Parameter optimization of adaptive flux-weakening strategy for permanent-magnet synchronous motor drives based on particle swarm algorithm

Wei Xu  
*Huazhong University of Science and Technology*

Moustafa Magdi Ismail  
*Huazhong University of Science and Technology*

Yi Liu  
*Huazhong University of Science and Technology, yiliu@uow.edu.au*

Md Rabiul Islam  
*University of Wollongong, mrislam@uow.edu.au*

Follow this and additional works at: [https://ro.uow.edu.au/eispapers1](https://ro.uow.edu.au/eispapers1)

Part of the [Engineering Commons](https://ro.uow.edu.au/eispapers1), and the [Science and Technology Studies Commons](https://ro.uow.edu.au/eispapers1)

Research Online is the open access institutional repository for the University of Wollongong. For further information contact the UOW Library: research-pubs@uow.edu.au
Parameter optimization of adaptive flux-weakening strategy for permanent-magnet synchronous motor drives based on particle swarm algorithm

Abstract
Operating in the high-speed range is necessary for high-performance permanent-magnet synchronous motor (PMSM) drives. However, due to the back electromotive force effect, the PMSM is approaching the voltage limit at field decreasing scope. This paper presents a new flux-weakening scheme along with an improved vector control strategy to alleviate the influence of this problem. Control parameters of the anti-windup proportional and integral (AWPI) controller are optimized off-line in relying on an adaptive velocity particle swarm optimization (AVPSO) algorithm. The AVPSO algorithm considers the summation of AWPI measurement error which is the objective function of the optimization problem without knowing the transfer function of the plant. Hence, the tuned flux-weakening controller with a filter is used to set the flux level without saturating the current controllers. Meanwhile, the other controllers of inner and outer loops award a great dynamic and steady-state performance for the PMSM. In the proposed scheme, the flux-weakening control is not dependent on machine parameters that adapts the flux level automatically and provide a fast transition between the constant torque region and the field-weakening region. Effectiveness and advantages of the proposed scheme are presented in this paper through both simulation and experimental results.

Disciplines
Engineering | Science and Technology Studies

Publication Details

This journal article is available at Research Online: https://ro.uow.edu.au/eispapers1/3224
Parameter Optimization of Adaptive Flux-Weakening Strategy for Permanent-Magnet Synchronous Motor Drives Based on Particle Swarm Algorithm

Wei Xu, Senior Member, IEEE, Moustafa Magdi Ismail, Yi Liu, Member, IEEE, and Md Rabiul Islam, Senior Member, IEEE

Abstract—Operating in the high-speed range is necessary for high-performance permanent magnet synchronous motor (PMSM) drives. However, due to the back electro motive force effect, the PMSM is approaching the voltage limit at field decreasing scope. This paper presents a new flux-weakening scheme along with an improved vector control strategy to alleviate the influence of this problem. Control parameters of the anti-windup proportional and integral (AWPI) controller are optimized off-line in relying on an adaptive velocity particle swarm optimization (AVPSO) algorithm. The AVPSO algorithm considers the summation of AWPI measurement error which is the objective function of the optimization problem without knowing the transfer function of the plant. Hence, the tuned flux-weakening controller with a filter is used to set the flux level without saturating the current controllers. Meanwhile, the other controllers of inner and outer loops award a great dynamic and steady-state performance for the PMSM. In the proposed scheme, the flux weakening control is not dependent on machine parameters which adapt the flux level automatically and provide a fast transition between the constant torque region and the field weakening region. Effectiveness and advantages of the proposed scheme are presented in this paper through both simulation and experimental results.

Index Terms—Surface mounted permanent magnet synchronous motor (SMPMRS), anti-windup proportional and integral (AWPI) controller, tuning method, adaptive velocity particle swarm optimization (AVPSO), flux weakening control.

I. INTRODUCTION

Permanent magnet synchronous motor (PMSM) applications tend to have a higher initial cost. Hence, they may offer a smaller size for more compact mechanical packages, desirable torque to inertia ratio, high reliability, and more controllability [1], [2]. Recently, the high-performance PMSM drive system has been developed, which increases their reputation in electric vehicle applications [3-7]. In this application, instant response to the desired change, stability for the load variation, and minimizing the speed and torque ripple are necessary. For this reason, it is irresistible to work in the high-speed range.

In recent years, numerous methods have been developed for PMSM drive systems to extend the speed range [8-19]. In [9], a novel method of PMSM drive has been proposed to maximize the speed range. Ref. [9] presents a three-dimensional finite element to create a gap between a stator and a rotor in an axial direction without moving the current vector. However, the above methods heavily depend on the no-load back-emf, which is necessary through computation of the linkage magnetic flux of stator windings and d-axis and q-axis inductance. The presented method in [12] uses the single linear multiple-input multiple output predictive controller to calculate the required flux-weakening d-axis current. Meanwhile, a new linearization approach is adopted to get the lower peak ripples of electrical current and torque. This approach tackles the strong coupled nonlinear mathematical model of interior buried PMSM. The control scheme of [17] modifies the field-weakening control of surface mounted permanent magnet synchronous motor (SMPMRS). The influence of the resistive voltage drop in the stator windings has not been considered in their studies. Nevertheless, the method presented in [17] is strongly dependent on motor parameters and operating conditions, but they guarantee good stability and transient responses. The proposed method in [11] depends on the measurement of inverter characteristics and the resistance of the used cable. This control method uses the voltage difference between the input and output of the inverter to modify the compensated d-axis current. Additionally, a proportional-integral (PI) controller uses the reference q-axis current to set the maximum torque per voltage. Therefore, the maximum torque can be accomplished at a high-speed range. The authors, in [16], have developed the flux-weakening control method, which determines the d-q axes reference currents to drive a magnet-buried PMSM at any value of speed. This method minimizes the current magnitude to reach the reference torque considering the voltage and current limits and battery power. In [19], a single q-axis current regulator has been proposed to control the voltage angle. The advantages of this method are the stability in reaching the zero-load state and...
the fast-dynamic response of currents when current references are changed.

Various implementation methods of the nonlinear control theory have been used in the PMSM control system to improve the dynamic performances of critical issues such as torque disturbances and motor parameter variations [20-22]. A disturbance observer has been designed in [22] based on a nonsingular terminal sliding mode strategy to solve time-varying parameters and torque disturbances of the PMSM drive system. The system chattering can be compensated and reduced simultaneously, and it can achieve the smaller ripple in the presence of time-varying load. In [20], the authors estimate the disturbances and uncertainties of the current and speed loop based on a high-order sliding mode observer. Both the speed robustness and current tracking accuracy are increased by transmitting the estimated disturbances to a designed deadbeat-based predictive current controller.

This paper proposes an offline optimum tuning method for controllers that are constructing the suggested vector control strategy to utilize dc-link voltage as much as possible. The error measurement of the anti-windup PI controllers (AWPI) can be minimized to about zero depending on the adaptive velocity particle swarm optimization (AVPSO) algorithm. The optimization of the proposed fitness-function places emphasis on obtaining the best possible parameters for improving the stability of the system under load torque disturbances over a wide speed range. In the proposed control strategy, the field weakening compensator regulates the magnitude of the duty cycles to set the flux level without preventing the saturation of the current regulator. With the proposed control strategy, the SMPMSM performance is independent of parameter variations. The conventional flux weakening control (CFWC) has been presented in [18], which is a line modulation-based flux weakening control method. The performance of the proposed flux-weakening control (PFWC) is compared with the CFWC in this paper. Consequently, the main features of the PFWC can be summarized as follows:

1. The flux-weakening control loop of PFWC is supported by the low-pass filter that passes the signal with a lower frequency, thus raising and keeping the average of the d-axis reference current from falling suddenly. In contrast, the CFWC misses the filter causing the lower average of the d-axis reference current. The PFWC strategy is applicable to the interior PMSM because the proposed algorithm has no dependence on the structure difference between the surface magnets and embedded magnets. Taking into consideration, the parameters of the low-pass filter should be convenient with the parameters of the interior-magnet motor.

2. There is a primary difference between PFWC and CFWC in the structure of the PI controller, where the PI controllers of PFWC are supported by an anti-windup structure that affects positively in the transient period. Table I describes the main differences between the CFWC and the PFWC according to the analysis above.

This paper is systematized as follows. Section II represents the system description and model. Section III also introduces the PFWC and limitations of voltage and current. Moreover, this section presents the CFWC method. Additionally, Section IV presents the recommended off-line tuning method of a PI controller and the implementation of AVPSO algorithm. Afterwards, the proposed methods are numerically simulated in Section V, and verified by experimental results in Section VI. Finally, the conclusions are drawn in Section VII.

II. SYSTEM MODELING

Fig. 1 presents the basic block diagram of the surface mounted PMSM drive used in this paper for analysis. In this figure, the modified vector control drive commands the SMPMSM through a space vector PWM (SVPWM) based two-level voltage source inverter (VSI). The counting mechanical position and the measured phases currents are used as the control inputs. Moreover, the measured dc link voltage is used to calculate the output references of the duty cycles of the current regulators and to determine the onset point of the flux weakening. Considering that all the lower-case symbols are used to introduce instantaneous values and the upper case standing for the steady state. In SMPMSM with more than one magnet, the differential equations are defined as

\[
v_{di} = R_s i_{di} + \frac{d}{dt} \lambda_{dq} + \omega_r (L_s i_{dq} + \lambda_{mq}) \tag{1}
\]

\[
v_{dq} = R_s i_{dq} + \frac{d}{dt} \lambda_{dq} - \omega_r L_s i_{dq} \tag{2}
\]

where \( \lambda_{mq} \) is the flux linkage due to the rotor magnets linking the stator, \( L_s \) is the stator inductance, \( \omega_r \) is the electrical velocity of the rotor, and \( R_s \) is the stator resistance. Additionally, \( v_{di} \) and \( v_{dq} \) are d-q axes voltages, \( i_{di} \) and \( i_{dq} \) are d-q axes fluxes, \( \omega_r \) and \( \lambda_{dq} \) are d-q axes stator currents, respectively.

Moreover, the mechanical equation of the motor can be represented as

\[
J \frac{d\omega_m}{dt} = T_e - T_L - B \omega_m \tag{3}
\]

where \( \omega_m \) is the mechanical velocity of the rotor, \( T_L \) is the load torque, \( T_e \) is the electromagnetic torque, \( B \) is the viscous frictions coefficient, and \( J \) is the inertia of the shaft. Furthermore, the electromagnetic torque in a steady state can be given by

\[
T_e = \frac{3}{2} n_p \lambda_{qf} i_{qf} \tag{4}
\]

where \( n_p \) is the number of pair pole. The average model of VSI in \( d-q \) axes can be expressed as

\[
\begin{align*}
\frac{d i_{dq}}{dt} & = \frac{1}{3L_s} d_{dq} V_{dc} - \frac{\omega_r}{3L_s} \lambda_{dq} + \begin{bmatrix} -R_s & \omega_r \\ L_s & 0 \end{bmatrix} i_{dq} \\
J \frac{d V_{dc}}{dt} & = \frac{1}{3L_s} d_{dq} i_{qf}
\end{align*}
\tag{5}
\]
where $d_s$ and $d_q$ are $d$-$q$ axes duty cycles, $V_{dc}$ is dc-link voltage, $I_{dc}$ is dc-link circuit current, and $C$ is the dc-link equivalent capacitor. In addition, $i_{dqst}$, $d_{qst}$, and $\lambda_{qst}$ can be considered as $\left[i_{\alpha s} \ i_{\beta s}\right]$, $\left[d_{\alpha s} \ d_{\beta s}\right]$, and $\left[\lambda_{\alpha s} \ \lambda_{\beta s}\right]$, respectively.

The voltage vector magnitude ($\rho$) of VSI is indicating the region where the SMPMSM is working and can be determined by

$$\rho = \sqrt{v_a^2 + v_b^2} / \left(V_{dc} / \sqrt{3}\right)$$

where $\rho$ is the per-unit value of the voltage vector magnitude while the base value is the maximum voltage that the inverter can supply to the motor ($V_{dc} / \sqrt{3}$), $v_a$ and $v_b$ are the $\alpha$ and $\beta$ components of the voltage vector obtained by the reverse Park transformation with the inputs $v_{qst}$ and $v_{dst}$ of the VSI. As the main flux weakening problem, an increase in motor rotational speed comes with a proportional increase in the electromotive force term of (1). Therefore, the voltage is not efficient to control the current, and the torque becomes highly distorted. As a result, it is necessary to feed negative $d$-axis current for the extension of the motor speed range.

### III. FLUX-WEAKENING SCHEMES

#### A. Operating Limits in Flux-Weakening Scope

As mentioned before, the space vector PWM technique switches the VSI. A voltage vector under the flux weakening region was laying on the boundary of the hexagon, which limits the voltage identifying the maximum supply voltage ($V_{\text{max}} = V_{dc} / \sqrt{3}$) [11]. Moreover, both converter’s power rating and motor’s thermal rating are used to calculate the maximum current $I_{\text{max}}$. Accordingly, the voltage and the current limits of the motor can be expressed as

$$V_{\alpha}^2 + V_{\beta}^2 \leq V_{\text{max}}^2$$

$$I_{\alpha}^2 + I_{\beta}^2 \leq I_{\text{max}}^2 .$$

By omitting the resistance term in the high rotating speed range, the equations (1), (2), and (7) can be modified as

$$V_{\alpha}^2 + V_{\beta}^2 \leq V_{\text{max}}^2$$

$$I_{\alpha}^2 + I_{\beta}^2 \leq I_{\text{max}}^2 .$$

The equation (9) expresses the circle of a motor voltage limit with a radius of $V_{\text{max}} / (\omega L_s)$ and centered at $(-\lambda_m / L_s, 0)$. Fig. 2 shows the circles with a variable radius voltage limit; circle intersects with the constant radius current circle. As speed increases, the operating point moves from A to B. Consequently, the $q$-axis current point of the maximum torque is the cross point between the two circles, which can be defined as

$$I_q = L_s / (2\lambda_m) \sqrt{(2\lambda_m V_{\text{rms}} / L_s)^2 - ((\lambda_m / L_s - V_{\text{rms}} / (\omega L_s))^2 + I_{\text{rms}}^2)}$$

And then, the flux weakening current function of the speed can be expressed as

$$I_{\alpha} = -\sqrt{I_{\text{rms}}^2 - I_q^2} .$$

#### B. Proposed Flux-Weakening Strategy

Fig. 3 describes the block diagram of the proposed flux weakening control strategy based on the AWPI structure. In this structure, the integrator parameter is multiplying with the error of the PI controller, which is subtracting with the value of $\Delta y$ times by $K_{aw}$ as clarified in Fig. 3(a), where the symbol of “*$” are the reference values and the symbol of “$\star$” indicates the differential value. Also, $K_{aw}$ is the anti-windup variable which can be calculated as the ratio between the integral parameter to the proportional parameter ($K_i/K_p$), and $\phi^*$ is the AWPI controller error. A feature of the coordinated structure, the anti-windup structure (AWS) decreases the error of integral value to reduce the overshoot effect of saturation. Further, Fig. 3(c) presents the block diagram of the proposed control strategy. For improving the current response, the decoupling terms of (1) and (2) are
IEEE Transactions on Power Electronics

removed from the $d$-$q$ axes stator voltages references as follows:

$$
\begin{align*}
\tilde{v}_{\text{decoupling}}^d &= -L_d \omega_s \tilde{i}_d \\
\tilde{v}_{\text{decoupling}}^q &= L_q \omega_s \tilde{i}_q + \omega_s \lambda_m.
\end{align*}
$$

(12)

The error equations of the current AWPI controllers can be defined as

$$
\begin{align*}
\phi_1^d &= \frac{v_r^d}{K_{p-d}} + \int \frac{L_n}{K_{p-d}} - \frac{L_n}{K_{p-q}} i_d \omega_s - \frac{\lambda_m}{K_{p-d}} \omega_s - \tilde{i}_d^* + i_d \, \Delta \theta_d \\
\phi_2^d &= -\frac{v_r^d}{K_{p-q}} \phi_1^d + \int \frac{L_n}{K_{p-q}} - \frac{L_n}{K_{p-d}} i_d \omega_s - \frac{\lambda_m}{K_{p-q}} \omega_s - \tilde{i}_d^* + i_d \, \Delta \theta_d
\end{align*}
$$

(13)

where $K_{p-d}$ and $K_{p-q}$ are proportional and integral gains of the $q$-$d$ axes current controllers, $K_{awq}$ and $K_{awd}$ are the ratios between the integral gain to the proportional gain of the $q$-$d$ axes current controllers, $\phi_1^d$ and $\phi_2^d$ are the integrations of the error of the $q$-$d$ axes current controllers, $\phi_1^d$ and $\phi_2^d$ are the errors of the $q$-$d$ axes current controllers, respectively.

Furthermore, the error equation of speed AWPI controller can be described as

$$
\phi_3^s = \frac{v_r^s}{K_{p-s}} + \int \frac{K_m^2}{K_{p-s}} \Delta \omega_m - \omega_m^* + \omega_m
$$

(15)

where $K_{p-s}$ and $K_{p-d}$ are proportional and integral gains of the speed controller, respectively. $K_m$ is the ratio between $K_{p-s}$ to $K_{p-d}$ of the speed controller, $\phi_3^s$ is the error of the speed controller, and $\phi_3^*$ is the integration of the error of the speed controller.

The $q$-axis current maximum limit ($i_{q_{\text{max}}}$) generating the torque decreases with the increase of the absolute value of $d$-axis reference current which presenting as

$$
i_{q_{\text{max}}}^* = \sqrt{\frac{T_{\text{max}}}{\bar{d}^2}} - \frac{i_d^\prime}{2}.
$$

(16)

![Fig. 3. Proposed flux weakening scheme, where (a) Structure of anti-windup PI controller, (b) flux weakening vector control loop, and (c) modified vector control.](image-url)
Therefore, the \(d\)-axis current reference should be adjusted as much as possible to boost the torque.

The main idea of the PFWC part as shown in Fig. 3(b) is the employment of the magnitude of the compensated duty cycles \((D_{dl})\) to determine the outbreak of the decreased field. Even if the dc link voltage drops suddenly, the duty cycles feedback can adjust the flux level freely. Showing appreciation for this outer PFWC loop, the mission accomplishes automatically despite a motor parameters variation or a load disturbance. In other words, as the motor speed is getting higher, the performance of the current controllers is getting lower because the compensated voltages are reaching the maximum voltage limit.

In the flux-weakening region, if the magnitude of the compensated duty cycles exceeds the reference limit, then the controller senses the error of the duty cycles reflecting the current controller. Moreover, the outer loop is activated when \(D_{dl}\) is equal or higher than \(D_{dl_{\text{max}}}=1\), otherwise \(t_{di} = 0\). Fig. 3 (c) illustrates how to calculate the \(D_{dl}\) that can be derived as

\[
\begin{align*}
\Delta d' &= (v_{d}' - v_{d_{\text{comm}}})/V_{dc} - 1 \leq \Delta d' \leq 1 \\
\Delta d &= \sqrt{\Delta d'^2 + \Delta d'^2}, \quad D_{dl} \in [0, \sqrt{2}]
\end{align*}
\]  

where \(v_{d}'\) and \(v_{d_{\text{comm}}}\) are the output voltages of the \(q-d\) axes the current regulators, \(d'\) and \(d''\) are the compensated duty cycles of the \(q-d\) axes current regulators, respectively. Finally, the error equation of PFWC loop can be represented by

\[
\phi_i = \frac{i_{dc}}{K_{P,FW}} - K_{I,FW} \phi_i + \frac{K_{P,FW}^2}{K_{P,FW}} d'_{见效} - D_{dl_{max}} + D_{dl}
\]  

where \(K_{P,FW}\) and \(K_{I,FW}\) are the proportional and integral gains of the duty cycle controller, respectively. \(K_{P,FW}\) is the ratio between \(K_{F,CW}\) to \(K_{P,FW}\) of the duty cycle controller, \(\phi_i\) is the error of the duty cycle controller, and \(\phi_i\) is the integration of the error of duty cycle controller.

**C. Conventional Flux-Weakening Strategy**

Fig. 4 shows the block diagram of the CFWC system of the SMPMSM [18]. As indicated in this figure, the negative \(d\)-axis current is produced using the line-modulation loop enabling the SMPMSM to operate in the flux-weakening region. The maximum line modulation ratio is defined as

\[
\begin{align*}
m_{\text{max}} &= \delta_{\text{max}} - \delta_{\text{min}} \\
\delta_{\text{max}} &= \max\{\delta_a, \delta_b, \delta_c\} \\
\delta_{\text{min}} &= \min\{\delta_a, \delta_b, \delta_c\}
\end{align*}
\]  

where \(m_{\text{max}}\) is the maximum line-modulation-ratio, \(\delta_{\text{max}}\) and \(\delta_{\text{min}}\) are the maximum and minimum duty cycles, \(\delta_a, \delta_b, \text{and } \delta_c\) are the inverter duty cycles of leg-1, leg-2 and leg-3, respectively.

Besides, \(\delta_a\) and \(\delta_b\) can be defined as

\[
\begin{align*}
m_a &= u_a' / V_{dc} \\
m_b &= u_b' / V_{dc}
\end{align*}
\]  

\[
\begin{align*}
\delta_a &= m_a + \delta_a' \\
\delta_b &= m_b + \delta_b
\end{align*}
\]  

where \(u_a'\) and \(u_b'\) are the reference line voltage determining by inverse Park transformation of \(v_a'\) and \(v_b'\), \(m_a\) and \(m_b\) are the line-modulation-ratios, respectively.

In order to calculate \(\delta_c\), the median value of the duty cycle of leg-3 can be defined as

\[
\delta_c = \frac{\delta_{c_{\text{max}}} + \delta_{c_{\text{min}}}}{2}
\]  

where \(\delta_{c_{\text{max}}}\) and \(\delta_{c_{\text{min}}}\) are maximum and minimum values of the phase-c-based duty cycle, respectively. More details about the calculation method of \(\delta_c\) can be found in [18]. Moreover, the line modulation inverter technique of CFWC is used instead of SVPWM to generate the gate signals [23]. The reference value of \(d\)-axis current is zero except if \(m_{\text{max}} > 1\) the difference between \(m_{\text{max}}\) and \(m_{\text{max}}\) produces a negative reference current, where \(m_{\text{max}}\) is the reference maximum line-modulation-ratio. Meanwhile, the reference value of \(q\)-axis current is saturated at (16).

**IV. TUNING METHODOLOGY AND IMPLEMENTATION OF PROPOSED PARTICLE SWARM OPTIMIZATION ALGORITHM**

**A. Proposed Tuning Method**

Determination of the optimal control parameters of the PFWC strategy is essential to ensure the effectiveness of the system stability. This paper introduces a tuning method which is independent to the transfer function of the plant. However, the parameters determine the minimum value of the equilibrium point term (\(J(\dot{x}_i, \dot{u}_i)\)) of Taylor series are the optimal parameters. Equation (23) defines Taylor series expansion as

\[
\begin{align*}
J(\dot{x}, \dot{u}) &= J(\dot{x}_0, \dot{u}_0) + \frac{\partial J(\dot{x}_0, \dot{u}_0)}{\partial \dot{x}} (\dot{x} - \dot{x}_0) + \frac{\partial J(\dot{x}_0, \dot{u}_0)}{\partial \dot{u}} (\dot{u} - \dot{u}_0) + \frac{1}{2!} \left[ \frac{\partial^2 J(\dot{x}_0, \dot{u}_0)}{\partial \dot{x}^2} (\dot{x} - \dot{x}_0)^2 + \frac{\partial^2 J(\dot{x}_0, \dot{u}_0)}{\partial \dot{u}^2} (\dot{u} - \dot{u}_0)^2 + \frac{\partial^2 J(\dot{x}_0, \dot{u}_0)}{\partial \dot{x} \partial \dot{u}} (\dot{x} - \dot{x}_0)(\dot{u} - \dot{u}_0) \right] + \cdots
\end{align*}
\]  

where the subscript “0” indicates the equilibrium point value. The performance of the PI controller highly depends on the selection of the equilibrium point in the flux weakening region. Hence, the equilibrium point term (\(J(\dot{x}_i, \dot{u}_i)\)) of PFWC strategy can be calculated from (1)-(3), (13)-(15) and (18) as (24).

The proposed fitness function can be redefined as

\[
\text{Minimize } \sum_{i=1}^{4} \phi_i.
\]  

For this purpose, the proposed AVPSO algorithm [24] is applied to minimize the fitness function to zero by finding the optimal gains of the proportional and integral.
B. Implementation of the Proposed Adaptive Velocity Particle Swarm Algorithm

The particle swarm optimization (PSO) algorithm starts by generating the initial position, and initial best local location \( \vec{V}_i \) and \( \vec{b}_i \) of each of the \( n \) particles. After this initialization step, the PSO would implement a finite loop corresponding to the optimal particle position \( \vec{V}_i \) and its corresponding to the optimal particle position \( \vec{p}_i \). The stopping criterion of this loop is the continuity of the global best solution without change for more than 12 iterations, or the counter reaches one hundred iterations.

Focusing on the AVPSO algorithm against the proposed objective function, the evaluation procedure works in sight of knowing all fitness function variables. Consequently, the evaluation step faces a problem namely coefficients absent regarding \( \phi_i \), \( \phi_v \), \( \phi_s \), \( \phi_n \), \( \phi_i^* \), \( \phi_s^* \), \( \phi_v^* \), and \( \phi_n^* \). Therefore, it is necessary to call a separate AVPSO algorithm for each time during the evaluation of (25). In this interior optimization problem, the vector length of the particle equals 6 that can be defined as

\[
\bar{p}_i = (1 \times 6) = p_{\text{global}} \begin{bmatrix} p_{\text{global}} \\ p_{\text{global}} \end{bmatrix} \\
\text{where } p_{\text{global}} \begin{bmatrix} 1 : 200 \end{bmatrix}
\]

where \( p_{\text{global}} \) is the global best particle location that corresponding to the global minimum solution \( g_{\text{best}} \) and its corresponding to the optimal particle position \( p_{\text{global}} \). In addition, the internal PSO algorithm has the same equations for updating the velocity and position as the outer AVPSO algorithm. Besides, \( \bar{V}_i \) indicates the \( k \)th particle position, \( \bar{b}_i \) the best \( k \)th local particle location, \( p_{\text{best}} \) the global best particle location that corresponding to the \( k \)th particle of the minimum evaluation, \( g_{\text{best}} \) the evaluation vector of the \( k \)th particle position, \( g_{\text{best}} \) the minimum value for \( g_{\text{best}} \), \( V_k \) the \( k \)th updated particle velocity, and \( \vec{p}_i \) the \( k \)th updated position. Finally, the internal PSO algorithm evaluates the proposed fitness function under the sight of the updated particle position \( \vec{p}_i \) of the outer AVPSO algorithm. Meanwhile, the outer PSO algorithm explores a lower value than that obtained in previous iterations.
V. SIMULATION RESULTS

To evaluate the performance of the proposed SMPMSM drive system a model is developed in the MATLAB/Simulink software environment. The main parameters of the motor are listed in Table II. A simulation block is designed to find the optimal gains of AWPI controllers in the proposed control strategy by using the proposed tuning method. The optimization problem of (25) is designed based on the proposed optimization algorithm with the population size of 50 and the generation number of 100. In Fig. 7, the optimization algorithm achieves the minimum error of about 1.10134e-13 standing for the optimal tuning at 39 iterations. For this purpose, it decided to stop near 51 generation. Moreover, Table III presents the optimal parameters obtained by using the proposed off-line optimization method. Fig. 8 shows the frequency domain analysis of the control system. As presented in Fig. 8(a), the open loop bode diagram of the speed controller indicates the minimum stability of gain margin of about -324 dB and a phase margin of about 95.7 degrees at a crossover frequency of 0.647 kHz. Moreover, the peak gain also is 436 dB at the frequency of 1.59e-24 kHz. In the similar process, Fig.8(b) exhibits the open loop bode diagram of the current controller indicating the minimum stability of phase margin of about 112 degrees at a crossover frequency of 0.0387 kHz. The peak gain is 484 dB at the frequency of 1.59e-24 kHz. In the similar process, Fig.8(b) exhibits the open loop bode diagram of the current controller indicating the minimum stability of phase margin of about 112 degrees at a crossover frequency of 0.0387 kHz. The peak gain is 484 dB at the frequency of 1.59e-24 kHz.

Fig. 9 illustrates the performance of PFWC and CFWC when the motor is controlled to run at the flux-weakening region under the desired speed of 2300 rpm with an initial load reducing from 8.5 Nm to half at 2 s. Further, the simulation result of the PFWC algorithm with the standard PI controller structure (SPI3) also is presented in Fig. 9 to verify the effectiveness of the AWPI structure. As shown in Fig. 9(a), the PFWC algorithm is better than the CFWC algorithm in terms of the speed overshoot and the steady-state error. The PFWC algorithm with both controller structures has no steady-state error, while the average value of the steady-state error of the CFWC algorithm is 2.1% and decreasing to about 1% after load drop. Additionally, the speed overshoots at the motor starting and the load drop periods of the PFWC algorithm with an AWS are 3.5% and 6%, and the counterparts of these periods for the CFWC algorithm are 6.5% and 10.5%, respectively.

TABLE II

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rated line voltage</td>
<td>$v_N$</td>
<td>270</td>
<td>V</td>
</tr>
<tr>
<td>Rated phase current</td>
<td>$i_N$</td>
<td>6.8</td>
<td>A</td>
</tr>
<tr>
<td>Stator resistance</td>
<td>$R_s$</td>
<td>0.8</td>
<td>Ω</td>
</tr>
<tr>
<td>Stator inductance</td>
<td>$L_s$</td>
<td>5</td>
<td>mH</td>
</tr>
<tr>
<td>Permanent magnet</td>
<td>$\lambda_m$</td>
<td>0.35</td>
<td>Wb</td>
</tr>
<tr>
<td>Rated speed</td>
<td>$N_r$</td>
<td>2000</td>
<td>rpm</td>
</tr>
<tr>
<td>Rated power</td>
<td>$P_N$</td>
<td>3.0</td>
<td>kW</td>
</tr>
<tr>
<td>Number pole pairs</td>
<td>$n_p$</td>
<td>3</td>
<td></td>
</tr>
</tbody>
</table>

TABLE III

<table>
<thead>
<tr>
<th>Name</th>
<th>Symbol</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Speed controller</td>
<td>$K_{p_d}$</td>
<td>0.1</td>
</tr>
<tr>
<td>$d$-axis current controller</td>
<td>$K_{i_d}$</td>
<td>13.6</td>
</tr>
<tr>
<td>$q$-axis current controller</td>
<td>$K_{p_q}$</td>
<td>22.5</td>
</tr>
<tr>
<td>$q$-axis current controller</td>
<td>$K_{i_q}$</td>
<td>319.3</td>
</tr>
<tr>
<td>Flux weakening controller</td>
<td>$K_{i_{f-w}}$</td>
<td>14.9</td>
</tr>
<tr>
<td></td>
<td>$K_{i_{f-w}}$</td>
<td>614.7</td>
</tr>
</tbody>
</table>

The PWM inverter has a constant switching frequency of 5 kHz with a dc-bus voltage of 400 V. The PWM inverter has a constant switching frequency of 5 kHz with a dc-bus voltage of 400 V. Fig. 9 illustrates the performance of PFWC and CFWC when the motor is controlled to run at the flux-weakening region under the desired speed of 2300 rpm with an initial load reducing from 8.5 Nm to half at 2 s. Further, the simulation result of the PFWC algorithm with the standard PI controller structure (SPI3) also is presented in Fig. 9 to verify the effectiveness of the AWPI structure. As shown in Fig. 9(a), the PFWC algorithm is better than the CFWC algorithm in terms of the speed overshoot and the steady-state error. The PFWC algorithm with both controller structures has no steady-state error, while the average value of the steady-state error of the CFWC algorithm is 2.1% and decreasing to about 1% after load drop. Additionally, the speed overshoots at the motor starting and the load drop periods of the PFWC algorithm with an AWS are 3.5% and 6%, and the counterparts of these periods for the CFWC algorithm are 6.5% and 10.5%, respectively.

The PWM inverter has a constant switching frequency of 5 kHz with a dc-bus voltage of 400 V. Fig. 9 illustrates the performance of PFWC and CFWC when the motor is controlled to run at the flux-weakening region under the desired speed of 2300 rpm with an initial load reducing from 8.5 Nm to half at 2 s. Further, the simulation result of the PFWC algorithm with the standard PI controller structure (SPI3) also is presented in Fig. 9 to verify the effectiveness of the AWPI structure. As shown in Fig. 9(a), the PFWC algorithm is better than the CFWC algorithm in terms of the speed overshoot and the steady-state error. The PFWC algorithm with both controller structures has no steady-state error, while the average value of the steady-state error of the CFWC algorithm is 2.1% and decreasing to about 1% after load drop. Additionally, the speed overshoots at the motor starting and the load drop periods of the PFWC algorithm with an AWS are 3.5% and 6%, and the counterparts of these periods for the CFWC algorithm are 6.5% and 10.5%, respectively.
Also, Fig. 9(a) presents the difference in dynamic performance between PFWC-SPIS and PFWC-AWS that is summarized in reduction the settling time from 1.3 to 0.56 s, and in reducing the speed overshoot at the load drop period from 7% to 6%, respectively. The average $q$-axis currents of both PFWC and CFWC are decreased from about 5.64 to 2.9 A at 2 s under the reduction of the motor torque as presented in Fig. 9(b). Fig. 9(c) presents the difference of $d$-axis average currents that are -8.55 A for the PFWC with different PI structures and -6.5 A for the CFWC. Fig. 9(d) presents the unfiltered waveform of the voltage vector magnitude, which certainly proves that all control strategies involved in the flux-weakening region. The instantaneous magnitude of the voltage vector produces the maximum value. Furthermore, Fig. 9(d) defines the difference of the dc-bus voltage utilization under PFWC and CFWC strategies that are achieving average values of about 1 and 0.98, respectively. Meanwhile, the average value of the line-modulation ratio under PFWC and CFWC are about 0.98 and 0.97, respectively, as illustrated in Fig. 9(e). Additionally, the magnitudes of duty cycles shown in Fig. 9(f) have the average values of about 1 and 0.98, respectively, where the $D_{dq}$ is calculated for CFWC by

$$D_{dq} = \left(\frac{\sqrt{v_{dq}^2 + v_{q}^2}}{V_{dc}}\right).$$

Lastly, the overall system efficiencies of the PFWC and the CFWC strategies from the
dc-bus to mechanical output are 76.5% and 74.7% and then decreasing to about 45.3% and 44.85% after load drop, respectively.

Fig. 10 presents the dynamic simulation results of both flux weakening algorithms under the similar conditions used for Fig. 9, except for the motor parameters that are varying. These simulation results show what extent the algorithms depend on those parameters. The stator resistance is detuned from the nominal value to the value at the temperature of 122 °C. Thus, the stator resistance is changed from 0.8 to 1.12 Ω, which can be determined by

\[ R_s = \left( R_s \left( t_a + k_1 \right) / \left( t_b + k_1 \right) \right) \]

where \( R_s \) is the \( R_s \) measured at the temperature \( t_a = 20 \) °C, \( t_b \) is the temperature in °C to which the resistance is to be corrected, \( k_1 \) is about 234.5 for 100% conductivity copper, and \( R_s \) is the winding resistance in Ω corrected to the temperature \( t_b \). For the winding inductances, when the magnetic saturation occurs, the winding inductances would drop about 40% [26]. It can be concluded from Figs. 10(a) and (b) that the speed and the q-axis current traces of the PFWC algorithm have fewer oscillations at steady-state than that of the CFWC algorithm.

Fig. 9. Simulation results of PFWC and CFWC in case of motor torque reduction under the speed of 2300 rpm, where (a) motor speed, (b) q axis currents, (c) d-axis current, (d) magnitude of the voltage vector, (e) line modulation ratio, and (f) magnitude of the duty cycles.

Fig. 10. Simulation results of PFWC and CFWC in case of parameters variation with load reduction under the speed of 2300 rpm, where (a) motor speed, (b) d-q axes currents, (c) magnitude of the voltage vector, (d) line modulation ratio, and (e) magnitude of the duty cycles.
Comparing with the correctly tuned case in Fig. 9, the steady-state error value of the CFWC algorithm increases to about 3% and the counterpart of the PFWC algorithm is still less than 1%. Both strategies seek to minimize the speed error under the parameter variation. As a result, the $d$-axis average currents of the PFWC and CFWC algorithms lightly decrease to about -8.7 and -7.5 A leading to an increase in the average value of the magnitudes of the duty cycles to about 1.01 and 0.98, respectively, as shown in Figs. 10(b) and (e). Fig. 10(c) presents that the per-unit magnitude of the unfiltered voltage vector under the CFWC algorithm is increased slightly to the average value of about 0.986, and the counterpart under the PFWC algorithm is increased slightly to the average value of about 1.01. Furthermore, the averages of the line-modulation ratio value of the PFWC and CFWC algorithms are increased to about 0.99 and 0.98, respectively, as depicted in Fig. 10(d). Moreover, the overall system efficiencies of the PFWC and CFWC algorithms are 76.4% and 74.2% and then decreased to about 44.8% and 44.2% after load drop, respectively.

VI. EXPERIMENTAL RESULTS

This section proves the effectiveness of the proposed control algorithm considering the optimized parameters of AWPI controllers listed in Table III. Fig. 11 shows a photograph of the experimental test platform. This figure shows the test motor coupled with a 3-kW interior magnet PMSM with an encoder of 4096 pulses per cycle. For this reason, the closed-loop torque mode control realizes the interior magnet PMSM as a load using field-oriented control. Moreover, the algorithms are implemented in the TMS320F28335 DSP board with C programming codes. The inputs for the control board are the dc-bus voltage regulated as 150 V, the feedback signal of the encoder, and the measured phase currents. The sampling time of control loops is 100 $\mu$s. Tektronix oscilloscope with 1× passive voltage probe is used to measure signals. Measured signals have additional ripple due to the hardware noises. To verify the effectiveness of AWPI structure, Fig. 12 provides the dynamic performance under modified vector control, as shown in Fig. 3(c), for both structures based on the AWS and the SPIS. The reference speed is 500 rpm that is increased to the maximum limit of the rotational speed at 10 s without using the flux weakening control loop ($i_d^* = 0$), and the initial load torque is 7.5 Nm.

Fig. 12(a) shows the speed overshoot of SPIS with value 12%, while the speed overshoot of AWS is 4%. Meanwhile, the settling times are 0.76 and 0.15 s, respectively. Besides, the averages of maximum rotational speed achieving in constant torque region are 780.7 rpm. The averages currents of $d$-$q$ axes are 0 and 4.5 A, respectively, as shown in Fig. 12(b). Fig. 12(c) explains the utilizing of the dc-bus voltage, where the average line modulation ratio increases from 0.64 to 0.94. Meanwhile, Fig. 12(d) presents the voltage vectors under the constant torque region. Both structure cases increase average voltage vectors from 0.68 to 0.95 at 10 s. Fig. 12(e) presents the magnitude of the duty cycles. The error between $D_{dq}$ and $D_{dq, max}$ will be the input of the proposed duty cycles regulating
loop. Consequently, the AWPI regulator increases the negative of $d$-axis current to prevent the current controllers from the saturation.

Fig. 13 presents the limit of the maximum speed of PFWC and CFWC at the flux-weakening region with initial load torque of 7.5 Nm. In this case, the speed programmed in a ramp function reverses the direction at the time of 50 s to ensure the four-quadrant operation of the driving algorithm, which includes the transition between the constant torque and flux weakening regions. As shown in Fig. 13(a), the speed change of PFWC within the constant torque and flux-weakening fields is faster than that of CFWC in the reverse direction. Furthermore, the PFWC involves in a higher speed than the CFWC with the values of about 1175 and 1016 rpm, respectively. Fig. 13(e) presents that the voltage vectors under the flux-weakening region are laying on the boundary of the maximum voltage that the inverter can supply to the motor preventing the speed from breaking these limits under the operating conditions. The average voltage vector magnitude under PFWC and CFWC are 1 and 0.986, respectively. Both PFWC and CFWC increase average $q$-axis currents from -4.76 to 5 A at 50 s, as shown in Fig. 13(b). However, they produce different $d$-axis currents. As shown in this figure, the $d$-axis average current of PFWC is about -8.45 A. Similarly, the $d$-axis average current of CFWC is about -5.87 A. The reason is

![Figure 13](image1.png)

Fig. 13. Experimentally measured results of the reversing direction case, where (a) motor speed, (b) $d$-$q$ axes currents, (c) line modulation ratio, (d) magnitude of the duty cycles, and (e) magnitude of the voltage vector.

![Figure 14](image2.png)

Fig. 14. Experimentally measured results of the load torque reduction case, where (a) motor speed, (b) $d$-$q$ axes currents, (c) line modulation ratio, (d) magnitude of the duty cycles, and (e) magnitude of the voltage vector.
that both PFWC and CFWC have different average line-modulation ratios of 0.98 and 0.97, respectively, as presented in Fig. 13(c). Meanwhile, the average duty cycle magnitude given in Fig. 13(d) under PFWC and CFWC are 1 and 0.95, respectively. The control in the flux-weakening region under the unrated torque decreases the overall efficiencies of PFWC and CFWC to about 72.9% and 72.2%, respectively.

Fig. 14 shows the dynamic performance of PFWC and CFWC running the SMPMSM at the flux-weakening region with a reference speed of 2300 rpm and a load torque variation from 3.5 to 0.5 Nm at 50 s. The dc-bus voltage is increased to 400 V to break the speed limit of the previous case shown in Fig. 13. While suddenly reducing the load torque, the PFWC has a small transient period to keep the reference rotational speed at the flux-weakening region better than that of CFWC as presented in Fig. 14(a). Moreover, the steady-state error of PFWC is better than that of CFWC with the value of about 1% and 3.2% for PFWC and CFWC, respectively. High oscillation wave attaches the average of $q$-axis current under CFWC as shown in Fig. 14(b). Both PFWC and CFWC increase the average $q$-axis current from 2.22 to 0.32 A at the load torque reduction time. Additionally, the average value of $d$-axis current under PFWC is about -7.6 A, and that value under CFWC reaches -5.9 A. Besides, the average values of the line-modulation ratio under both PFWC and CFWC are about 0.98 and 0.97, respectively, as provided in Fig. 14(c). Meanwhile, those of the magnitude of duty cycles, as shown in Fig. 14(d), are about 1 and 0.98, respectively. The overall efficiencies of the PFWC and the CFWC algorithms are 71.8% and 71.5%, respectively. The appearance of the voltage vector at the boundary of the maximum voltage limit confirms that the motor speed has been involved in the flux-weakening region as presented in Fig. 14(e). The average voltage vector magnitude under PFWC and CFWC are 1 and 0.98, respectively.

VII. CONCLUSION

This paper presents parameter optimization of the improved vector control scheme to control an SMPMSM in the flux weakening region. The anti-windup structure which improves the dynamic performance of the vector control strategy employs the full saturated output of the PI controllers to defeat the overshoot effect of saturation. The novelty of the parameter tuning method relies on adopting the equilibrium point term of Taylor series as the proposed objective function. Thus, the proposed adaptive velocity PSO algorithm optimizes the objective function looking for the optimal parameter to achieve the minimum error for the controllers. Meanwhile, the control strategy utilizes the compensated duty cycles to determine the outbreak of the field weakening point.

The theoretical study with the simulation and the experiment results of the PFWC demonstrate parameters robustness that assures the success of the proposed tuning method. Further, the results confirm the success of the AWPI structure in the reduction of the overshoot impact during the transient process. Besides, this control strategy decides the flux weakening point, and then the negative $d$-axis current is injected which results in an additional voltage to control the motor in field decreasing region. Simulation results verify that the proposed flux weakening method has little dependence on the machine parameters. From the experimental results, the proposed algorithm significantly increases the maximum speed limit of constant torque region, which demonstrates that the dc-link voltage utilization for the proposed controller is better than that for CFWC. Meanwhile, the proposed flux weakening control loop introduces a fast and stable transfer within a field decreasing region.

REFERENCES

IEEE Transactions on Power Electronics


Wei Xu (M’09-SM’13) received the double B.E. and M.E. degrees from Tianjin University, Tianjin, China, in 2002 and 2005, and the Ph.D. from the Institute of Electrical Engineering, Chinese Academy of Sciences, in 2008, respectively, all in electrical engineering. From 2008 to 2012, he held several academic positions in both Australian and Japanese universities and companies. Since 2013, he has been full professor with the State Key Laboratory of Advanced Electromagnetic Engineering and Technology, Huazhong University of Science and Technology, China. His research topics mainly cover design and control of linear/rotary machines. He is Fellow of the Institute of Engineering and Technology (IET). He has served as Associate Editor for several Journals, such as IEEE Transactions on Industrial Electronics, IEEE Journal of Emerging and Selected Topics in Power Electronics, IEEE Transactions on Vehicular Technology, etc.

Moustafa Magdi Ismail received the B.Sc. and M.Sc. degree in the school of Electrical Engineering, Minia University, Minia, Egypt, in 2011 and 2016, respectively. He was appointed an Assistant Lecturer in the School of Electrical Engineering, Minia University from Oct. 2011 to Sept. 2017. From Sept. 2017, he has been pursuing the Ph.D. degree at the State Key Laboratory of Advanced Electromagnetic Engineering and Technology, School of Electrical and Electronic Engineering, Huazhong University of Science and Technology, Wuhan, China. His current research interests include advanced control of electrical drives, power converter systems, smart grid, and optimization algorithms.