of soil against the transverse ribs. Due to this difficulty, most of the studies only investigated the overall performance in pull-out resistance, and the passive resistance in reinforced soil has received less attention in most of the numerical simulations currently available. To fully understand the loading mechanism and the performance of reinforced subballast in a pull-out test, it is inevitable to develop a numerical model that can capture the passive resistance of geosynthetics. A three-dimensional finite element model, using the ABAQUS package, is developed in this study to investigate the actual behaviour of geocell reinforced subballast. In order to validate the experimental results, a single pocket form by geogrid GG2 was selected for the numerical simulation. Furthermore, to simulate the exact configuration of the laboratory size pull-out test, the geometry of the box and the geocell pocket (i.e., number and dimension of the apertures) were taken to be the same as the experimental configuration (Figs. 6).

5.1. Material properties

An elasto-plastic material with a non-associated flow rule was used in simulations to model the subballast. To capture the plastic behaviour of subballast, the Mohr-Coulomb yield criterion with a friction coefficient of 0.5 was adopted. To model the geocell pocket, a linear elastic-perfectly plastic material was used. The geometry of the geocell reinforcement is one of the main factors considered in this pullout study where a hexagonal shape was selected for
the geocell pocket, as it is similar to the actual geocell pocket conducted in the experiment and on the field. Also, it provides a more uniform stress distribution than a square or diamond shape when it is subjected to loading. The subballast-geocell interaction was established by developing two contact surface pairs, i.e. inside and outside of the pocket with a hard normal contact. A small value of cohesion (2 kPa) was used during this simulation to improve numerical stability and to ensure the model to converge in the reasonable computation time. A summary of the material properties used in the simulations is provided in Table 3. Exploiting the symmetry of the developed model, only half of the geocell assembly was simulated in the current analysis, as shown in Figs. 6c-d.

5.2. Boundary conditions, loading and mesh size justification

In the FEM simulations, the boundary conditions were applied to allow nodes in the boundary to move in a vertical direction, and these nodes were restricted from moving in the direction normal to the boundaries (i.e. lateral directions), and the base of the model was fixed as illustrated in Figs. 6a-c. In order to obtain the optimum size of mesh and element number, several models with different numbers of elements were analysed. A sensitivity analysis was performed under an overburden pressure of $q = 45$ kPa and $E_{\text{subballast}} = 7000$ kPa with a geocell pocket of 150 mm in height to evaluate the effect of mesh density. The subballast was modelled using quadratic tetrahedral elements of type C3D10, and the number of elements varying from 17,656 to 231,310. A uniform loading applied on top of the specimen before testing and then propagated throughout the assembly during the pull-out test. The mobilised tensile strengths ($\tau_{\text{tensile}}$) of the geocell pockets for models with different number of elements were compared at a depth of $h = 18.75$ mm, after the geocell pockets had been displaced by 30 mm, as shown in Fig. 7. It is seen that the value of $\tau_{\text{tensile}}$ decreases as the number of elements ($N$) increases, and when the number of elements exceeds about
100,000 elements, the reduction in the mobilised tensile strength is negligible. Based on this observation, a finite element model with $N=100,236$ elements was adopted in the current study.

5.3. Numerical Results

5.3.1. Geocell displacement

It is well known that in pull-out testing, displacement of the geosynthetic decreases with the increasing distance from the applied force. Fig. 8a shows a typical displacement of the geocell pocket during pull-out testing, and Fig.8b shows the normalised geocell displacement $(\Delta h \%)$ in the direction parallel to the pull-out force, for different overburden pressures $(q)$. Based on these results, $\Delta h$ decreases with an increase in the overburden pressure and this observation is similar to those measured in the laboratory by the strain gauges as shown in Fig. 4a. This can be justified that increasing $q$, hence the normal pressure over the geocell strip, leads to improving its resistance to the pull-out force. As expected, maximum displacement occurred at the point where the geocell pocket was attached to the pull-out force.

5.3.2. Tensile strength

One of most important parameters that governs the behaviour of reinforced soil is the mobilised tensile strength ($\tau_{\text{tensile}}$) in the reinforcement, which cannot be measured directly during laboratory testing. Fig. 9a shows a typical mobilised tensile strength in different parts of geocell during pull-out testing. As shown here, minor $\tau_{\text{tensile}}$ is observed in the transverse ribs, compared to the longitudinal ribs. In order to compare the $\tau_{\text{tensile}}$ at different depths ($h$), the values of $\tau_{\text{tensile}}$ are plotted for longitudinal ribs and junctions at different overburden pressure $(q)$ for various depths as presented in Fig. 9b. It is seen that both the longitudinal
ribs and junctions exhibit an identical trend where the magnitude of $\tau_{\text{tensile}}$ increases with an increase of the overburden pressure. The magnitude of $\tau_{\text{tensile}}$ in the junctions is observed to be almost half of that in the longitudinal ribs. In addition, the degree of $\tau_{\text{tensile}}$ decreases with an increase in the depth of the geocell pocket ($h$), where $\tau_{\text{tensile}}$ is found to be almost negligible in both longitudinal ribs and junctions beyond $h \geq 120$ mm.

5.3.3. Stress distribution over geocell pocket and passive resistance

To compare the lateral pressure over the geocell strip at different overburden pressures, the magnitude of $\sigma_n$ over the geocell strip is plotted for different overburden pressures ($q$), as shown in Fig. 10a. Compared to normal pressure measured by different methods, a relatively good agreement is observed, though $\sigma_n$ measured by the pressure cell is slightly greater than the numerical (FEM) and theoretical values. As expected, the values of normal pressure over the geocell strip increases when the overburden pressure ($q$) increases. In every case, the value of $\sigma_n$ is about less than half the overburden pressure. This highlights the difference in the loading mechanism between a conventional pull-out box, in which $\sigma_n$ on the geosynthetics is equal to the applied pressure, and the current pull-out box.

Another factor that was investigated in the numerical analysis is the passive resistance ($\tau_{\text{passive}}$) of subballast against the pull-out force. Accordingly, the value of $\tau_{\text{passive}}$ at different overburden pressures is plotted (Fig. 10b) and it shows that the magnitude of $\tau_{\text{passive}}$ is increased by increasing $q$. Using a best-fit regression analysis, the normal stress applied to the geocell strip is provided as a function of the overburden pressure (Fig. 10b). To provide more insight into passive resistance, the vertical pressure on different sections of the subballast is shown in Fig. 10(c). This shows that the mobilised passive resistance is found to be relatively uniform over the depth of the geocell pocket. This is probably because the specimen is not
deep enough for any change in stress in the subballast, and this leads to a uniform stress
distribution with depth. In addition, this figure also shows that the magnitude of stress applied
to the soil inside the geocell pocket decreases slightly, about 4-5 kPa. This is probably
because the geocell can effectively confine the infill material, thus reducing the pressure
transmitted to the lower soil layer. Details of the passive resistance of the soil particle trapped
within the aperture are presented in Fig. 10d. As shown here, the magnitude of $\tau_{\text{passive}}$ is
slightly greater at the middle of the section (about 2-3 kPa) compared to the sides, and this
could be attributed to less friction between subballast and longitudinal ribs than subballast
itself.

5.4. Parametric study

5.4.1. Geocell stiffness

The results of this study can be used to predict the behaviour of the geocell in pull-out testing,
when various types of geosynthetics with different properties are deployed. In this study, the
impact of geocell stiffness ($E_{\text{geocell}}$) is investigated by varying its modulus from a relatively
low to high range of 0.05 GPa to 5.0 GPa to simulate the behaviour of different geosynthetics
(e.g. GC1, GC2, GG1, GG3 and GG4). Moreover, the influence of the friction coefficient ($\delta$)
was studied from a range of 0.25 to 0.9 to simulate the relatively smooth to rough interface
between the infill and the geosynthetic interface. Fig. 11a shows the variations in the
mobilised tensile strength ($\tau_{\text{tensile}}$) in the longitudinal ribs for different $E_{\text{geocell}}$ at different
depths of the geocell pocket. As expected, by increasing the stiffness of the geocell, the
magnitude of $\tau_{\text{tensile}}$ is increased. The numerical simulation shows that by increasing $E_{\text{geocell}}$ up
to 1 MPa, there is a significant improvement in $\tau_{\text{tensile}}$, beyond which any improvement is
marginal (Fig. 11a). It can be concluded that deploying geosynthetics with a relatively high
modulus does not provide a significant difference in behaviour, compared to one with a lower
stiffness. Fig. 11a also shows that regardless of the geosynthetic stiffness, at a lower depth ($h = 131.25$ mm), almost the same tensile strength is mobilised. Fig. 11b shows the degree of mobilised tensile strength ($\tau_{\text{tensile}}$) at different values of friction coefficient ($\delta$) and as expected, increased $\delta$ leads to an increase in the magnitude of $\tau_{\text{tensile}}$. It also shows that at the lower depth of the geocell ($h \geq 90$ mm), in all of cases, the degree of $\tau_{\text{tensile}}$ is reduced markedly.

5.4.2. Passive resistance

The effect of geocell stiffness ($E_{\text{geocell}}$) and friction coefficient ($\delta$) can be best evaluated by comparing the passive resistance ($\tau_{\text{passive}}$) provided by the transverse ribs during pull-out testing. Fig. 12a presents the developed $\tau_{\text{passive}}$ against the transverse ribs for geocell with different values of stiffness ($E_{\text{geocell}}$). Based on these results, the maximum passive strength is observed at the lowest value of $E_{\text{geocell}}$. Increasing $E_{\text{geocell}}$ leads to a substantial reduction in the passive resistance against the transverse ribs. This can be explained by the fact that there will be a higher $\tau_{\text{tensile}}$ mobilised in geocell at a higher value of $E_{\text{geocell}}$. As result, this will help to increase the stability of the reinforced subballast and lead to a reduction in the passive resistance. This behaviour continues up to about $E_{\text{geocell}} = 1000$ MPa, beyond which no significant reduction is observed. This is because no further $\tau_{\text{tensile}}$ is mobilised at the geocell with a higher stiffness ($E_{\text{geocell}} < 1000$ MPa). Thereby, it can be concluded that geosynthetics with a lower stiffness can provide a higher magnitude of passive resistance during pull-out testing. Fig. 12b presents the degree of passive resistance ($\tau_{\text{passive}}$) at different friction coefficients ($\delta$) for different overburden pressures ($q$). The magnitude of $\tau_{\text{passive}}$ increases as a result of enhanced $\delta$ at different values of $q$. The degree of $\tau_{\text{passive}}$ determined by Eq. (2) is also presented in Fig. 12b where it is found that the magnitude of $\tau_{\text{passive}}$ calculated by Eq. (2) is in a good agreement with the numerical results when the friction coefficient is within the range of $0.4 \leq \delta \leq 0.45$. 
6. Practical implications

It is found from this study that geocell modulus, value of friction coefficient and loading mechanism have considerable influence on the performance of geocell-reinforced subballast. These influential factors need to be considered in track design in determining the mobilised tensile strength and passive resistance when geocells are utilised. For this purpose, large-scale pull-out tests were carried out to examine the pull-out resistance, mobilised tensile strength, and passive strength of the geocell-reinforced subballast under a realistic range of overburden pressure (1 kPa to 45 kPa). The measured data were used to calibrate and validate the three-dimensional finite element analysis.

The proposed 3D-FEM model can be used in practice for real-life scenarios to simulate pull-out tests on cellular reinforcement (i.e. geocell pocket) for subballast aggregates, modelling the actual stress conditions acting on the geocells, thereby capturing the role of influential factors as mentioned above. This model is also helpful for the practitioner to assess the mobilised tensile strength of a geocell-reinforced granular assembly, considering the passive resistance attributed to the transverse ribs and the mobilised tensile strength of the longitudinal ribs. The 3D FEM model is also able to capture the mobilised strains with the depth of geocells as accurately validated by extensive large-scale pull-out tests. In the absence of past pull-out tests on subballast reinforced by a geocell assembly, this study offers some original insight for the practitioner to improve design as well as to conduct a performance verification of the track.

7. Conclusion

The behaviour of geocell-reinforced subballast was investigated using a new pull-out apparatus under varying overburden stress (1 kPa ≤ q ≤ 45 kPa). A numerical analysis was conducted to simulate and measure the mobilised tensile strength and passive resistance at...
different overburden pressures, geocell modulus, and friction coefficients. A parametric study was also developed to investigate the impact of geocell stiffness and friction coefficient on the passive resistance and mobilised tensile strength. The results showed that the geocell reinforcement provided a considerable degree of passive resistance, where the open area and lateral pressure over geocell strip were found to be most influential factors. The results confirmed that the behaviour of geocell-reinforced granular medial was governed by the loading mechanism, whereby the magnitudes of friction coefficient and geocell modulus had a significant impact on the performance of the reinforced specimen.

This study also proved that geocells yield to higher passive resistance when they are used in pull-out testing, compared to the results obtained using the large-scale direct shear apparatus. This can be related to the impact of loading mechanism on the overall behaviour of reinforced materials where the contribution of geogrid transverse ribs has been mobilised to provide significant passive resistance during pull-out. The results also showed that the cellular reinforcement provided a higher bearing resistance in pull-out testing, in comparison with planar geomembranes tested in direct shear. It was also found that the passive bearing resistance had a significant influence on the overall interface shear strength where the lower geosynthetics stiffness resulted in a higher magnitude of passive resistance. Geocells provided a higher passive resistance when subjected to a relatively lower normal stress while the geocell with a higher stiffness exhibited a greater passive resistance against the transverse ribs.

Acknowledgments

The authors to acknowledge the financial support received from the Research Centre for Geomechanics and Railway Engineering (GRE) and the Australian Research Council (ARC).
The authors are grateful for Alan Grant, Laboratory Manager and Ritchie McLean, Technical Officer at GRE for their assistance during laboratory testing.

List of Notations

- $A$ = aperture size (mm)
- $D_{50}$ = average particle size (mm)
- $\rho$ = density (kg/m$^3$)
- $C_u$ = uniformity coefficient (dimensionless)
- $Cc$ = coefficient of curvature (dimensionless)
- $D_R$ = relative density (%)
- $D_{max}$ = maximum particle size (mm)
- $D_{min}$ = minimum particle size (mm)
- $\gamma_d$ = dry unit weight of the soil (kN/m$^3$)
- $d$ = diameter of geocell pocket (mm)
- $\sigma_n$ = normal stress (kPa)
- $OA$ = percentage of opening area (%)
- $P$ = pull-out force (kN)
- $h$ = geocell height (mm)
- $q$ = overburden pressure (kPa)
- $E_{geocell}$ = geocell stiffness (MPa)
- $\Delta h$ = normalised geocell displacement (%)
- $\nu$ = poisson’s ratio
- $\psi$ = dilation angle (degree)
- $\phi$ = friction angle (degree)
- $c$ = cohesion (kPa)
- $\tau_{passive}$ = passive resistance (kPa)
- $\tau_{tensile}$ = mobilised tensile strength (MPa)
- $\delta$ = friction coefficient
- $l_{pull-out}$ = pull-out displacement (%)
- $k_o$ = coefficient of earth pressure (kPa)
- $N$ = number of elements
References:


Table 1. Physical characteristics and technical specification of geocell used for the study.

Table 2. Summary of proposed models for capturing bearing resistance.

Table 3. Finite element properties of subballast and geocell used in current study.
List of Figures

Figure 1. Loading mechanism of geocell-reinforced subballast in a typical railway environment.

Fig. 2. (a) Schematic illustration of (a) different geocell pockets used in this study and (b) schematic diagram of large-scale pull-out box apparatus (800×600×500 mm) and (c) subballast reinforced with GG2.

Figure 3. Comparison between pull-out force and vertical strain ($\varepsilon_v$) of reinforced subballast.

Figure 4. Variation of mobilised strain in longitudinal ribs at (a) reinforced subballast with GG2 and (b) different types of geosynthetics.

Figure 5. (a) Typical stress characteristic for pull-out bearing failure (Modified after Bergado and Chai, 1994); comparison of passive resistance ($\tau_{\text{passive}}$) at different opening area (OA) of different geosynthetics in: (b) current pull-out box, and (c) large-scale direct shear box.

Figure 6. Finite element discretization of full mesh (a and b) and half mesh (c and d) exploiting symmetry

Figure 7. Mobilised tensile strength predicted by FEM model with different number of elements (N).

Figure 8. (a) Typical geocell displacement during pullout force, and (b) variation of axial displacement of longitudinal ribs at different depth of geocell pocket.

Figure 9. Typical mobilised tensile strength in (a) geocell formed by geogrid GG2 and (b) at different depths of geocell pocket.

Figure 10. Normal stress developed over geocell strips induced by the overburden pressure, (b) passive resistance at different overburden pressures, (c) typical normal stress in the geocell-reinforced subballast and (d) passive resistance in the soil trapped in the geocell aperture.
Figure 11. Variation of mobilised tensile strength at different (a) geocell stiffnesses ($E_{geocell}$) and (b) friction coefficient ($\delta$).

Figure 12. Variation of passive resistance at different (a) geocell stiffnesses ($E_{geocell}$) and (b) friction coefficient ($\delta$).
Table 1. Physical characteristics and technical specification of geocell used for the study

<table>
<thead>
<tr>
<th>Geosynthetic type</th>
<th>Geomembrane</th>
<th>Geogrid</th>
</tr>
</thead>
<tbody>
<tr>
<td>GC1</td>
<td>PE</td>
<td>GG1</td>
</tr>
<tr>
<td>GC2</td>
<td>PE</td>
<td>GG2</td>
</tr>
<tr>
<td>GG3</td>
<td>PP</td>
<td>GG3</td>
</tr>
<tr>
<td>GG4</td>
<td>PP</td>
<td>GG4</td>
</tr>
<tr>
<td>Material</td>
<td>PE</td>
<td>PP</td>
</tr>
<tr>
<td>Structure</td>
<td>Perforated, textured strip</td>
<td>Triaxial</td>
</tr>
<tr>
<td></td>
<td>Perforated, textured strip</td>
<td>Biaxial</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Biaxial</td>
</tr>
<tr>
<td>Technical Characteristics</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Tensile strength</td>
<td>at 5% strain (kN/m)</td>
<td>7.5</td>
</tr>
<tr>
<td>Ultimate strength</td>
<td>(kN/m) (MD/CMD)</td>
<td>9.5%/ -</td>
</tr>
<tr>
<td>Physical Characteristics</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Open Area (%)</td>
<td>15.83</td>
<td>22.97</td>
</tr>
<tr>
<td>A/D_{50}</td>
<td>3.03</td>
<td>3.03</td>
</tr>
<tr>
<td>Aperture shape</td>
<td>circle</td>
<td>circle</td>
</tr>
<tr>
<td>Aperture size (mm)</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>Cell depth (mm)</td>
<td>150</td>
<td>150</td>
</tr>
<tr>
<td>Thickness (mm)</td>
<td>1.5%</td>
<td>1.5%</td>
</tr>
<tr>
<td>Rib thickness (mm) (MD/CMD)</td>
<td>-/-</td>
<td>-/-</td>
</tr>
</tbody>
</table>

Note: PP: polypropylene, PE: Polyethylene, MD: Machine Direction, CMD: Cross Machine
Direction Note: \(^{a}\)ASTM 4885; \(^{b}\)ASTM 6637; \(^{c}\)ASTM 5199
Table 2. Summary of proposed models for capturing bearing resistance

<table>
<thead>
<tr>
<th>Reference</th>
<th>Bearing (passive ) resistance</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jewell (1990)</td>
<td>$P_{RB} = \left(\frac{L}{S}\right)\alpha_b H \times \left(e^{(\pi \tan \theta)} \tan^2 \left(45 + \frac{\phi'}{2}\right)\sigma_b\right)$</td>
<td>$S=$spacing between bearing members; $\alpha_b$ the fraction of total area available for bearing; $H=$the height of the reinforcement.</td>
</tr>
<tr>
<td>Chai (1992)</td>
<td>$\sigma_b = \frac{d_n}{\left(1 + \frac{d_n}{E_{ip} \sigma_{ult}}\right)}$</td>
<td>$P_{RB(\delta_i)}=$pullout bearing load; $d_n=$normalised displacement $E_{ip}=$the initial slope of bearing resistance curve; $\sigma_{ult}$is the ultimate value of the bearing stress.</td>
</tr>
<tr>
<td>Bergado et al. (1987)</td>
<td>$F_b = m A_b N_c C_u$</td>
<td>$m=$total number of the transverse members; $N_c=$the bearing capacity factor for a strip footing embedded in the soil; $A_b=$the cross sectional area perpendicular to direction of pull of the individual transverse members; $C_u=$undrained cohesion strength.</td>
</tr>
<tr>
<td>Moraci and Gioffrè (2006)</td>
<td>$P_{RB} = n_t n_{tb} A_b \sigma_b'$</td>
<td>$n_t=$number of geogrid bearing members; $n_{tb}=$number of nodes in as transverse element; $A_b=$area of each rib element; $\sigma_b'$=effective bearing stress on the geogrid bearing members.</td>
</tr>
<tr>
<td>Gurung and Iwao (1999)</td>
<td>$T_b = A_b (C N_c + \sigma_n' N_q) (1 - D I)$</td>
<td>$C=$cohesion of soil; $A_b=$is the bearing area of the transverse members; $N_q$and $N_c=$bearing capacity factor; $D I=$the degree of interface.</td>
</tr>
<tr>
<td>Bergado and Jin-Chun (1994), Bergado et al. (1993)</td>
<td>$\sigma_{bm} = c N_c + \sigma_n' N_q$</td>
<td>$N_q$and $N_c=$bearing capacity factor; $c=$cohesion of soil; $\sigma_n=$normal stress.</td>
</tr>
<tr>
<td>(Bergado and Teerawattanasuk 2001)</td>
<td>$P_b = L \sin(\alpha/2 - \theta) \times \left[\frac{U_m}{1 - \frac{U_m}{E_{ip}} + \frac{1}{D \sigma_{ult}}} + \frac{L \sin(\theta/2)}{2.5 L \sin(\theta/2)}\right]$</td>
<td>$\sigma_{ult} =$ultimate bearing strength; $E_{ip} =$initial slope of pull-out bearing resistance; $D =$diameter of transverse member; $L =$length of single transverse member; $\theta =$the rotational angle of a single transverse member; $\alpha =$initial angle of the transverse element; displacement due to deformation.</td>
</tr>
</tbody>
</table>
Table 3. Finite element properties of subballast and geocell used in current study

<table>
<thead>
<tr>
<th>Subballast</th>
<th>Density (kg/m³)</th>
<th>Poisson’s Ratio, ν</th>
<th>Elastic modulus (MPa)</th>
<th>Cohesion yield stress (kPa)</th>
<th>Angle of dilation, ψ (degree)</th>
<th>Friction angle, φ (degree)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,955</td>
<td>0.3</td>
<td>7</td>
<td>2</td>
<td>4</td>
<td>39</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Geocell (GG2)</th>
<th>Density (kg/m³)</th>
<th>Poisson’s Ratio, ν</th>
<th>Elastic modulus, $E_{geocell}$ (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>950</td>
<td>0.3</td>
<td></td>
<td>50 – 5,000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Plate</th>
<th>Density (kg/m³)</th>
<th>Poisson’s Ratio, ν</th>
<th>Elastic modulus, $E_{plate}$ (MPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2,000</td>
<td>0.3</td>
<td></td>
<td>500,000</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Subballast-geocell interface parameters</th>
<th>$E_{slip tolerance}$</th>
<th>Friction coefficient, δ</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.005</td>
<td></td>
<td>0.25 – 0.9</td>
</tr>
</tbody>
</table>
Figure 1. Loading mechanism of geocell-reinforced subballast in a typical railway environment.
Fig. 2. (a) Schematic illustration of (a) different geocell pockets used in this study and (b) schematic diagram of large-scale pull-out box apparatus (800×600×500 mm) and (c) subballast reinforced with GG2.
Fig. 3. Comparison between pull-out force and vertical strain ($\varepsilon_v$) of reinforced subballast.
Figure 4. Variation of mobilised strain in longitudinal ribs at (a) reinforced subballast with GG2 and (b) different types of geosynthetics.
Figure 5. (a) Typical stress characteristic for pull-out bearing failure; comparison of passive resistance ($\tau_{passive}$) at different opening area (OA) of different geosynthetics in: (b) current pull-out box, and (c) large-scale direct shear box.
Figure 6. Finite element discretization of: Full mesh (a and b); and half mesh (c and d) exploiting symmetry
Figure 7. Mobilised tensile strength predicted by FEM model with different number of elements (N).
Figure 8. (a) Typical geocell displacement during pullout force, and (b) variation of axial displacement of longitudinal ribs at different depth of geocell pocket.
Figure 9. Typical mobilised tensile strength in (a) geocell formed by geogrid GG2 and (b) at different depths of geocell pocket.
Figure 10. (a) normal stress developed over geocell strips; (b) passive resistance at different overburden pressures, (c) typical normal stress in the geocell-renforced subballast; and (d) passive resistance in the soil trapped in the geocell aperture.
Figure 11. Variations of mobilised tensile strength: (a) varying geocell stiffnesses ($E_{\text{geocell}}$); and (b) varying friction coefficient ($\delta$).
Figure 12. Variations of passive resistance: (a) varying geocell stiffnesses ($E_{\text{geocell}}$); and (b) varying friction coefficient ($\delta$).