Gallium-Doped Li7La3Zr2O12 Garnet-Type Electrolytes with High Lithium-Ion Conductivity

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Abstract
Owing to their high conductivity, crystalline Li7−3xGa3xLa3Zr2O12 garnets are promising electrolytes for all-solid-state lithium-ion batteries. Herein, the influence of Ga doping on the phase, lithium-ion distribution, and conductivity of Li7−3xGa3xLa3Zr2O12 garnets is investigated, with the determined concentration and mobility of lithium ions shedding light on the origin of the high conductivity of Li7−3xGa3xLa3Zr2O12. When the Ga concentration exceeds 0.20 Ga per formula unit, the garnet-type material is found to assume a cubic structure, but lower Ga concentrations result in the coexistence of cubic and tetragonal phases. Most lithium within Li7−3xGa3xLa3Zr2O12 is found to reside at the octahedral 96h site, away from the central octahedral 48g site, while the remaining lithium resides at the tetrahedral 24d site. Such kind of lithium distribution leads to high lithium-ion mobility, which is the origin of the high conductivity; the highest lithium-ion conductivity of 1.46 mS/cm at 25 °C is found to be achieved for Li7−3xGa3xLa3Zr2O12 at x = 0.25. Additionally, there are two lithium-ion migration pathways in the Li7−3xGa3xLa3Zr2O12 garnets: 96h-96h and 24d-96h-24d, but the lithium ions transporting through the 96h-96h pathway determine the overall conductivity.

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Gallium-doped Li$_7$La$_3$Zr$_2$O$_{12}$ garnet-type electrolytes with high lithium-ion conductivity

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Abstract

Owing to their high conductivity, crystalline Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) garnets are promising electrolytes for all-solid-state lithium-ion batteries. Herein, the influence of Ga doping on the phase, lithium-ion distribution, and conductivity of Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) garnets is investigated, with the determined concentration and mobility of lithium ions shedding light on the origin of the high conductivity of Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\). When the Ga concentration exceeds 0.20 Ga per formula unit, the garnet-type material is found to assume a cubic structure, but lower Ga concentrations result in the coexistence of cubic and tetragonal phases. Most lithium within Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) is found to reside at the octahedral 96\(_h\) site, away from the central octahedral 48\(_g\) site, while the remaining lithium resides at the tetrahedral 24\(_d\) site. Such kind of lithium distribution leads to high lithium-ion mobility, which is the origin of the high conductivity; the highest lithium-ion conductivity of 1.46 mS/cm at 25 °C is found to be achieved for Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) at \(x = 0.25\). Additionally, there are two lithium-ion migration pathways in the Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) garnets: 96\(_h\)-96\(_h\) and 24\(_d\)-96\(_h\)-24\(_d\), but the lithium ions transporting through the 96\(_h\)-96\(_h\) pathway determine the overall conductivity.

**Keywords:** Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) garnet, lithium ion, lithium vacancy, ionic conductivity, mobility
1. Introduction

Lithium ion batteries are one of the most promising energy storing devices, offering high volumetric and gravimetric energy density compared with other battery technologies \(^1\). However, the flammability of organic liquid electrolytes results in notorious safety issues that hamper their full utilization in electric vehicles and stationary energy storage systems \(^1, 2\). Solid electrolytes are advantageous to conventional electrolytes in solving such safety issues. Additionally, their excellent stability potentially enables metallic Li to be used as a negative electrode, which, in combination with a high-voltage positive electrode, could provide high energy density and long cycle life. Consequently, all-solid-state lithium-ion batteries based on solid electrolytes are attracting increasing attention in battery research \(^3\text{-}6\). In some cases, in which power sources are to be operated under extreme environmental conditions, such as at high temperature and pressure in space, in defense applications and oil and gas exploration, all-solid-state lithium-ion batteries are clearly the best choice \(^7\).

Amongst the oxide solid electrolytes, Li\(_7\)La\(_3\)Zr\(_2\)O\(_{12}\) (LLZO) garnets are regarded as ideal candidates for lithium ion batteries \(^5, 8\text{-}10\). LLZO was first synthesized and characterized by Murugan \textit{et al.} \(^11\), although it was only recently that Geiger \textit{et al.} showed that LLZO is crystallized with both cubic and tetragonal symmetry, with the cubic phase exhibiting a lithium-ion conductivity two orders of magnitude higher than that for the tetragonal phase \(^12\). Li\(_7\)La\(_3\)Zr\(_2\)O\(_{12}\) is formed by a three-dimensional La\(_3\)Zr\(_2\)O\(_{12}\)-type framework structure consisting of 8-coordinate La\(^{3+}\) and 6-coordinate Zr\(^{4+}\), where two tetrahedral sites are bridged by a single octahedron via face-sharing,
constructing a migration pathway for lithium ions. The lithium ion distribution is the key factor in determining the modification of LLZO \(^{13}\). Tetragonal LLZO contains a completely ordered distribution of lithium ions and crystallizes in the space group \(I4_1/acd\). Cubic LLZO crystallizes in the space-group \(Ia\bar{3}d\), and exhibits a disordered lithium ion distribution and vacancies caused by lithium deficiency. Cation doping increases the number of vacancies and results in a disordered Li sublattice, where all Li sites are partially occupied in the LLZO structure. \(\text{Ta}^{5+}\), \(\text{Nb}^{5+}\), \(\text{Te}^{6+}\), and \(\text{W}^{6+}\) \(^{17}\) that substitute on the \(\text{Zr}^{4+}\) site, as well as \(\text{Al}^{3+}\) \(^{11}\) and \(\text{Ga}^{3+}\) \(^{18-26}\) that substitute in the Li sublattice, have been employed to stabilize the cubic phase.

The lithium-ion conductivity (\(\sigma\)) of LLZO can be expressed by the following equation:

\[
\sigma = e \cdot n_c \cdot \mu
\]

in which \(e\) is the elementary charge, \(n_c\) the concentration of mobile Li ions, and \(\mu\) the Li mobility. Therefore, the lithium-ion conductivity of LLZO is determined by the concentration and mobility of mobile lithium ions, both of which can be tuned by doping.

In the \(\text{Li}_{7.3}\text{La}_{3}\text{Zr}_{2.3}\text{Ta}_0\text{O}_{12}\) system, a maximum value of lithium-ion conductivity was theoretically demonstrated to be \(~ 6.4 \text{ Li per formula unit}\) \(^{13, 27}\). Not all lithium ions can contribute to conduction simultaneously, because only 2.6 vacancies per formula are available in \(\text{Li}_{6.4}\text{La}_{3}\text{Zr}_{1.4}\text{Ta}_{0.6}\text{O}_{12}\). Ahmad estimated that the concentration of charge carriers in LLZO is \(~ 12.3\%\) \(^{28}\), which is close to that found for W-doped LLZO \(^{29}\). The majority of lithium ions are trapped and the concentration of vacancies...
is higher than that of the mobile lithium ions, it is therefore possible to improve the lithium-ion conductivity of LLZO by activating lithium ions to participate in conduction. Additionally, enlarging the size of the lithium-ion migration pathway can increase the mobility of lithium ions. This may also be achieved by strategic doping in cubic LLZO, such as by doping Sr\(^{2+}\) onto La\(^{3+}\) sites.

Moreover, there are coulombic interactions between the ions in the migration pathway due to their small separation distance, and it is conceivable that the coulombic repulsion between dopants, such as Al\(^{3+}\), Zn\(^{2+}\) and Ga\(^{3+}\), and Li\(^+\) is stronger than that between lithium ions; such coulombic repulsion can activate lithium ions. Thus, lithium ions can be activated by proper doping, which affects the concentration and mobility of charge carriers.

Among all dopants, Ga is the most effective in enhancing the lithium-ion conductivity. Ga\(_2\)O\(_3\) is introduced into LLZO according to

\[
\text{Ga}_2\text{O}_3 + 6\text{Li}_{li}^X \rightarrow 2\text{Ga}_{li}^{\bullet\bullet} + 4\text{V}_{li}^\prime + 3\text{Li}_2\text{O}.
\]

Although several researchers reported improved lithium-ion conductivity of LLZO by Ga-doping, the reported lithium-ion conductivity was only ~10\(^{-4}\) S/cm. More recently Bernuy-Lopez et al. reported a lithium-ion conductivity of 1.3 mS/cm for Li\(_{6.4}\)Ga\(_{0.2}\)La\(_3\)Zr\(_2\)O\(_{12}\) at 24 °C, and showed, using nuclear magnetic resonance measurements, that the Ga\(^{3+}\) was located on tetrahedral sites. Jalem et al. tried to explain the high conductivity of Ga-doped LLZO through understanding the influence of Ga\(^{3+}\) on the Li site connectivity using molecular dynamics simulations, with their results showing that > 90% connectivity was retained up to \(x = 0.30\) in...
Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ $^{22}$ Even more recently, Rettenwander et al. reported a lithium-ion conductivity of 1.32 mS/cm for Li$_{6.4}$Ga$_{0.2}$La$_3$Zr$_2$O$_{12}$ at 20 °C, with a detailed study of the crystalline structure explaining the high lithium-ion conductivity $^{34}$. In this work, the lithium-ion conductivity of LLZO at room temperature is improved to 1.46 mS/cm through Ga-doping, and the origin of high lithium-ion conductivity of Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ electrolytes is expounded.

2. Experimental

2.1 Sample preparation

Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ ($x = 0.10, 0.15, 0.20, 0.25, 0.30, 0.35, \text{ and } 0.40$) electrolytes were prepared via a solid-state reaction from Li$_2$CO$_3$, La$_2$O$_3$, ZrO$_2$, and Ga$_2$O$_3$. 10 mol.% excess of Li$_2$CO$_3$ was used to compensate the lithium loss during high temperature calcination. The powders were ball-milled for 15 h, heated in air at 900 °C for 6 h, followed by ball-milling for another 15 h. The powders were then cold isostatically pressed into pellets at 250 MPa and sintered at 1100 °C for 24 h in air. In order to avoid Al$^{3+}$ contamination, a pellet of the same composition was put between the crucible and the sample during sintering. The samples were also covered with respective mother powders to prevent Li loss during sintering.

2.2 Composition and structure characterization

The chemical compositions of the samples were determined by inductively coupled plasma optical emission spectroscopy (ICP-OES) with an Optima 4300DV (America PerkinElmer Corporation). The relative densities of the samples were measured by the Archimedes method using water. Preliminary characterization of the crystalline
phases was performed using X-ray diffraction (XRD) with a XRD-7000S (Japan Shimadzu Corporation). Raman spectra were recorded in the range of 50 to 1200 cm\(^{-1}\) at room temperature (LabRAM HR800, France Horiba JobinYvon Corporation). Neutron powder diffraction (NPD) data were collected using ECHIDNA, the high-resolution neutron powder diffractometer at the Australian Nuclear Science and Technology Organisation (ANSTO) \(^{35}\). The neutron beam wavelength was determined to be 0.162172(5) nm using the La\(^{11}\)B\(_6\) NIST standard reference material (SRM 660b). GSAS-II was used to analyze the NPD data \(^{36}\). \(^6\)Li magic angle spinning nuclear magnetic resonance (MAS NMR) spectra were used to probe the local chemical environment of Li atoms and analyze the lithium-ion dynamics. The \(^6\)Li MAS NMR spectra were gathered at a Larmor frequency of 58.9 MHz on a Bruker Avance III 400 NMR spectrometer with a sample spinning speed of 20 kHz. The chemical shifts of \(^6\)Li were calibrated by using a 1 M LiCl solution. \(^6\)Li MAS NMR spectra were collected using a \(\pi/2\) pulse with a length of 7.5 \(\mu s\) and a recycle delay of 100 s. The spin lattice relaxation was characterized by the saturation recovery method.

2.3 Conductivity measurements

AC impedance measurements were undertaken to measure conductivity in the temperature range \( -60 \) to \( 60 \) °C using a Solartron 1260 impedance and gain-phase analyzer in the frequency range of 1 to \( 5 \times 10^6 \) Hz and at an amplitude of 50 mV. The sample is \( \sim 12 \) mm in diameter and 2 to 3 mm in thickness. Li-ion blocking Ag electrodes on the large surfaces were used. Before each measurement, samples were annealed for 1 h at the desired temperature to ensure equilibrium. Cells with only Li
electrodes were also prepared; two pieces of metallic Li were pasted on the large surfaces of the sample and heated at 120 °C for 3 h in a glovebox filled with Ar. The Li/LLZO/Li cell was sealed in the battery testing equipment for the AC impedance measurement at 30 °C. By applying a DC voltage of 0.1 V to the Ag/LLZO/Ag cell, we also determined the electronic conductivity by means of the DC polarization method, and the current was recorded for 1000 s during the polarization.

3. Results and discussion

3.1 Composition and structure

The elemental composition of the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples obtained by ICP-OES (Table 1) are close to the nominal composition, with the exception of a slightly higher lithium content, likely as a result of an excess of Li in the starting materials. No aluminum contamination was found.

The relative densities of the samples obtained by the Archimedes method reveal relative densities below 90% for samples with $x = 0.10$ and 0.15 and above 93% for well-sintered samples with $x \geq 0.20$.

XRD data of the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples are shown in Fig. 1(a), where all diffraction peaks can be assigned to a cubic garnet structure, although peaks from the Li$_{6.70}$Ga$_{0.10}$La$_3$Zr$_2$O$_{12}$ and Li$_{6.55}$Ga$_{0.15}$La$_3$Zr$_2$O$_{12}$ samples are broadened compared to those of the samples with $x \geq 0.20$, which could be attributed to the presence of the tetragonal garnet.

The Raman spectra of tetragonal and cubic garnets are readily distinguishable. The Raman spectra of the samples are shown in Fig. 1(b). The typical Raman spectra
of the LLZO garnets can be divided into three regions, a low-frequency region below 300 cm\(^{-1}\), an intermediate-frequency region between 300 and 550 cm\(^{-1}\), and a high-frequency region above 550 cm\(^{-1}\). The high-frequency region corresponds to the vibrational stretching modes of the ZrO\(_6\) octahedra, while the intermediate region has features mainly arising from vibrational bending modes of the octahedra, and the low-frequency region contains features corresponding to the translational modes of mobile ions. Features in the range of 100 to 300 cm\(^{-1}\) reveal the existence of the tetragonal garnet in the Li\(_{6.70}\)Ga\(_{0.10}\)La\(_3\)Zr\(_2\)O\(_{12}\) and Li\(_{6.55}\)Ga\(_{0.15}\)La\(_3\)Zr\(_2\)O\(_{12}\) samples, where sharp and split peaks arising from the reduction of symmetry from cubic to tetragonal exist \(^{37, 38}\). Therefore, samples with \(x = 0.10\) and 0.15 contain both tetragonal and cubic phases, and increasing Ga content to \(x \geq 0.20\) results in the pure cubic garnet.

3.2 Lithium ion conductivity

The conductivity of the Li\(_{7-3x}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) samples was measured by the AC impedance technique. Fig. 2 exhibits the impedance spectra and the fitting results for the Li\(_{6.25}\)Ga\(_{0.25}\)La\(_3\)Zr\(_2\)O\(_{12}\) sample under different conditions. When the testing temperature is –60 °C, a semi-circle and a dispersive line is seen in the spectrum, as shown in Fig. 2(a). With increasing temperature, the semi-circle reduces in size and vanishes at 0 °C. In the range of 10 to 60 °C, only a dispersive line is obtained, as shown in Fig. 2(b). The impedance spectra of the other samples are similar.

The intercept of the high frequency semi-circle of the impedance spectrum on the real axis represents the resistance of the sample, and the dispersive line represents the
lithium-ion transfer resistance of the Ag electrodes. The capacitances for the semicircles at low temperatures are on the level of $10^{-11}$ F, indicating a bulk property characteristic of LLZO electrolytes. Fig. 2(c) shows that when using Li electrodes the intercept of the high frequency semi-circle is almost identical to that obtained using Ag electrodes; therefore, the intercept of the high frequency semi-circle represents the sample resistance, while the intercept of the semi-circle at lower frequencies stands for the interfacial resistance between the sample and the Li electrodes.

Since it is impossible to distinguish the bulk and grain boundary resistances from the spectra, total conductivity is calculated here. The total conductivities of the samples at 25 °C are given in Table 1. When $x = 0.10$ and 0.15, the samples show low lithium-ion conductivities of 0.025 and 0.085 mS/cm, respectively, at 25 °C, due to the presence of the tetragonal garnet. With increasing Ga content, the total conductivity increases and then decreases, reaching a maximum at $x = 0.25$. The total conductivity of Li$_{6.25}$Ga$_{0.25}$La$_3$Zr$_2$O$_{12}$ at 25 °C is 1.46 mS/cm. For comparison, the electrical properties of the LLZO electrolytes are summarized in Table 2. Generally, only a few lithium-ion conductivities reported in literatures are above 1 mS/cm at 25 °C. A lithium-ion conductivity of about 1.3 mS/cm for Ga-doped LLZO through normal sintering was obtained by Bernuy-Lopez et al. $^{23}$ and Rettenwander et al. $^{34}$ The lithium-ion conductivity of Li$_{6.4}$La$_3$Zr$_{1.4}$Ta$_{0.6}$O$_{12}$ was enhanced to 1.6 mS/cm by hot-pressing by Du et al. $^{39}$, and the lithium-ion conductivity of Li$_{6.5}$La$_3$Zr$_{1.5}$Ta$_{0.5}$O$_{12}$ obtained by spark plasma sintering by Baek et al. $^{40}$ was 1.35 mS/cm, while the value for Al-containing Li$_{6.4}$La$_3$Zr$_{1.4}$Ta$_{0.6}$O$_{12}$ obtained by normal sintering was only ~1
mS/cm$^{14}$. Fig. 3 shows the temperature dependence of the total conductivities of the Li$_{7-x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples. Apparently, the conductivities of the samples ($x \geq 0.20$) with the cubic phase are higher than those of the samples containing both tetragonal and cubic phases. Activation energies are calculated from the slopes of the plots; the activation energy at temperatures lower than $\sim 20$ °C is slightly higher than that at higher temperatures, owing to the “ion trapping effect” at low temperatures, *i.e.* mobile Li$^+$ ions are trapped by immobile negatively charged defects$^{29}$. The activation energies for the overall testing temperature, as well as high and low temperature sides are given in Table 1. The activation energy decreases at first and then increases with increasing Ga content, reaching a minimum of 0.25 eV at $x = 0.25$. The low activation energies indicate that lithium ions transport easily in the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples. The activation energy for the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples with the cubic phase, derived from the data in the overall testing temperature, are in the range of 0.25 to 0.28 eV, which are amongst the lowest of the LLZO electrolytes in Table 2.

3.3 Electronic conductivity

An ideal solid electrolyte must be a purely ionic conductor, because electronic conduction causes electrical leakage or a short circuit in the lithium-ion battery. The DC polarization method was used to measure the electronic conductivity of the samples. DC voltage applied to the sample induces polarization, reaching steady-state over 1000 s (Fig. 4). Because the Ag electrode is blocking to lithium ions, but not to electrons, the current at the steady state arises only from the electronic conduction.
The electronic conductivity \((\sigma_e)\) is on the order of \(10^{-8} \text{ S/cm}\) (Table 1), being 4 or 5 orders of magnitude lower than the lithium-ion conductivity. Thus, the transference number of lithium ions \(t_{Li} = \frac{\sigma_{\text{total}} - \sigma_e}{\sigma_{\text{total}}}\) for the Li\(_{7.3}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) samples is nearly unity.

3.4 Modulus spectrum analysis

Complex modulus formalism is an important tool to derive information related to charge-transport processes. The complex electric modulus \((M^*)\) can be calculated from the complex impedance \((Z^*)\) through the relation:

\[
M^*(\omega) = i\omega C_0 Z^* = M'(\omega) + iM''(\omega)
\]

where the geometrical capacitance \(C_0 = \varepsilon_0 A/t\) (\(\varepsilon_0\) is the permittivity of free space, \(A\) the area of the electrode, and \(t\) the sample thickness), and \(M'\) and \(M''\) are the real and imaginary parts of the electric modulus, respectively.

Fig. 5 shows the imaginary part of the electric modulus \((M'')\) as a function of frequency for the Li\(_{7.3}\)Ga\(_x\)La\(_3\)Zr\(_2\)O\(_{12}\) samples in the temperature range of \(-60\) to \(0\) °C. The appearance of a peak in the modulus spectrum at low temperatures provides a signal of conductivity relaxation. The low frequency wing below the peak maximum \((M_{\text{max'''}})\) represents the range in which charge carriers are mobile at long distance. On the other hand, at frequencies above the peak maximum the charge carriers are confined to potential wells and mobile at short distance. The peak frequency increases with increasing temperature and the peak disappears at a threshold temperature, \(e.g.,\) \(-50\) °C for Li\(_{6.25}\)Ga\(_{0.25}\)La\(_3\)Zr\(_2\)O\(_{12}\) and \(-30\) °C for Li\(_{5.80}\)Ga\(_{0.40}\)La\(_3\)Zr\(_2\)O\(_{12}\). The temperature dependence of the peak frequency suggests that hopping dominates the
relaxation process. Also, the absence of a peak at temperatures > −50 °C for 
Li_{6.25}Ga_{0.25}La_{3}Zr_{2}O_{12} suggests that there is only long-range migration.

The peak frequency $f_{\text{max}}$ represents the conductivity relaxation frequency, and $f_{\text{max}}\tau_{\text{max}} = 1$, where $\tau_{\text{max}}$ is the characteristic relaxation time, representing the time scale of the transition from long- to short-range mobility. Better information on the bulk conduction properties can be obtained from the Arrhenius plot of $f_{\text{max}}$. In Fig. 5(f), the temperature dependence of $f_{\text{max}}$ for the Li_{5.80}Ga_{0.40}La_{3}Zr_{2}O_{12} sample is shown. The activation energy is 0.30 eV, very close to that obtained from the Arrhenius plot of the total conductivity in the low temperature range, further evidencing the long-range migration of free lithium ions.\textsuperscript{48, 57}

3.5 Concentration and mobility of charge carriers

The frequency dependence of the real part of the AC conductivity, $\sigma'(\omega)$, for the cubic Li_{7-3x}Ga_{x}La_{3}Zr_{2}O_{12} samples at selected temperatures are shown in Fig. 6. The $\sigma'(\omega)$ and frequency follow the Jonscher’s power law:\textsuperscript{58}

$$\sigma'(\omega) = \sigma_{dc} + A\omega^n = K\omega_c \left[1 + \left(\frac{\omega_{c}}{\omega}\right)^n\right]$$

(4)

where $\sigma_{dc}$ is the DC ionic conductivity, $\omega$ the angular frequency, $\omega_c$ the jumping rate of charge carriers, $A$ and $K$ the pre-factors, and $n$ a dimensionless frequency exponent in the range $0 < n < 1$. As shown in Fig. 6, one platform at high frequencies, representing the DC ionic conductivity, is found for each curve, and the decrease in the ionic conductivity at low frequencies can be ascribed to the electrode process. The bulk properties are the focus, therefore, the data at high frequencies are fitted according to the Jonscher’s power law. The fitting curves are also shown in Fig. 6.
The DC conductivity and the jump rate $\omega_c$ are calculated from the fitting curves. The concentration of mobile lithium ions is calculated according to the Nernst-Einstein-Smoluchowki equation:

$$\sigma_{dc} = e n_c \mu = \frac{n_c \omega_c e^2 \alpha^2}{2\pi k_B T}$$

(5)

where $n_c$ is the concentration of the mobile lithium ions, $\mu$ the mobility of the charge carriers, $\alpha$ the jumping distance (0.2 nm for LLZO \textsuperscript{28,29}), $k_B$ the Boltzmann constant, and $T$ the absolute temperature. The diffusion coefficient ($D$) is related to the mobility and the DC conductivity through the relationship:

$$D = \frac{k_B T \mu}{e} = \frac{\sigma_{dc} k_B T}{n_c e^2}$$

(6)

The typical results for the $\text{Li}_{7-3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$ samples are summarized in Table 3. The concentration of mobile lithium ions is on the order of $10^{21}$ cm$^{-3}$, mobility is on the order of $10^{-7}$ to $10^{-6}$ cm$^2$V$^{-1}$s$^{-1}$, and the jumping rate is on the order of $10^7$ rad/s at $-10$ °C. The concentration of mobile lithium ions in the $\text{Li}_{7-3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$ samples are comparable with that in pristine and W-doped LLZO \textsuperscript{28,29}, while the mobility and jumping rate of mobile lithium ions in the $\text{Li}_{7-3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$ samples are significantly higher. The diffusion coefficients are also higher than those previously reported for lithium ion conductors \textsuperscript{28,29}. The high ionic conductivities of the $\text{Li}_{7-3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$ samples can thus be ascribed to the increased mobility of lithium ions.

3.6 Lithium ion distribution

Lithium ion distribution at tetrahedral and octahedral sites is a crucial factor determining the overall mobility of lithium ions in LLZO electrolytes, because lithium
ions at octahedral sites exhibit higher mobility than those at tetrahedral sites \cite{29}.

The initial structure model used in the Rietveld analysis of the NPD data for the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ ($x = 0.20$ and $0.30$) samples was taken from Wang \textit{et al.} \cite{29} and Chen \textit{et al.} \cite{33}, in which Ga atoms occupy the Li (24$d$) site \cite{23}. The results of structure refinement are listed in Table 4 and the corresponding Rietveld refinement plots are shown in Fig. 7. Two kinds of lithium ions occupy 24$d$ (tetrahedral) and 96$h$ (octahedral) sites, and 96$h$ sites characterize positions that deviate from the center of octahedral 48$g$ sites, with lithium content at the 96$h$ site being higher than that at the 24$d$ site. The other ions (La, Zr and O) are at their normal lattice sites.

$^6$Li MAS NMR was used to detect the lithium-ion local environment and dynamics in the Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples, and corresponding $^6$Li MAS NMR spectra are shown in Fig. 8(a). The typical chemical shift of lithium at 24$d$ tetrahedral and 48$g$ octahedral sites are 0.8 and 1.9 ppm, respectively, and that of lithium at 96$h$ octahedral sites is characterized by a low chemical shift \cite{29,59}. Combined with the NPD results, we can conclude that the peaks at around 1.3 ppm in Fig. 8(a) can be attributed to lithium at the 96$h$ site, and this signal overlaps that at 0.8 ppm arising from lithium ions at the 24$d$ site. It is difficult to quantitatively determine lithium content at tetrahedral and octahedral sites by fitting these overlapped peaks. Fortunately, the spin-lattice relaxation time ($T_1$) of lithium is also sensitive to the local environment. Fig. 8(b) shows the saturation recovery of the $^6$Li signal, and a bi-exponential function describes the data well. The fitting reveals a main component (\sim92\%) with smaller $T_1$ ($t2 = 1.72186$ s) arising from lithium at octahedral sites and
minor component with larger $T_1$ ($t_1 = 60.8798 \text{ s}$) arising from lithium at tetrahedral sites. The smaller $T_1$ of lithium at the 96h octahedral site suggests a higher mobility.

From the NPD and $^6$Li MAS NMR results, it is clear that more lithium resides at octahedral than tetrahedral sites. Lithium at the 96h site is not centrally located within the octahedron (Fig. 9). Electrostatic repulsion, including Li$^+$ - Li$^+$ and Li$^+$ - dopant pairs, causes the redistribution of lithium between tetrahedral and octahedral sites, and the Li$^+$ - dopant repulsion also influences the lithium at neighboring sites. Therefore, the strong coulombic repulsion between immobile Ga$^{3+}$ and the nearby lithium ions shifts lithium away from their central position within the octahedron in the Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ garnets. The lithium-ion distribution in Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ is therefore significantly different to that in the Te or W doped garnets, where a large number of lithium ions are located at 48g sites. Hence, the high lithium-ion conductivity of Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ electrolytes can be ascribed to enhanced mobility of lithium ions arising from the coulombic repulsion between Ga$^{3+}$ and Li$^+$ ions. This could also explain the relatively low activation energies for conductivity in the Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ system.

In cubic LLZO, lithium ions can transport along tetrahedral and octahedral sites, with the possibility for lithium exchange between the sites as a consequence of vacancies at both sites. Generally, the direct lithium-ion transport along tetrahedral sites is difficult; Li NMR and dielectric loss spectroscopy measurements suggest a pathway of 48g/96h-48g/96h involving only octahedral sites. However, anisotropic atomic displacement parameters obtained using neutron diffraction,
maximum entropy methods and two-dimensional \(^{6}\text{Li}^{6}\text{Li}\) exchange NMR spectra, suggest that the diffusion occurs through the pathway \(24d-48g/96h-24d\) \cite{29,62,63}. As the jumping rate of lithium at tetrahedral sites is lower than that at octahedral sites, the lithium-ion migration rate through the \(24d-96h-24d\) pathway is limited by the jumping rate of lithium at tetrahedral sites. In the \(24d-96h-24d\) pathway, \(\text{Ga}^{3+}\) ions have little impact on lithium-ion mobility, because they are separated from lithium at tetrahedral sites by Li at octahedral sites (Fig. 9). However, the mobility of lithium ions in the \(\text{Li}_{7.3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}\) samples is greatly enhanced by Ga, relative to both pristine and W-doped LLZO \cite{28,29}. As found in the work of Wang et al. \cite{29}, the \(^{6}\text{Li}^{6}\text{Li}\) exchange signal, characterizing lithium-ion transport between the two different sites, indicated the lithium-ion transport along octahedral sites. Wagner et al. \cite{26} also proposed an additional lithium-ion diffusion pathway in the \(\text{Ga}^{3+}\) doped garnets, as informed by \(^7\text{Li}\) NMR spin-lattice relaxation rates. Taken together, there are two migration pathways (Fig. 9(c)) in the \(\text{Li}_{7.3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}\) garnets: \(24d-96h-24d\) and \(96h-96h\); however, the migration rate of lithium ions between \(96h-96h\) sites is much higher.

4. Conclusions

The present study thoroughly investigates the influence of Ga doping on the properties of \(\text{Li}_{7.3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}\) garnets. The minimum concentration of Ga required for stabilizing the cubic phase is found to be 0.20 Ga per formula unit, below which both cubic and tetragonal phases coexist. In the \(\text{Li}_{7.3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}\) garnets, lithium ions predominantly occupy the 96\(h\) site, which is non-central within the octahedron as a result of coulombic repulsion between \(\text{Ga}^{3+}\) and \(\text{Li}^{+}\). The remaining Li is found at
the tetrahedral site. The highest lithium-ion conductivity of 1.46 mS/cm at 25 °C is found at a Ga concentration of 0.25 per formula unit, at which the activation energy for conductivity reaches its minimum of 0.25 eV. The enhancement of conductivity by Ga can be ascribed to a high mobility of lithium ions arising from the coulombic repulsion between Ga$^{3+}$ and Li$^+$. This work opens the door to the strategic doping of other electrolytes to enhance ionic conductivity.

**Acknowledgements**

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Table 1. Chemical composition, relative density, total conductivity, activation energy, and electronic conductivity of Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples

<table>
<thead>
<tr>
<th>$x$</th>
<th>Li:La:Zr:Ga</th>
<th>Relative density (%)</th>
<th>$\sigma_{\text{total}}$ (mS/cm)</th>
<th>$E_a$ (eV)</th>
<th>$\sigma_{\text{electronic}}$ ($10^{-7}$ S/cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Nominal ICPOES result$^a$</td>
<td></td>
<td></td>
<td>Overall High $T$ Low $T$</td>
<td></td>
</tr>
<tr>
<td>0.10</td>
<td>6.70:3:2:0.10</td>
<td>86.7</td>
<td>0.025</td>
<td>0.34</td>
<td>-</td>
</tr>
<tr>
<td>0.15</td>
<td>6.55:3:2:0.15</td>
<td>89.6</td>
<td>0.085</td>
<td>0.33</td>
<td>-</td>
</tr>
<tr>
<td>0.20</td>
<td>6.30:3:2:0.20</td>
<td>7.02:3:1.95:0.19</td>
<td>93.4</td>
<td>0.87</td>
<td>0.28</td>
</tr>
<tr>
<td>0.25</td>
<td>6.25:3:2:0.25</td>
<td>6.79:3:1.97:0.25</td>
<td>94.1</td>
<td>1.46</td>
<td>0.25</td>
</tr>
<tr>
<td>0.30</td>
<td>6.10:3:2:0.30</td>
<td>6.32:3:1.96:0.29</td>
<td>96.3</td>
<td>1.12</td>
<td>0.25</td>
</tr>
<tr>
<td>0.35</td>
<td>5.95:3:2:0.35</td>
<td>6.43:3:1.99:0.33</td>
<td>95.1</td>
<td>0.71</td>
<td>0.26</td>
</tr>
<tr>
<td>0.40</td>
<td>5.80:3:2:0.40</td>
<td>6.64:3:2.02:0.42</td>
<td>92.8</td>
<td>0.57</td>
<td>0.26</td>
</tr>
</tbody>
</table>

$^a$ Atomic ratio of Li:La:Zr:Ga is normalized by La content in the formula Li$_{7-3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$.
Table 2. Electrical properties of LLZO electrolytes

<table>
<thead>
<tr>
<th>Composition</th>
<th>Relative density (%)</th>
<th>$\sigma_{\text{total}}$ (mS/cm)</th>
<th>Temperature (°C)</th>
<th>$E_a$ (eV)</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{Li}<em>{6.25}\text{Ga}</em>{0.25}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>94.1</td>
<td>1.46</td>
<td>25</td>
<td>0.25</td>
<td>this work</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.4}\text{Ga}</em>{0.2}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>--</td>
<td>1.32</td>
<td>20</td>
<td>0.256</td>
<td>[34]</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.55}\text{Ga}</em>{0.15}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>--</td>
<td>1.3</td>
<td>25</td>
<td>0.30</td>
<td>[23]</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.6}\text{Ga}</em>{0.2}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>--</td>
<td>0.9</td>
<td>25</td>
<td>0.30</td>
<td>[23]</td>
</tr>
<tr>
<td>$\text{Li}_x\text{Ga}_y\text{La}_z\text{Zr}<em>2\text{O}</em>{12}$</td>
<td>92.5</td>
<td>0.54</td>
<td>20</td>
<td>0.32 ~ 0.37</td>
<td>[21]</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.25}\text{Ga}</em>{0.25}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>--</td>
<td>0.35</td>
<td>--</td>
<td>--</td>
<td>[18]</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.15}\text{Ga}</em>{0.3}\text{La}_x\text{Zr}<em>y\text{O}</em>{12}$</td>
<td>96 ~ 98</td>
<td>0.41</td>
<td>25</td>
<td>0.27</td>
<td>[19]</td>
</tr>
<tr>
<td>$\text{Li}_{6.15}\text{Al}_x\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>0.37</td>
<td></td>
<td>25</td>
<td>0.30</td>
<td>[29]</td>
</tr>
<tr>
<td>$\text{Li}_{6.4}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>99.6</td>
<td>1.6</td>
<td>25</td>
<td>0.26</td>
<td>[39]</td>
</tr>
<tr>
<td>$\text{Li}_{7.4}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>1.35</td>
<td>25</td>
<td>0.36</td>
<td>[40]</td>
</tr>
<tr>
<td>$\text{Li}_{6.75}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.74</td>
<td>25</td>
<td>0.33</td>
<td>[41]</td>
</tr>
<tr>
<td>$\text{Li}_{6.4}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.724</td>
<td>25</td>
<td>0.24</td>
<td>[42]</td>
</tr>
<tr>
<td>$\text{Li}_{6.8}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>-- 6.8\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}</td>
<td>0.69</td>
<td>RT ~ 0.36</td>
<td>[43]</td>
<td></td>
</tr>
<tr>
<td>$\text{Li}_x\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.18</td>
<td>25</td>
<td>0.42</td>
<td>[44]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.92</td>
<td>25</td>
<td>--</td>
<td>[14]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.73</td>
<td>--</td>
<td>--</td>
<td>[14]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>94.1</td>
<td>0.928</td>
<td>24</td>
<td>0.32 ~ 0.34</td>
<td>[45]</td>
</tr>
<tr>
<td>$\text{Li}_{6.4}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.61</td>
<td>33</td>
<td>0.34</td>
<td>[46]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.409</td>
<td>25</td>
<td>0.30</td>
<td>[15]</td>
</tr>
<tr>
<td>$\text{Li}<em>{6.8}\text{La}<em>x\text{Y}</em>{0.25}\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.436</td>
<td>27</td>
<td>0.34</td>
<td>[47]</td>
</tr>
<tr>
<td>$\text{Li}_{6.5}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>1.02</td>
<td>30</td>
<td>0.37</td>
<td>[48]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>82.4</td>
<td>0.40</td>
<td>27</td>
<td>0.33</td>
<td>[16]</td>
</tr>
<tr>
<td>$\text{Li}_{7.2}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>80.2</td>
<td>0.369</td>
<td>27</td>
<td>0.37</td>
<td>[16]</td>
</tr>
<tr>
<td>$\text{Li}_{6.5}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>93 ~ 95</td>
<td>0.49</td>
<td>25</td>
<td>0.35</td>
<td>[29]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.80</td>
<td>25</td>
<td>0.31</td>
<td>[49]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.1</td>
<td>30</td>
<td>0.36</td>
<td>[50]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.4</td>
<td>25</td>
<td>0.41</td>
<td>[51]</td>
</tr>
<tr>
<td>$\text{Li}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>82</td>
<td>0.34</td>
<td>25</td>
<td>0.33</td>
<td>[52]</td>
</tr>
<tr>
<td>$\text{Ge}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.763</td>
<td>25</td>
<td>--</td>
<td>[53]</td>
</tr>
<tr>
<td>$\text{Li}_{7.2}\text{La}<em>x\text{Zr}<em>y\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.81</td>
<td>25</td>
<td>0.26</td>
<td>[54]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.2</td>
<td>25</td>
<td>--</td>
<td>[55]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>99</td>
<td>0.37</td>
<td>RT</td>
<td>--</td>
<td>[56]</td>
</tr>
<tr>
<td>$\text{Al}_{x}\text{La}<em>y\text{Zr}<em>z\text{Ta}</em>{0.25}\text{O}</em>{12}$</td>
<td>--</td>
<td>0.244</td>
<td>25</td>
<td>0.34</td>
<td>[11]</td>
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</table>
Table 3. DC conductivity ($\sigma_{DC}$), jumping rate ($\omega_c$), frequency exponent ($n$), concentration ($n_c$), mobility ($\mu$), and diffusion coefficient ($D$) of charge carriers for Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples

<table>
<thead>
<tr>
<th>Sample</th>
<th>Temp. (°C)</th>
<th>$\sigma_{DC}$ (mS/cm)</th>
<th>$\omega_c$ ($10^7$ rad/s)</th>
<th>$n$</th>
<th>$n_c$ ($10^{21}$ cm$^{-3}$)</th>
<th>$\mu$ ($10^{-7}$ cm$^2$V$^{-1}$s$^{-1}$)</th>
<th>$D$ ($10^{-8}$ cm$^2$s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Li$<em>{6.40}$Ga$</em>{0.20}$La$_3$Zr$<em>2$O$</em>{12}$</td>
<td>-10</td>
<td>0.187</td>
<td>5.65</td>
<td>0.59</td>
<td>1.18</td>
<td>9.96</td>
<td>2.26</td>
</tr>
<tr>
<td></td>
<td>-30</td>
<td>0.075</td>
<td>2.57</td>
<td>0.90</td>
<td>0.96</td>
<td>4.90</td>
<td>1.02</td>
</tr>
<tr>
<td></td>
<td>-60</td>
<td>0.011</td>
<td>0.35</td>
<td>0.89</td>
<td>0.89</td>
<td>0.76</td>
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Table 4. Structural parameters of Li$_{6.40}$Ga$_{0.20}$La$_3$Zr$_2$O$_{12}$ and Li$_{6.10}$Ga$_{0.30}$La$_3$Zr$_2$O$_{12}$ samples obtained using NPD data (space group $Ia\overline{3}d$)

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<th>Stoichiometry</th>
<th>Lattice parameter (nm)</th>
<th>$R_{wp}$ (%)</th>
<th>GOF</th>
<th>Site</th>
<th>Occupancy</th>
<th>$x$</th>
<th>$y$</th>
<th>$z$</th>
<th>$U_{iso}$ (Å$^2$)</th>
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Fig. 1 (a) XRD patterns and (b) Raman spectra of Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples.
Fig. 2 AC impedance spectra and fitting results of Li$_{6.25}$Ga$_{0.25}$La$_3$Zr$_2$O$_{12}$ (a, b) at different temperatures, and (c) with Ag and Li electrodes at 30 °C. The insets in (a) and (b) are the equivalent circuits used. The inset in (c) represents the high frequency regions of the corresponding impedance spectra.
Fig. 3 Temperature dependence of the conductivity of Li$_{7.3}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples. The dashed line shows the slopes at high and low temperatures.
Fig. 4 DC polarization plots of Li$_{7.3x}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples.
Fig. 5 Frequency dependence of $M''$ for $\text{Li}_{7.3x}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$ samples with different $x$ values: (a) 0.20, (b) 0.25, (c) 0.30, (d) 0.35 and (e) 0.40, and (f) temperature dependence of $f_{\text{max}}$ for $\text{Li}_{5.80}\text{Ga}_{0.40}\text{La}_3\text{Zr}_2\text{O}_{12}$ sample.
Fig. 6 Frequency dependent $\sigma(\omega)$ of Li$_{7.3}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples with different $x$ values: (a) 0.20, (b) 0.25, (c) 0.30, (d) 0.35 and (e) 0.40.
Fig. 7 Rietveld refinement plots using room temperature NPD data for (a) Li_{6.40}Ga_{0.20}La_{3}Zr_{2}O_{12} and (b) Li_{6.10}Ga_{0.30}La_{3}Zr_{2}O_{12} samples.
Fig. 8 (a) $^6$Li MAS NMR spectra of Li$_{7.3}$Ga$_x$La$_3$Zr$_2$O$_{12}$ samples with $x$ values shown inset, and (b) spin-lattice relaxation curve and fitting result of Li$_{6.10}$Ga$_{0.30}$La$_3$Zr$_2$O$_{12}$. In the fitting equation, A1 and t1 represent the smaller component with a longer spin-lattice relaxation time, while A2 and t2 represent the larger component with a shorter spin-lattice relaxation time.
Fig. 9. (a) Crystal structure of $\text{Li}_{7.3}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$, (b) $\text{Li}^+$ and $\text{Ga}^{3+}$ environment, and (c) lithium-ion diffusion pathways in $\text{Li}_{7.3}\text{Ga}_x\text{La}_3\text{Zr}_2\text{O}_{12}$. 