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Z P. Xiong

University of Wollongong, zx868@uowmail.edu.au

A G. Kostryzhev

University of Wollongong, andrii@uow.edu.au

N E. Stanford

Deakin University

E V. Pereloma

University of Wollongong, elenap@uow.edu.au

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Abstract

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Microstructures and Mechanical Properties of Dual Phase Steel produced by Laboratory Simulated Strip Casting

Z.P. Xiong^{1*}, A.G. Kostryzhev¹, N.E. Stanford³, E.V. Pereloma^{1,2}

¹*School of Mechanical, Materials and Mechatronic Engineering, University of
Wollongong, Wollongong, NSW 2522, Australia*

²*Electron Microscopy Centre, University of Wollongong, Wollongong, NSW 2519,
Australia*

³*Institute of Frontier Materials, Deakin University, Geelong, Victoria 3216, Australia*

Abstract: Conventional dual phase (DP) steel (0.08C-0.81Si-1.47Mn-0.03Al wt. %) was manufactured using simulated strip casting schedule in laboratory. The average grain size of prior austenite was $117\pm44\ \mu\text{m}$. The continuous cooling transformation diagram was obtained. The microstructures having polygonal ferrite in the range of 40-90 %, martensite with small amount of bainite and Widmanstätten ferrite were observed, leading to an ultimate tensile strength in the range of 461 – 623 MPa and a corresponding total elongation in the range of 0.31 – 0.10. All samples exhibited three strain hardening stages. The predominant fracture mode of the studied steel was ductile, with the presence of some isolated cleavage facets, the number of which increased with an increase in martensite fraction. Compared to those of hot rolled DP steels, yield strength and ultimate tensile strength are lower due to large ferrite grain size, coarse martensite area and Widmanstätten ferrite.

Key words: Strip casting; Dual phase steel; Continuous cooling transformation diagram; Mechanical properties; Crussard-Jaoul model; Electron microscopy

*Correspondence author email address: zuileniwota@126.com (Z.P. Xiong)

1. Introduction

Dual phase (DP) steels are widely used in automotive industry due to a good combination of continuous yielding behaviour, high strength, high strain hardening rate, low yield stress-to-tensile strength ratio and good formability [1-3]. DP steels have high tensile strength in the range of 500 ~ 1200 MPa and total elongation in the range of 12 ~ 34%, which depend on fractions of ferrite, martensite and bainite [1, 4]. Traditional microstructures of DP steels consist of polygonal ferrite and martensite. To satisfy custom requirements, ferrite-bainite-martensite and ferrite-bainite steels were produced in order to modify mechanical properties: bainite instead of martensite were shown to improve formability with a little decrease of strength [5-7]. The effect of martensite fraction, distribution and martensite region size, and the effect of ferrite fraction and grain size on mechanical behaviour of DP steels have been intensively studied. With increasing the martensite fraction, the yield strength and ultimate tensile strength increase while uniform and total elongations decrease [8, 9]. The distribution of martensite also affects the mechanical behaviour [10-12]. Martensite regions existing as isolated areas within ferrite matrix result in a better combination of strength and ductility than martensite regions forming a chain-like network structure surrounding ferrite [10]. Refinement of ferrite or/and martensite regions simultaneously enhances strength and ductility [13-16]. Ultrafine-grained DP steels with the average ferrite grain size of ~1.2 μm exhibit a high ultimate tensile strength up to 1000 MPa [13].

In industry, the DP steels are successfully produced using hot rolling and cold rolling & annealing [1]. As alternative, the strip casting could be suggested as a more economic and environmentally friendly way for DP steels production. This technology is already used for carbon steels, silicon steels and stainless steels in industry [17, 18]. It allows obtaining several millimetres thick strips directly from molten metals [17, 18]. Due to this and elimination of many subsequent hot rolling stages required by conventional continuous casting and thin slab casting, the strip casting process has many advantages, such as energy saving and emission reduction, lower capital and operating costs, a smaller and more flexible operating regime, a higher tolerance to a high residual scrap and easy adjustment for different steel grades [17-20].

In this study, the feasibility of producing DP steel using strip casting was investigated in the laboratory. Heat treatment schedules were designed to obtain microstructures with 40% ~ 90% ferrite. Mechanical properties were tested and compared to hot rolled DP steels. The correlation between microstructure and mechanical properties was analysed.

2. Materials and experimental techniques

The chemical composition of studied DP steel is shown in Table 1. Square specimens of $36 \times 36 \text{ mm}^2$ and 1.2 mm thickness and cylindrical specimens of 20 mm diameter

and 6 mm length were produced via dip tester at Deakin University in order to simulate rapid cooling during solidification in strip casting process [21]. The dip tester is used to immerse a copper substrate into molten steel for a short and controlled period of time to simulate a rapid solidification. As-cast microstructure consisted predominantly of martensite and some bainite as shown in Fig. 1.

Heat treatments were carried out using a Theta Dilatronic III Quenching and Deformation dilatometer. It was operated under a vacuum of $\sim 6.7 \times 10^{-2}$ Pa which prevented oxidation and decarburization of the samples. The temperature was measured using an S-type (Pt/Pt-10%Rh) thermocouple spot-welded to the surface centre of a cylindrical and flat samples (Fig. 2).

To simulate the prior austenite grain size (PAGS) observed in cast samples, the flat samples (Fig. 2b) were heated at a rate of 30 Ks^{-1} to 1250 or 1300 °C, held for 120 or 180 s, and then helium quenched to room temperature at a rate of around 140 Ks^{-1} .

To obtain the continuous cooling transformation (CCT) diagram, cylindrical samples (Fig. 2a) were heated at a rate of 30 Ks^{-1} to 1300 °C, held for 180 s to simulate the grain size and distribution of prior austenite in strip casting, and then cooled to room temperature at cooling rates of 0.1, 1, 3, 10, 40 and 90 Ks^{-1} .

The schedule to simulate strip casting process is illustrated in Fig. 3.a. The samples were heated at a rate of 30 Ks^{-1} to the austenitisation temperature $T_A=1300 \text{ °C}$, held for time $t_A=180 \text{ s}$, cooled to the austenite-to-ferrite transformation region at a rate of 90 Ks^{-1} or cooled to 1000 °C at a rate of 30 Ks^{-1} and then cooled at a rate of 10 Ks^{-1} (hereafter referred as 30-10 Ks^{-1} schedule) to ferrite formation temperature T_F , held for t_F time to achieve the desired ferrite fraction, and then quenched to the room temperature at 140 Ks^{-1} using helium.

Following the heat treatments, the specimens were cross-cut in the centre perpendicular to the long axis. The centre area of the cross section was used for observation. To reveal the prior austenite grain boundaries, the specimens were etched for 15~20 s at 65 °C temperature in the solution of saturated picric acid in ethanol plus few drops of benzene sulfonate. Equivalent grain diameter was utilised to describe the distribution of prior austenite grain sizes. Approximately 150 ~ 250 grains were measured for each condition. Etching with 2 vol.% nital was used to reveal ferrite and martensite. Microstructures and fracture surfaces were studied using a Leica DMR research optical microscope (OM), a JEOL JSM-7001F field emission gun – scanning electron microscope (FEG – SEM) operating at 15 kV of accelerating voltage and fitted with an 80 mm² X-Max energy dispersive X-ray spectroscopy (EDS) detector, and a JEOL 2011 transmission electron microscope (TEM) operating at 200 kV. Thin foils for TEM were prepared using twin jet electropolishing method with an electrolyte containing 10% of perchloric acid and methanol. The volume fraction of retained austenite was measured using the X-ray diffraction (XRD) technique. XRD

was conducted for a scattering angle $2\theta = 38-150^\circ$ on the surface of flat samples (Fig. 2b) after electropolishing. Fractions of phases were calculated based on pixel quantities of different grey scales using Image Pro-Plus and Photoshop software. The equivalent circle diameter was calculated using at least 260 ferrite grains or martensite regions.

Tensile testing employed sub-sized specimens (Fig. 3.b) and an in-house modified “Kammrath and Weiss GmbH” tensile stage with 5 kN load cell. The thickness of tensile test samples was between 0.8 and 1.0 mm. Tensile tests were carried out on a minimum of two dog-bone samples per condition at an initial strain rate of $4 \times 10^{-4} \text{ s}^{-1}$. The strain hardening rate (θ) and strain hardening exponent (n) were calculated as follows,

$$\theta = d\sigma / d\varepsilon \quad (1)$$

$$n = d(\ln \sigma) / d(\ln \varepsilon) \quad (2)$$

where σ is true stress and ε is true strain [22].

3. Results

3.1 Prior austenite microstructure simulation

Fig. 4 shows typical prior austenite grain structures in as-cast and heat treated samples. PAGS distributions after different austenitisation schedules are shown in Fig. 5. PAGS increased with an increase in holding time or holding temperature: after holding at 1250°C for 120 and 180 s, the average grain size was 48 ± 19 and $83 \pm 37 \mu\text{m}$ respectively; while after holding at 1300°C for 120 and 180 s, the average grain size was 72 ± 30 and $117 \pm 44 \mu\text{m}$ respectively. The average grain size after holding at 1300°C for 180 s ($117 \pm 44 \mu\text{m}$) was very close to that of as-cast sample ($118 \pm 57 \mu\text{m}$). In addition, the sample held at 1300°C for 180 s had comparable prior austenite grain size distribution to that of as-cast sample (c.f. Fig. 5a and e). Therefore, this condition was selected for all future experiments.

3.2 Continuous cooling transformation diagram

The CCT diagram is plotted in Fig. 6 while the corresponding microstructures are shown in Fig. 7. Ferrite and pearlite formed at the cooling rate of 0.3 Ks^{-1} . When the cooling rate was increased to 1 Ks^{-1} , bainite started to form. A small amount of pearlite was still observed at 3 Ks^{-1} . With cooling rate increasing to 10 and 40 Ks^{-1} , more bainite formed and a very little fraction of allotriomorphic ferrite was found at prior austenite grain boundaries. When cooling rate reached 90 Ks^{-1} , the microstructure was fully bainite and martensite. At 90 Ks^{-1} the bainite transformation start temperature (B_s) was determined to be 644°C , whereas martensite started to form at $M_s = 426^\circ\text{C}$. As expected [23], austenite to ferrite transformation start (A_{r1}) and finish (A_{r3}) temperatures tended to decrease with increasing cooling rate. However, the bainite start transformation temperature at first decreased with an increase in cooling rate up to 3 Ks^{-1} from 468 to 398°C , and then increased with

further increasing cooling rate up to 90 Ks^{-1} , which corresponds to observations by other researchers [24, 25].

3.3 Effect of holding temperature, holding time and cooling rate on austenite to ferrite transformation

Based on the CCT diagram, four holding temperatures of 600, 650, 670 and 700 °C were chosen to investigate ferrite formation. For the cooling rate of 90 Ks^{-1} from austenitisation temperature to ferrite formation temperature, the Time-Temperature-Transformation (TTT) diagram is illustrated in Fig. 8a. As seen from this diagram, holding at 650 °C required a minimum time to start ferrite formation. Therefore, the temperature of 650 °C was selected for investigation of the effect of time on ferrite formation.

A dependence of ferrite fraction on holding time for two cooling rates is plotted in Fig. 8b. For the cooling rate of 90 Ks^{-1} , the ferrite formation was fast within the first 100 s of holding. Then, the formation of ferrite continued at a slower rate until reaching $81 \pm 2\%$, the value corresponding to that defined by the lever rule. For the cooling schedule of $30\text{-}10 \text{ Ks}^{-1}$, ferrite formed during cooling from 1300 to 650 °C, as evident by the presence of $20 \pm 6\%$ ferrite in the sample immediately quenched on reaching 650 °C. Cooling with $30\text{-}10 \text{ Ks}^{-1}$ schedule resulted in a higher ferrite fraction for the same holding time (Fig. 8b), compared to the cooling at 90 Ks^{-1} . In addition, cooling with $30\text{-}10 \text{ Ks}^{-1}$ schedule better depicts the industrial ones [20, 21]. Thus, the microstructures and mechanical properties were characterised only for the samples with the cooling rate of $30\text{-}10 \text{ Ks}^{-1}$ in the following sections.

3.4 Microstructure characterisation

Microstructures of samples cooled at $30\text{-}10 \text{ Ks}^{-1}$ and held at 650 °C for different times are shown in Figs. 9, 10 and 11. The ferrite fractions of 0.42 ± 0.06 , 0.64 ± 0.05 , 0.78 ± 0.01 and 0.85 ± 0.03 were obtained after holding for 30, 40, 50 and 60 s, respectively (Fig. 9). Hereafter, these samples were denoted as DP 30, DP 40, DP 50 and DP 60, respectively. The microstructures for all holding times consisted of polygonal ferrite, martensite, and very little amounts of bainite and Widmānstatten ferrite (Figs. 10 and 11). The XRD measurements showed the absence of face-centred cubic phases (Fig. 12). This suggests the absence of retained austenite or its amount below the detection level by XRD. In addition, martensite regions (indicated by arrows in Fig. 10c and d) exhibited concave and convex shape. As an example, the details of microstructure for DP 40 condition are shown in Fig. 11. Optical microstructure (Fig. 11 a) shows a general view of microstructure, containing $64 \pm 5\%$ polygonal ferrite and Widmānstatten ferrite with martensite regions. A small amount of bainite was found in martensite regions using SEM (Fig. 11b). A general view of martensite packets in regions surrounded by polygonal ferrite is seen in bright field TEM image in Fig. 11c. Equiaxed polygonal ferrite grains with a low dislocation

density are visible in Fig. 11d. Lath martensite with high dislocation density, which formed packets, is shown in Fig. 11e. Unfortunately, Widmānstatten ferrite and bainite were not found using TEM because of their low density.

Grain sizes of ferrite and sizes of martensite regions are given in Table 2 while their representative distributions are plotted in Fig. 13. The average grain size of ferrite was around 20 μm while the average size of martensite regions was around 15 μm . The microstructure was inhomogeneous, i.e. a large size difference of one to two orders of magnitude between the largest and smallest grains was observed. DP 40, DP 50 and DP 60 had a log-normal grain size distribution of ferrite (Fig. 13c shows a representative distribution) while DP 30 exhibited an exponential grain size distribution of ferrite (Fig. 13a). All of the samples had an exponential size distribution of martensite regions (representative distributions are shown in Figs. 13b and d). Polygonal ferrite nucleated at prior austenite grain boundaries. As holding time increased, polygonal ferrite grains grew, resulting in larger grain size (c.f. Fig. 13a and c). Meanwhile, prior austenite was consumed, leading to smaller size of martensite regions after quenching (c.f. Fig. 13b and d).

3.5 Mechanical properties

Typical round-house engineering stress-strain curves inherent in DP steels [10, 26] were also observed in our steel for all four heat treatment conditions (Fig. 14a). With a decrease in ferrite fraction from 0.85 to 0.42 the yield strength (YS) and ultimate tensile strength (UTS) increased from 290 to 381 MPa and from 461 to 623 MPa, respectively (Table 3), while the corresponding uniform elongation and total elongation decreased from 0.17 to 0.063 and from 0.31 to 0.10, respectively. These types of behaviour correspond to those in hot rolled DP steels [9, 27]. The product of UTS and total elongation, which can be used to characterise toughness, increased with increasing ferrite fraction (Table 3).

The strain hardening rate decreased with strain following an exponential function (Fig. 14b). With decreasing ferrite fraction, the strain hardening rate increased. The strain hardening exponent for all heat treatment conditions increased steeply at low strains and then saturated (Fig. 14c). However, the behaviour of strain hardening exponent varied with ferrite fraction. A sample having a lower amount of ferrite (larger amount of martensite) showed the maximum of the exponent at lower strains. With further straining, the exponent decreased more quickly for a sample with a lower ferrite fraction. For example, it quickly increased to a maximum value of 0.22 at a true strain of 0.03 and then quickly decreased to 0.12 for DP 40. DP 60 showed a more gradual increase to a maximum value of 0.20 at a true strain of 0.08 and then a gradual, slightly fluctuated decrease to 0.17 at a true strain of 0.14.

3.6 Fractography

Although the necking behaviour was observed for all four processing conditions, it varied with ferrite fraction. With an increase in ferrite fraction, the fracture surface at low magnification changed from flat to uneven and to conical shape (Fig. 15a1 - d1), and the fracture surface at high magnification showed larger and deeper voids at high magnification, the density of which increased with an increase in ferrite fraction (c.f. Fig. 15a2 and d2). The sample with 85% ferrite exhibited a ductile fracture surface characterised by many voids (Fig. 15d2). However, when ferrite fraction increased to 0.42, the fracture surface consisted of many smaller voids and some larger cleavage facets (Fig. 15a2), indicating the predominant ductile with some brittle fracture. These support the transition to a more ductile behaviour with an increase in ferrite fraction. Besides, in some voids the MnS inclusions were observed for all heat treatment conditions (Fig. 16), which could be a site for void formation [6, 28].

4 Discussion

4.1 The effect of ferrite fraction on mechanical behaviour

In the studied steel YS increased with a decrease in ferrite fraction (an increase in martensite fraction) due to dislocation density in ferrite increasing with volume change accommodation of martensite formation [29]. There is non-uniform distribution of dislocations within ferrite grains: low density within the grains (Fig. 17a); medium density in the regions adjacent to ferrite-ferrite boundaries (Fig. 17b); high density in the regions adjacent to martensite due to accommodation of volume change during austenite to martensite transformation (Fig. 17 c) [29]. As ferrite fraction increases, there are fewer regions adjacent to martensite. Thus, the overall density of dislocations in ferrite is lower. It results in lower yield strength because when the density of dislocations is low, it is easy for existing dislocations to move unobstructed due to less interaction between the dislocations [16]. The generation of new dislocations in the material with a low density of dislocations is also easier, as the material has capacity for energy storage [14]. During the tensile test, more dislocations piled up near ferrite-martensite interfaces. With increasing ferrite fraction, ferrite-martensite interfaces decreased, leading to a lower YS. This also was observed in Ref [9]. Furthermore, with decrease in the fraction of martensite regions the overall strength of the material is reduced according to the law of mixtures [28].

The initial strain hardening rate and initial strain hardening exponent increased with a decrease in ferrite fraction (Fig. 14b and c) due to an increased initial density of dislocations leading to an earlier dislocation immobilisation and pile-up [9, 16, 26]. The samples with a larger ferrite fraction had a more gradual increase and then a slower decrease in strain hardening exponent. The samples with a lower ferrite fraction exhibited a sharp increase in the strain hardening exponent during early stages of straining, which could be explained by the more rapid increase in the number of dislocations in ferrite. Higher dislocation density in ferrite would result in a reduced mean free path for dislocation movement and a higher dislocation generation rate leading to an earlier increase in the strain hardening exponent. Finally, this led to

a decreased elongation to failure in samples with lower ferrite fraction. Due to a higher amount of soft phase, the samples with a higher ferrite fraction exhibited more ductile fracture behaviour.

To analyse the multistage strain hardening behaviour in the studied steel the modified Crussard-Jaoul (C-J) model was used [30]:

$$\varepsilon = \varepsilon_0 + c\sigma^m \quad (3)$$

where ε_0 is the initial true strain, c is a constant and m is the strain hardening index. m can be calculated using the following equation:

$$\ln(d\sigma / d\varepsilon) = (1 - m) \ln \sigma - \ln(cm) \quad (4)$$

The plots of $\ln(d\sigma/d\varepsilon)$ versus $\ln\sigma$ are shown in Fig. 14d. The strain hardening behaviour showed three stages, which is a typical phenomenon for DP steels [5, 16, 26]. As the modified C-J analysis was unable to fit the flow curve over the entire uniform strain range region, values of strain hardening index m for each strain hardening stage are listed in Table 4. A smaller strain hardening index m means higher strain hardening ability. The rate of dislocation accumulation is strongly linked to the ferrite grain size. In this regard, the finer ferrite grain size the smaller is m_1 . As could be seen from Table 4, DP 40 and DP 50 samples with the lowest average grain sizes (Table 2) display the lowest m_1 values. During Stage 1 coarse ferrite grains deformed preferentially because smaller ferrite grains withstood the lower strain [31]. A small fraction of coarse ferrite grains did exist as shown in Figs. 9, 13a and 13c. During Stage 2, ferrite grains were further strain hardened and restrained by martensite with dislocations piling up in the regions adjacent to martensite, resulting in a lower value of m_2 than m_1 for the DP 50 and DP 60 samples, which have high ferrite fractions. On the other hand, the $m_2 > m_1$ value for DP 30 and DP 40 conditions, as higher m -values are associated with the larger martensite fraction [5, 16]. In addition, Widmnstatten ferrite may contribute to deformation in this stage. During Stage 3 the simultaneous deformation of strain hardened ferrite and martensite took place, leading to a continuous decrease in strain hardening rate and higher m_3 -values compared to m_1 and m_2 . For all conditions, m_1 is around 5.0 when ferrite fraction is in the range of 0.64 to 0.85. As ferrite fraction decreased to 0.42, m_1 increased to 6.4. It is probably because higher martensite fraction affected almost all ferrite grains and induced much more dislocations in ferrite induced by martensite formation [26, 29, 32], resulting in a decrease in strain hardening ability. m_2 increased with a decrease in ferrite fraction, due to a higher restraint from deformation of ferrite grains by martensite regions, which led to a decrease in strain hardening ability. m_3 increased with an increase in martensite fraction because martensite has less ability to strain harden due to a very high initial dislocation density and the ferrite is already more strain hardened when the amount of martensite is higher. The value of m calculated using the experimental data for entire strain hardening region increased with decreasing ferrite fraction, which qualitatively corresponds to the discussed above increase in m_2 and m_3 and also

to an increase in strain hardening exponent (Fig. 14c).

4.2 Comparison with mechanical properties of hot rolled DP steels

Fig. 18 compares the mechanical properties of the present samples with DP steels that have been conventionally processed. It can be seen that the UTS and YS of the studied DP steel are lower than those of hot rolled ones, while the total elongation is relatively higher [2, 10, 13, 27, 33-39]. The product of UTS $\times$ total elongation is relatively lower than that of hot rolled ones, which suggests a lower toughness in the studied steel compared to the reference steels. According to the microstructure observation (Figs. 9, 10, 11 and 17) and metallographic analysis (Figs. 13 and Table 2), ferrite grain size and its distribution, size and shape of martensite regions, and presence of Widmānstatten ferrite could be responsible for the lower combination of mechanical properties.

A very coarse prior austenite grain size of $117\pm44\text{ }\mu\text{m}$ resulted in a large grain size of ferrite due to a small number of ferrite nucleation sites. It is detrimental to YS, UTS and toughness. Based on the Hall – Petch equation ($\sigma = \sigma_0 + kd^{1/2}$, where σ_0 is lattice friction stress, k is constant, d is average grain size and σ is YS), YS and UTS decrease with increasing grain size [14]. For example, with an increase in ferrite grain size from 1.2 to 12.4 μm when the ferrite fraction was 0.7, YS and UTS decreased by 80 and 167 MPa, respectively [13]. The studied here DP steel had the ferrite grain size of around 20 μm (Table 2), which reflected in significantly reduced strength. The size of martensite regions also affects the strength [16]. Large size of martensite regions is harmful to mechanical properties, due to a decrease in geometrically necessary dislocations and effective barriers to dislocation motion in ferrite [16, 40-42]. In addition, the size distribution of martensite regions was not homogeneous, as shown in Figs. 9, 13b and d. Some martensite regions exceeding 50 μm (Table 2 and Fig. 13) could reduce ductility, because a coarser martensite may crack at lower strains following stress accumulation [31, 40].

In studied steel the ferrite grains were mostly of a polygonal shape while martensite regions exhibited less regular shape and had some concave and convex profiles as indicated by the arrows in Figs. 10c and d. Such shapes of martensite regions can be explained by a variation in the rates of growing polygonal ferrite from prior austenite boundaries. As demonstrated using *in situ* tensile test in Ref [43], concave and convex parts of martensite regions easily induce stress concentration and plastic deformation localisations, which lead to earlier void formation along the tensile direction and reduce fracture strain.

Widmānstatten ferrite was observed in all four samples as shown in Figs. 10a and b, although it is not common in DP steels. Widmānstatten ferrite can form following polygonal ferrite formation [44]. In our DP steel, a very coarse prior austenite grain size ($117\pm44\text{ }\mu\text{m}$) led to the large remaining austenite areas after the polygonal ferrite

formation during holding. This large remaining austenite grains facilitated the formation of Widmānstatten ferrite [45, 46]. Moreover fast cooling following holding at 650 °C also facilitated the formation of Widmānstatten ferrite [46, 47]. According to Ref [46], Widmānstatten ferrite may increase YS and UTS. However, in the studied DP steel, it also could contribute to the decrease in elongation to failure due to the stress concentration around the tips of Widmānstatten ferrite.

Compared to hot rolling, the studied processing route here did not carry out deformation. In hot rolling deformation in austenite temperature region or in the two-phase region results in an increase in dislocation density and deformation bands in ferrite, and elongated structure [48], leading to the increase in YS and UTS [49, 50]. In the studied DP steel, the dislocation density in ferrite was low (Fig. 17 a and b). On the other hand, deformation facilitates the nucleation and growth of polygonal ferrite, leading to a decrease in the amount of Widmānstatten ferrite [51], a decrease in ferrite grain size and the size of martensite regions [37, 52, 53]. All the aspects of microstructure development discussed here will be taken into account in further technology optimisation.

5. Conclusion

The characterisation of microstructure and mechanical properties of DP steel produced by the laboratory simulated strip casting leads to the following conclusions:

- (1) The developed processing route for simulation of the strip casting in laboratory, resulted in DP steel microstructures containing 40~90 % polygonal ferrite, martensite and small amounts of bainite and Widmānstatten ferrite.
- (2) For DP steel with nominal composition of 0.08C-0.81Si-1.47Mn-0.03Al, wt. %, experimental CCT and TTT diagrams were obtained. The nose temperature of ferrite formation field was determined being around 650 °C. Decreasing the cooling rate from austenitisation temperature to 650 °C resulted in larger fraction of ferrite formed.
- (3) The variation of ferrite fraction in DP steel resulted in an ultimate tensile strength in the range of 461 ~ 623 MPa and a corresponding total elongation in the range of 0.31 ~ 0.10. The better strain hardening behaviour was displayed by the samples having higher ferrite fraction (such as 0.42 and 0.64). The strain hardening behaviour of studied steels was similar to that of hot rolled DP steels and was characterised by three stages according to modified Crussard-Jaoul model.
- (5) The predominant fracture mode was ductile, with the presence of some isolated cleavage facets, the amount of which increased with an increase in martensite fraction.
- (4) Comparison of mechanical properties of the studied steel with those of hot rolled

DP steels showed the lower yield stress and ultimate tensile strength, although the comparable elongation in the former one, due to the large ferrite grain size, coarse martensite regions and the presence of Widmānstatten ferrite. The observed differences are associated with the absence of deformation in the utilised processing schedule.

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Figure captions

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Fig. 2 (a) Cylindrical samples used for the determination of continuous cooling transformation diagrams, and (b) flat samples used for prior austenite grain size measurement and simulation of strip casting.

Fig. 3 Schematic diagrams of (a) heat treatments to simulate strip casting and (b) tensile test sample.

Fig. 4 Comparison of prior austenite microstructures (a) in as-cast condition and (b) as-quenched after holding at 1300 °C for 180 s

Fig. 5 Prior austenite grain size distributions in (a) as-cast and (b-e) quenched conditions after holding at (b) 1250 °C for 120 s, (c) 1250 °C for 180 s, (d) 1300 °C for 120 s and (e) 1300 °C for 180 s

Fig. 6 Continuous cooling transformation (CCT) diagram of as-cast DP steel cooled from 1300 °C after holding for 180 s. *F* is ferrite, *P* is pearlite, *B* is bainite and *M* is martensite

Fig. 7 Microstructures after austenitising for 180 s at 1300 °C and cooling to room temperature at cooling rates of (a) 0.3, (b) 1, (c) 3, (d) 10, (e) 40 and (f) 90 Ks⁻¹. *F* is ferrite, *P* is pearlite, *B* is bainite and *M* is martensite

Fig. 8 (a) Time-Temperature-Transformation (TTT) diagram and (b) ferrite fraction versus holding time when holding at 650 °C

Fig. 9 Optical microstructures after holding at 650 °C for (a) 30 s, (b) 40 s, (c) 50 s and (d) 60 s. *PF* is polygonal ferrite

Fig. 10 Microstructures of DP 60 characterised using scanning electron microscopy. *PF* is polygonal ferrite, *WF* is Widmānstatten ferrite and *M* is martensite. Arrows in (c, d) point the concave and convex shapes of martensite regions.

Fig. 11 Representative microstructures of DP 40: (a) optical, (b) SEM and (c) TEM images. Higher magnification details of polygonal ferrite and lath martensite are shown in (d) and (e) respectively. *PF* is polygonal ferrite, *WF* is Widmānstatten ferrite, *B* is bainite and *M* is martensite. The zone axis of inset in (d) is $[001]_{\alpha}$ and of inset in (c, e) is $[111]_{\alpha}$.

Fig. 12 X-ray diffraction pattern of DP 40 sample

Fig. 13 The size distributions of (a, c) ferrite grains and (b, d) martensite regions for (a, b) DP 30 and (c, d) DP 60.

Fig. 14 (a) Engineering stress-strain curves for all studied conditions, (b) strain hardening rate and (c) instantaneous strain hardening exponent n as a function of true strain, and (d) strain hardening behaviours based on the modified Crussard-Jaoul model analysis, where three distinct stages of strain hardening were denoted by the vertical lines and numbers.

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Table 1 Chemical composition of the DP steel (wt. %).

C	Si	Mn	Al	Cu	Cr	P	S	B
0.0768	0.805	1.47	0.0346	0.0126	0.233	0.0055	<0.00050	0.00091

Table 2 A summary of microstructure statistics

Specimen	Ferrite fraction	Average size, μm		Largest size, μm		Smallest size, μm	
		Ferrite	Martensite	Ferrite	Martensite	Ferrite	Martensite
DP 30	0.42 $\pm$ 0.06	20 $\pm$ 15	17 $\pm$ 30	77	243	2	3
DP 40	0.64 $\pm$ 0.05	17 $\pm$ 10	10 $\pm$ 9	60	59	4	3
DP 50	0.78 $\pm$ 0.01	18 $\pm$ 10	12 $\pm$ 13	59	99	4	3
DP 60	0.85 $\pm$ 0.03	25 $\pm$ 14	16 $\pm$ 17	69	91	5	3

Table 3 Mechanical properties of DP steels

Specimen	Yield strength, MPa	Ultimate tensile strength, MPa	Uniform elongation	Total elongation	Product of ultimate tensile strength and total elongation, MPa%
DP 30	381 $\pm$ 28	623 $\pm$ 26	0.063 $\pm$ 0.007	0.10 $\pm$ 0.011	6230
DP 40	324 $\pm$ 17	582 $\pm$ 11	0.13 $\pm$ 0.001	0.20 $\pm$ 0.018	11640
DP 50	295 $\pm$ 21	489 $\pm$ 4	0.17 $\pm$ 0.001	0.29 $\pm$ 0.008	14181
DP 60	290 $\pm$ 16	461 $\pm$ 8	0.17 $\pm$ 0.005	0.31 $\pm$ 0.001	14291

Table 4 Comparison of the modified Crussard – Jaoul (C-J) analysis with the experimental results

Specimen	Modified C-J model			Experimental m^b
	m_1^a	m_2	m_3	
DP 30	6.4	8.7	16.4	16.4
DP 40	4.9	6.0	11.0	8.2
DP 50	5.0	4.9	7.0	6.1
DP 60	5.5	4.8	6.9	6.2

^a1 – m_{1-3} = slopes at Stage 1 to 3^b $m = 1/(\epsilon_u - \epsilon_y)$, where ϵ_u is maximum uniform true strain and ϵ_y is true strain at 0.2% offset proof stress