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Abstract

Enhanced flexoelectricity in perovskite ceramics and single crystals has been reported before. In this letter, 3-3 ceramic-ceramic $\text{Ba}_{0.6}\text{Sr}_{0.4}\text{TiO}_3/\text{Ni}_{0.8}\text{Zn}_{0.2}\text{Fe}_2\text{O}_4$ composite with a colossal permittivity was employed in the conventional pure bending experiment in order to examine the transverse flexoelectric response. The measured flexoelectric coefficient at 30 Hz is $128 \mu\text{C}/\text{m}$ and varies to $16 \mu\text{C}/\text{m}$ with the frequency increasing from 30 Hz to 120 Hz, mainly due to the inverse correlation between the permittivity and the frequency. This result reveals the permittivity dependence of flexoelectric coefficient in the frequency dispersion materials, suggesting that the giant permittivity composites can be good flexoelectric materials.

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Converse flexoelectric coefficient f_{1212} in bulk $\text{Ba}_{0.67}\text{Sr}_{0.33}\text{TiO}_3$

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The converse flexoelectric effect, referred as the electric field gradient induced strain, widely exists in dielectric materials, but its experimental studies have been reported by few research groups so far. In this Letter, we report our studies on the converse flexoelectric behavior of $(\text{Ba}_{0.67}\text{Sr}_{0.33})\text{TiO}_3$ ceramics and present the measured value of its flexoelectric coefficient f_{1212} . In the experiments, the electric field gradient was generated by applying an electric field across the two lateral sides of trapezoid $(\text{Ba}_{0.67}\text{Sr}_{0.33})\text{TiO}_3$ samples. The shear displacement was measured using a laser vibrometer. The converse flexoelectric coefficient f_{1212} was found to be $124 \pm 14 \mu\text{C}/\text{m}$ at room temperature. This result was in good agreement with the theoretical prediction of the flexoelectricity of the $(\text{Ba}, \text{Sr})\text{TiO}_3$ ceramics. © 2014 AIP Publishing LLC.

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Flexoelectricity, denoting the electric polarization induced by mechanical strain gradient or mechanical strain induced by electric field gradient, has drawn research interests in recent years.^{1–3} This phenomenon is generally expressed in tensor form⁴

$$\begin{aligned} \text{Direct : } P_l &= \mu_{ijkl} \frac{\partial S_{ij}}{\partial x_k}, & P_l &= f_{ijkl} \frac{\partial T_{ij}}{\partial x_k} \\ \text{Converse : } T_{ij} &= \mu_{ijkl} \frac{\partial E_k}{\partial x_l}, & S_{ij} &= f_{ijkl} \frac{\partial E_k}{\partial x_l}, \end{aligned} \quad (1)$$

where P_l is the induced polarization, μ_{ijkl} is the flexoelectric coefficient, a fourth-rank tensor, S_{ij} is the strain, and x_k or x_l is the axis; T_{ij} is the induced stress, f_{ijkl} is the converse flexoelectric coefficient associated with strain, and E_k is the electric field.

The first phenomenological model of flexoelectricity in solid dielectrics was proposed by Kogan.⁵ However, in Kogan's original paper, he used "piezoelectric effect" to describe this unique inhomogeneous electro-mechanical coupling effect. By comparing it with an analogical phenomenon observed in liquid crystals, Indenbom suggested later that the term, "flexoelectric effect" should be adopted to describe this effect.⁶ It is one of the fundamental properties of crystalline dielectric materials and usually considered as a weak pseudo piezoelectric effect.⁷ In principle, flexoelectric effect is present universally in all 32 point groups and seven Curie groups of crystal structures without any symmetry constraints.^{8,9} Consequently, non-piezoelectric materials, such as cubic materials and isotropic materials, could still generate electric polarization under inhomogeneous mechanical field or yield mechanical strain under inhomogeneous electric field, through the direct and converse flexoelectric effect,

respectively. This unique property greatly enhances the potential of flexoelectric material as new and attractive sensing/actuating solid materials.¹⁰ However, theoretical value of flexoelectric constant is estimated to be in the order of e/a (10^{-10} C/m), where e is the electronic charge and a is the crystal parameter.¹¹ For most bulk materials, compared with piezoelectric constant, flexoelectric constant is so small that the related phenomena are always unperceivable in macro scale.

High level of direct flexoelectric effect was found in high permittivity perovskites such as Barium Strontium Titanate (BST),¹² Barium Stannate Titanate (BTS),¹³ Barium Titanate (BT),¹⁴ Lead Magnesium Niobate (PMN),¹⁵ and Lead Zirconate Titanate (PZT).¹⁶ Intriguingly, the enhancement is four to five order larger than that of theoretical predictions. Moreover, PZT thin film¹⁷ and soft polymer polyvinylidene fluoride (PVDF)¹⁸ were also reported to have a large pure polarization when being bended. Recently, it was also reported that the scaling effect of direct flexoelectricity has great potential to be alternative of piezoelectricity for micro/nano devices.^{19–22}

Although significant advances have been made in the research of direct flexoelectricity, the investigation on converse effect is rather limited. As proposed by Fu and Cross,²³ one of the greatest challenges for converse flexoelectric measurement is the unavoidable influence from the simultaneous electrostriction effect. Conventionally, the influence of piezoelectricity can be readily excluded when non-piezoelectric material is selected for flexoelectric testing. However, both flexoelectric and electrostrictive effect can exist in all crystals without the symmetry limit.^{24,25} In one of our previous work, we demonstrated that the symmetry of flexoelectric coefficient is lower than electrostrictive constant M_{ijkl} .⁹ This difference exists in low symmetry crystals but disappears in high symmetry crystals. For example, in a triclinic crystal, the number of non-zero independent components of

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f_{ijkl} is 54 while 36 for M_{ijkl} . But for cubic or isotropic crystals, both μ_{ijkl} and M_{ijkl} have the same non-zero components expressed as $f_{1111}, f_{1122}, f_{1212}$ and $M_{1111}, M_{1122}, M_{1212}$.

For most non-piezoelectric materials, M_{ijkl} always plays a leading role for the contribution of strain. In terms of mathematics, a non-zero $\partial E_i/\partial x_j$ must be accompanied with E_i^2 , thus f_{1111} component coexists with M_{1111} effect. In Fu's measurement,²³ the flexoelectric strain is more than two orders smaller than electrostrictive strain, rendering it difficult to separate f_{1111} from M_{1111} . However, f_{1212} can exist alone when $\partial E_1/\partial x_3 \neq 0, E_1 E_3 = 0$ or can be a dominant contributor to a shear strain when $\partial E_1/\partial x_3 \neq 0, E_1 E_3 \rightarrow 0$. In other words, a unidirectional electric field distribution is of highly significance. Here, we underline the word *distribution*, which stands for the orientation variation in a board range of material. In this study, we experimentally verify the pure converse flexoelectric effect by applying a directional electric field E_1 , accompanied with a small E_3 component, as well as a large gradient $\partial E_1/\partial x_3$ so that the electrostrictive strain can be minimized in generating shear strain S_{13} .

The configuration to generate a directional electric field distribution is schematically shown in Fig. 1(a). Essentially, for a parallel plate capacitor, the electric field, as a continuous function, is perpendicular to the equipotential line and is reversely proportional to the effective distance between the two electrode plates. For the lateral plates of a truncated pyramid, considered as an unparallelled plate capacitor, the electric field E_1 is inhomogeneously distributed along the height direction x_3 due to the distance variation along direction x_1 . The measurement setup was laid down on a float optical table (Newport, ATS, Irvine, CA) to eliminate the vibrational noise. The AC voltage was generated by a power amplifier (Trek, 2220, Lockport, NY) under the excitation from a function generator (Tectronix, AFG3101, Lake Mary, FL). As suggested in our previous work,⁹ the symmetry of the cubic materials permits only shear strain S_{13} , which is generated

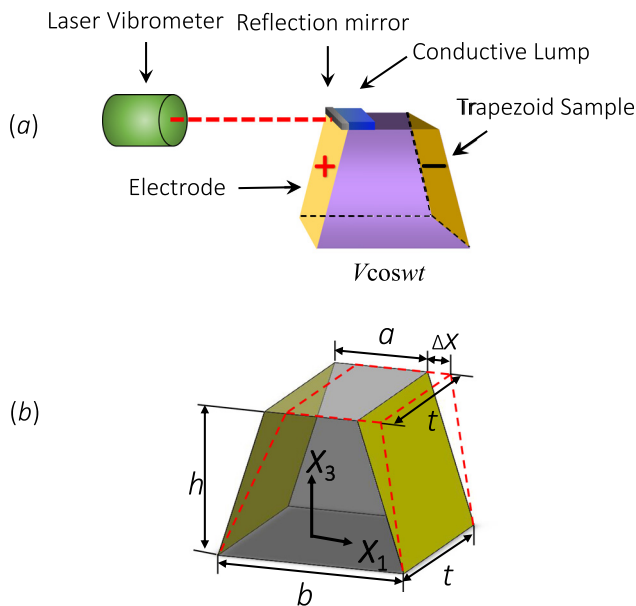


FIG. 1. (a) Diagram of sample assembly for converse flexoelectric measurement of the shear strain along x_1 direction generated by the electric field gradient along x_3 direction. (b) Schematic deformation of the trapezoid sample in the lateral mode.

by $\partial E_1/\partial x_3$ due to the coupling of f_{1212} . To measure this shear strain, the bottom surface of the sample was clamped on the table and a mirror was attached to the top surface of the sample. The deformation along x_1 direction was measured using a high resolution (<10 pm) laser vibrometer (Polytec, OFV-5000, Irvine, CA) and a lock-in amplifier (Stanford Research System, SR830, Sunnyvale, CA). Based on the measured shear deformation as illustrated in Fig. 1(b), the pure shear strain can be calculated as

$$S_5 = 2S_{13} = \frac{\Delta x}{h}, \quad (2)$$

where Δx is the detected deformation and h is the altitude of the sample.

The theoretical analysis for the electric field distribution in this non-parallel plate capacitor is shown in Fig. 2(a). When a voltage V is applied across the sample, electric charge Q will be accumulated on two surfaces. In nature, the electric field (E) direction is dependent on the equipotential line ϕ . For the presented situation, both two side surfaces of the sample and the geometric center line are equipotential. The electric field would radiate along the tangential lines of the arc formed by two sides of the capacitor. It can be written as

$$E_r = \frac{V}{r\theta}, \quad (3)$$

where r is the radius of the scallop and θ is the angle of the scallop. Thus, the electric field is not homogeneous in light of the space curvature of the electric field line. In this case, an electric field gradient along the longitudinal direction (x_3) is generated, as shown in Fig. 2(b). In addition, the angle between the electric field and x_1 axis changes from $-\theta/2$ to $\theta/2$ across the whole region due to the geometric relationship as illustrated in Fig. 2(c). Hence, the average electric field component for an arc with the angle of θ at the radius of r in the transverse direction \bar{E}_1 can be obtained as

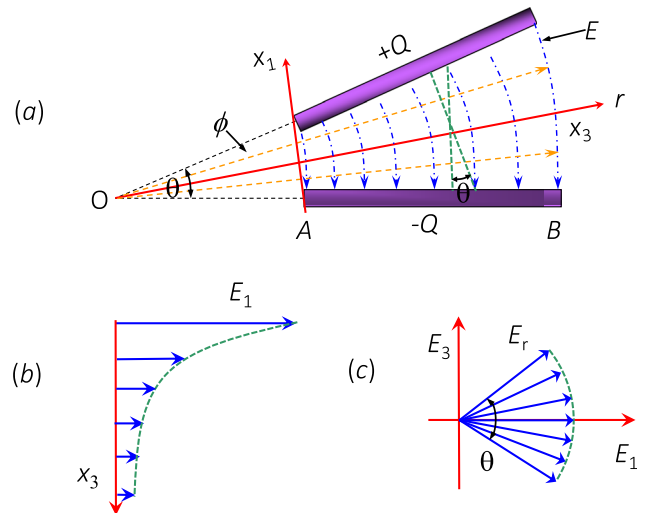


FIG. 2. Schematic view of a trapezoid sample with the voltage applied from side to side, (a) electric field line and equipotential distribution. O is the intersection point between the two extension lines of the slope side of the sample; (b) electric field gradient distribution; (c) electric field direction variation in arbitrary pitch arc r position.

$$\int_{-\theta/2}^{\theta/2} E_1 d\varphi = \int_{-\theta/2}^{\theta/2} E_r \cos \varphi d\varphi = \frac{\sin \theta/2}{\theta/2} E_r, \quad (4)$$

where φ is the arbitrary vertex angle of the arc. In order to simplify the calculation, the trapezoid sample was prepared with smooth side surfaces and rectangle top and bottom surfaces so that the average electric field \bar{E}_1 along the thickness gradient is

$$\frac{\partial \bar{E}_1}{\partial x_3} = \int_a^b \frac{\partial E_1}{\partial x_3} dx = \frac{\sin^2 \theta/2}{h(\theta/2)} \left(\frac{V}{b} - \frac{V}{a} \right), \quad (5)$$

where a and b are the side length of the top and bottom surface of the sample (Fig. 1(b)), respectively.

Equation (5) can be further simplified as Eq. (6) when θ is equal or lower than $\pi/4$ (the coefficient equals to 0.95)

$$\frac{\partial \bar{E}_1}{\partial x_3} = \frac{1}{h} \left(\frac{V}{b} - \frac{V}{a} \right). \quad (6)$$

This simplified calculation was verified using the COMSOL Multiphysics (Fig. 3). A two dimensional trapezoid structure was considered in the simulation. The designated bottom and top lines have the length of 2.5 mm and 1.5 mm, respectively. The height of the structure is 1 mm. Material was chosen as the BST. Ground boundary condition was assigned to one of the two tilted side, while a DC voltage of 200 V was applied to the other tilted side. Electric field distribution along the horizontal direction (E_1) can then be obtained. Further, numerical manipulation yields the electric field gradient along the vertical orientation ($\partial E_1/\partial x_3$). The average magnitude was estimated to be 4.6×10^7 V/m², matching well with the theoretical calculation (5.3×10^7 V/m²) using Eq. (6). There exist small singularity regions at the vertexes exhibiting high gradient concentrations. However, they would not make significant contribution to the averaged gradient value due to their small areas.

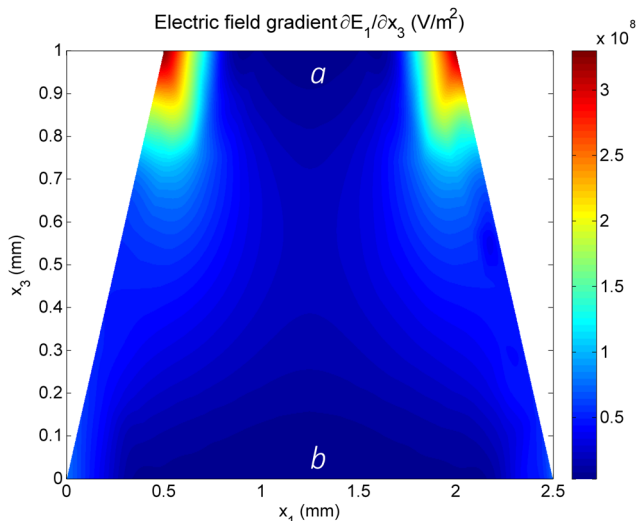


FIG. 3. Finite element simulation with COMSOL; areas with different color represent the magnitude of the calculated electric field gradient distribution within the trapezoid.

Moreover, the electric field component E_3 will, in principle, exist along with E_1 according to the above analysis. Nevertheless, the product of $E_1 \cdot E_3$ is zero as interpreted in Eq. (7), so that it may not yield a shear strain coupled by electrostrictive constant M_{1212} .

$$\int_{-\theta/2}^{\theta/2} E_1 E_3 d\varphi = \int_{-\theta/2}^{\theta/2} E_r \cos \varphi E_r \sin \varphi d\varphi = 0. \quad (7)$$

This analysis theoretically ensures the feasibility of the above method for distinguishing flexoelectricity from electrostriction in converse flexoelectricity measurements.

Up to now, the maximum direct flexoelectric coefficient ($120 \mu\text{C}/\text{m}$) was observed in $(\text{Ba}_{0.67}\text{Sr}_{0.33})\text{TiO}_3$ (BST) ceramic at its paraelectric state (at temperature of 23°C , which is 2°C above its T_C).¹² The reason of this extraordinary enhancement is not clear yet. A large direct flexoelectric coefficient generally corresponds to a large converse coefficient.¹ The aim of the present experiment is to identify the pure converse flexoelectric properties in the unpolarized BST ceramics. Three BST ceramic samples were prepared in specific shapes by a dicing saw (Disco, DAD320, Santa Clara, CA) and the dimensions are given in Table I. It is worthy to note that all three samples, including one sample with all rectangular surfaces (BST-I) and two samples with trapezoid shapes (BST-II and BST-III), were cut from the same raw material along one direction in order to exclude the orientation inhomogeneous of the material. Moreover, only the side surface of the sample is covered by electrode so that the influences from other directions do not exist. Electrode surfaces of all samples were coated with 200 nm thickness of nickel using a plating process (Transene, RTM Process, Danvers, MA). The sample BST-I was prepared as a reference where the electric field gradient is 0.

The measured face displacement of samples BST-I, BST-II, and BST-III as a function of voltages ranged from 200 V to 700 V at 10 Hz are shown in Figs. 4(a)–4(c), respectively. A visible 20 Hz response was found in all of the samples, displaying with a quadratic regulation in plot. In principle, in this experiment, irrespective the symmetry of the sample, all the possible contributions to shear strain S_{13} can be expressed as

$$\begin{aligned} S_{13} &= d_{113} E_1 \cos \omega t + f_{1212} \frac{\partial E_1}{\partial x_3} \cos \omega t \\ &\quad + M_{1212} E_1 E_2 \cos \omega t \cos \omega t \\ &= S_{13}(P) + S_{13}(F) + S_{13}(M), \end{aligned} \quad (8)$$

where d_{113} is the shear piezoelectric constant and ω is the driven frequency. Hereafter, the piezoelectric, flexoelectric, and electrostriction contribution is labeled as P , F , and M , respectively. As interpreted in Eq. (8), the origin of 2ω -signal is only associated with M , while the response with frequency of ω is yielded by P and F . For the sample shown in Fig. 4(a), M_{1212} contribution does not exist due to absence of E_3 . However, the clamped condition of bottom cannot restrict the oscillation of the top of the sample. The electric field in transverse direction would yield the direct displacement reflected in the mirror due to the coupling of the M_{1111} , thus to cause

TABLE I. Dimension of BST samples.

Sample	Cross section shape ($x_1 - x_3$ plane)	Vertex angle θ (degree)	Top length $x_1 a$ (mm)	Bottom length $x_1 b$ (mm)	Height $x_3 h$ (mm)	Thickness $x_2 t$ (mm)
BST I	Rectangle	90	3.64	3.64	3.03	0.67
BST II	Trapezoid	62	1.83	5.05	3.03	0.67
BST III	Trapezoid	46	1.83	7.55	3.03	0.67

2ω -response, as seen in the measured second harmonic results. In addition, a non-zero first harmonic response of the BST-I sample implies the existence of piezoelectric effect in BST, which contradicts the fact that the symmetry of BST material in paraelectric phase permits no macro piezoelectricity. Nevertheless, when the temperature is very close to the Curie temperature, ferroelectricity may exist due to local nano domains,²⁶ which may be one possible reason for the existence of piezoelectric responses in BST samples.

On the other side, in Fu's experiment,²³ the driving frequency of the power amplifier was 400 Hz. It is possible that the output waveform of the power amplifier was distorted, and hence, was not a standard cosine function at such a high driving frequency. In this case, the first harmonic signal is unavoidably influenced by the coupling of electrostrictive effect. As interpreted by Fu *et al.*, the small DC voltage shifts \tilde{n} generated by the power amplifier, resulting in a first harmonic response $2M_{ijkl}\tilde{n}V_1\cos\omega t$. In our experiment, the driven frequency was only 10 Hz and there was no detected 10 Hz background and electromagnetic noise, as shown in Figs. S1 and S2, respectively. Moreover, the driving outputs of the power amplifier were cosine waveforms as demonstrated in supplementary material Figs. S3, S4, and S5, so that M is proportional to the square of the electric field and would not contribute to the first harmonic response.²⁹ In other words, the first

harmonic value $\Delta x(V)$, in principle, does not encompass the influence from M and thus, can be used to calculate the contribution from P and F .

For rectangular sample BST-I, $\Delta x(V)$ is only derived from the piezoelectric displacement contribution P

$$\Delta x(V) = 2 \int d_{113} E_1(z) dz = \frac{2d_{113}h}{W} V, \quad (9)$$

where W is the width and z is the arbitrary position in the height direction.

As for the trapezoid samples II and III, $\Delta x(V)$ is expressed as

$$\begin{aligned} \Delta x(V) &= 2 \int (d_{113} E_1(z) + f_{1212} \frac{\partial E_1(z)}{\partial z}) dz \\ &= 2 \int_0^h d_{113} \frac{V}{a + 2(h-z)\cot\theta} dz + 2 \int_0^h f_{1212} \frac{\partial E_1}{\partial z} dz, \end{aligned} \quad (10)$$

where

$$\int_0^h d_{113} \frac{V}{a + 2(h-z)\cot\theta} dz = \frac{\tan\theta}{2} d_{113} \ln \frac{b}{a} V, \quad (11)$$

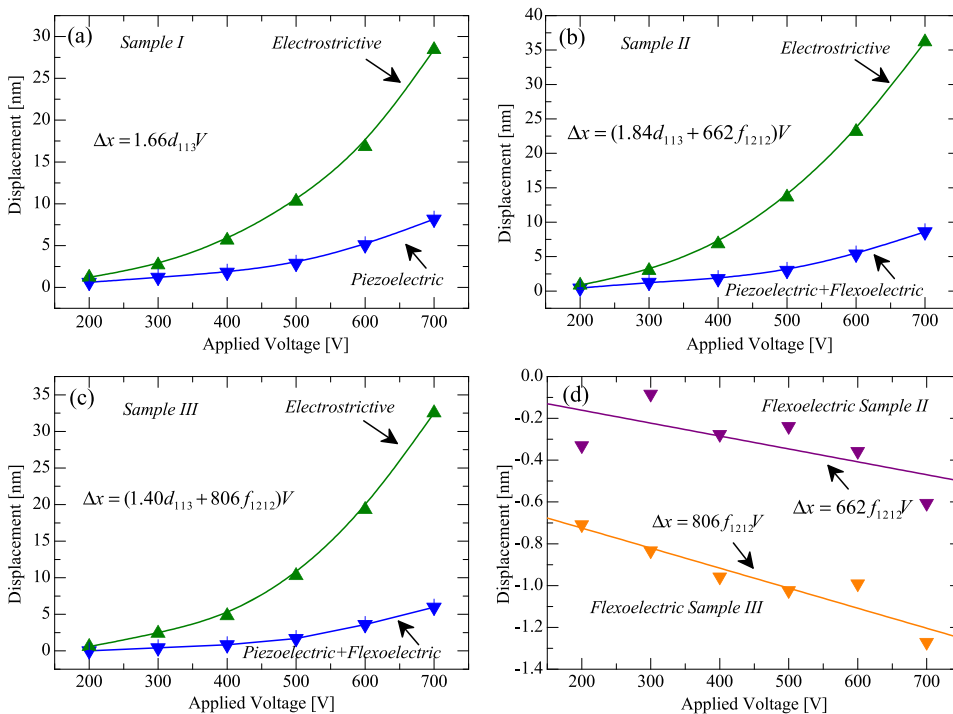


FIG. 4. Face displacement measured using a laser vibrometer as a function of voltage in room temperature for BST samples: (a) rectangle; (b) trapezoid 62°; and (c) trapezoid 46°. The green points are the second harmonic displacement associated with the electrostrictive effect. The blue points stand for the displacement associated with the piezoelectric and flexoelectric effect. The solid line is a guide to the eye. (d) Pure converse flexoelectric coefficient f_{1212} contribution extracted from the displacement subtraction in BST-II and BST-III as a function of voltage, respectively. The solid lines are the fitting slope of face displacement vs. voltage induced by net converse flexoelectric effect.

$$\int_0^h f_{1212} \frac{\partial E_1}{\partial z} dz = f_{1212} E_1 \Big|_0^h = f_{1212} \frac{\sin \theta/2}{\theta/2} V \left(\frac{1}{a} - \frac{1}{b} \right). \quad (12)$$

It is noticed that P is proportional with the angle and the bottom/top dimension ratio while F is reciprocal proportional with the dimension. This calculation suggests that F likely plays a dominant role when scaling down the dimension. Thus, we can calculate the P and F proportions in each sample with the relevant sample parameters given in Table I. The displacement information including first harmonic under different voltage direction and second harmonic of samples II and III are represented in Figs. 4(b) and 4(c). The contributions from P and F are given in the legends. We mention that all types of samples were prepared with a counterpart and each sample was tested for three times under the same AC voltage. The repeatability of the displacement, measured by the laser vibrometer, is observed well due to the minimization of vibrational noise by a floating optical table and the absence of mechanical impact from electric equipment (supplementary material Table SI).

Based on the above measurement results, pure F in BST-II and BST-III ceramics can be extracted by subtracting the associated piezoelectric displacement contribution (Fig. 4(d)). This calculation is based on an assumption that all the material constants in Eq. (8) are the same for all three samples. The identical sample preparation process ensures the homogeneity of the sample. Linear fitting of the F induced displacement yields the converse flexoelectric coefficient f_{1212} to be $9.3 \times 10^{-16} \text{ m}^2/\text{V}$ and $1.18 \times 10^{-15} \text{ m}^2/\text{V}$ for sample II and sample III, respectively. The less common used unit m^2/V can be converted to the nominal unit C/m by removing the factor of elastic constant. Generally, the elastic compliance constant s_{1212} of BST ceramics is around $8.5 \times 10^{-12} \text{ m}^2/\text{N}$,²⁷ by which the stress related flexoelectric constant μ_{1212} is estimated to be $110 \mu\text{C}/\text{m}$ (sample II) and $138 \mu\text{C}/\text{m}$ (sample III). We note that the minus slope of the high linearity line stands for the deformation direction induced by electric field gradient, which is different from the piezoelectric deformation direction for this material.

This converse flexoelectric coefficient is similar to the direct result μ_{1111} ($120 \mu\text{C}/\text{m}$) observed in the same materials.²⁸ As demonstrated in previous work, the relationship among the non-zero dependent components of the flexoelectric coefficients in isotropic crystals is expressed as $\mu_{1212} = 1/2(\mu_{1111} - \mu_{1122})$.⁹ In this case, the value of the μ_{1212} is half of the subtraction between μ_{1111} and μ_{1122} due to the high symmetry of the materials. In rigid ceramic materials, generally, stretch along one dimension is accompanied with compression in another two dimensions. Therefore, the sign of μ_{1122} should be opposite to that of μ_{1111} , just like the sign of elastic coefficient s_{11} is opposite to that of s_{12} and the sign of d_{33} is opposite to that of d_{31} . Based on above analysis, the theoretical prediction of μ_{1212} in the BST is estimated to be $110 \mu\text{C}/\text{m}$, which is comparable with the direct μ_{1111} ($120 \mu\text{C}/\text{m}$)²⁶ and μ_{1122} ($100 \mu\text{C}/\text{m}$).¹² Our experiment first observed the shear flexoelectric data being consistent with the theoretical prediction.

In conclusion, converse flexoelectric effect of BST was investigated by generating a unidirectional electric field distribution along height direction of trapezoid samples. The present study clearly demonstrated the linear relationship between the electric field gradient and shear strain. The converse flexoelectric coefficient μ_{1212} is estimated to be $124 \pm 14 \mu\text{C}/\text{m}$, being in good agreement with the theoretical prediction. This result could benefit the development of electromechanical devices based on the flexoelectric effect. For a properly designed trapezoid sample, a small electric field can generate a large electric field gradient so that a visible shear deformation may be dominated by converse flexoelectric effect rather than the piezoelectric effect, especially, when the sample dimension scales down to the micro/nano level.

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