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Electrostrictive effect in ferroelectrics: An alternative approach to improve piezoelectricity

Fei Li

Xi'an Jiaotong University, lifei1216@gmail.com

Li Jin

Xi'an Jiaotong University

Zhuo Xu

Xi'an Jiaotong University

Shujun Zhang

The Pennsylvania State University, shujun@uow.edu.au

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Electrostrictive effect in ferroelectrics: An alternative approach to improve piezoelectricity

Abstract

Electrostriction plays an important role in the electromechanical behavior of ferroelectrics and describes a phenomenon in dielectrics where the strain varies proportional to the square of the electric field/polarization. Perovskite ferroelectrics demonstrating high piezoelectric performance, including BaTiO₃, Pb(Zr_{1-x}Ti_x)O₃, and relaxor-PbTiO₃ materials, have been widely used in various electromechanical devices. To improve the piezoelectric activity of these materials, efforts have been focused on the ferroelectric phase transition regions, including shift the composition to the morphotropic phase boundary or shift polymorphic phase transition to room temperature. However, there is not much room left to further enhance the piezoelectric response in perovskite solid solutions using this approach. With the purpose of exploring alternative approaches, the electrostrictive effect is systematically surveyed in this paper. Initially, the techniques for measuring the electrostrictive effect are given and compared. Second, the origin of electrostriction is discussed. Then, the relationship between the electrostriction and the microstructure and macroscopic properties is surveyed. The electrostrictive properties of ferroelectric materials are investigated with respect to temperature, composition, phase, and orientation. The relationship between electrostriction and piezoelectric activity is discussed in detail for perovskite ferroelectrics to achieve new possibilities for piezoelectric enhancement. Finally, future perspectives for electrostriction studies are proposed. 2014 AIP Publishing LLC.

Keywords

improve, piezoelectricity, approach, electrostrictive, alternative, effect, ferroelectrics

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Electrostrictive effect in ferroelectrics: An alternative approach to improve piezoelectricity

Fei Li,¹ Li Jin,¹ Zhuo Xu,¹ and Shujun Zhang^{2,a)}

¹Electronic Materials Research Laboratory, Key Laboratory of the Ministry of Education and International Center for Dielectric Research, Xi'an Jiaotong University, Xi'an 710049, China

²Materials Research Institute, Pennsylvania State University, University Park, Pennsylvania 16802, USA

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Electrostriction plays an important role in the electromechanical behavior of ferroelectrics and describes a phenomenon in dielectrics where the strain varies proportional to the square of the electric field/polarization. Perovskite ferroelectrics demonstrating high piezoelectric performance, including BaTiO₃, Pb(Zr_{1-x}Ti_x)O₃, and relaxor-PbTiO₃ materials, have been widely used in various electromechanical devices. To improve the piezoelectric activity of these materials, efforts have been focused on the ferroelectric phase transition regions, including shift the composition to the morphotropic phase boundary or shift polymorphic phase transition to room temperature. However, there is not much room left to further enhance the piezoelectric response in perovskite solid solutions using this approach. With the purpose of exploring alternative approaches, the electrostrictive effect is systematically surveyed in this paper. Initially, the techniques for measuring the electrostrictive effect are given and compared. Second, the origin of electrostriction is discussed. Then, the relationship between the electrostriction and the microstructure and macroscopic properties is surveyed. The electrostrictive properties of ferroelectric materials are investigated with respect to temperature, composition, phase, and orientation. The relationship between electrostriction and piezoelectric activity is discussed in detail for perovskite ferroelectrics to achieve new possibilities for piezoelectric enhancement. Finally, future perspectives for electrostriction studies are proposed. © 2014 AIP Publishing LLC. [<http://dx.doi.org/10.1063/1.4861260>]

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^{a)}Author to whom correspondence should be addressed. Electronic mail: soz1@psu.edu; shujunzhang@gmail.com.

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I. INTRODUCTION

Electrostriction is a basic electromechanical phenomenon in all insulators or dielectrics. It describes the electric field/polarization-induced strain (S_{ij}) that is proportional to the square of electric field (E_i)/polarization (P_i), expressed in the following equations:

$$\begin{aligned} S_{ij} &= Q_{ijkl} P_k P_l, \\ S_{ij} &= M_{ijkl} E_k E_l, \end{aligned} \quad (1)$$

where Q_{ijkl} and M_{ijkl} are electrostrictive coefficients. Electrostriction is a four-rank tensor property; thus it can be observed in all crystal symmetries.¹

The strain induced by the electrostrictive effect is generally small when compared with that induced by piezoelectricity. Consequently, there has been limited attention focusing on the electrostrictive effect. In the 1980s, a systematic study on electrostriction was carried out on relaxor ferroelectrics with perovskite structures, such as $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ (PMN), $\text{Pb}(\text{Zn}_{1/3}\text{Nb}_{2/3})\text{O}_3$ (PZN), and $0.9\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3\text{-}0.1\text{PbTiO}_3$ (PMN-0.1PT) single crystals/ceramics, in which a high electrostrictive strain was observed because of the high dielectric response of the relaxors.²⁻⁷ Relaxors offer several advantages over ferroelectric materials, including low hysteresis in the strain-field response (excellent displacement accuracy), no remnant strain, reduced aging effects, and they do not require poling.³ Compared with classical ferroelectric ceramics, these materials are believed to have potential for use in actuator applications such as inchworms, micro-angle adjusting devices, and bistable optical devices, where reproducible and non-hysteretic deformation responses are required.³ In addition, in the 1990s, investigations on electrostriction were performed on polymers,⁸⁻¹⁵ including ferroelectric polymers, dielectric elastomers, and polymer composites. Ultra-high electrostrictive strains were observed in these polymeric materials (>4% for polyvinylidene fluoride [PVDF] and >40% for silicone), giving them potential for use in actuator applications.¹⁵

On the other hand, ferroelectrics are the mainstay materials for piezoelectric transducer and actuator applications and have been reported to possess much higher piezoelectric responses when compared with non-ferroelectric materials.¹⁶ Typical ferroelectric single crystals and ceramics, including barium titanate (BaTiO_3 , BT) (reported in the 1940s),¹⁷ lead titanate zirconate ($\text{Pb}(\text{Zr}_{1-x}\text{Ti}_x)\text{O}_3$, PZT) polycrystalline ceramics (reported in the 1950s),¹⁷ and relaxor-PT based single crystals (reported in the 1980s to 1990s),¹⁸⁻²³ exhibited piezoelectric responses that are two to three orders higher than Quartz crystals (first piezoelectric crystal ~ 2 pC/N). Similar to inorganic ferroelectrics, ferroelectric polymers such as PVDF also possess a higher piezoelectric response than their nonferrous counterpart.^{24,25} Thus, it is desirable to

understand the origins of high piezoelectric activity in ferroelectrics. For ferroelectrics whose paraelectric phase is centrosymmetric, the piezoelectric coefficient d_{mij} can be expressed as a derivative of strain to electric field

$$\begin{aligned} d_{mij} &= \frac{\partial S_{ij}}{\partial E_m} = \frac{Q_{ijkl} P_k \partial P_l}{\partial E_m} + \frac{Q_{ijkl} P_l \partial P_k}{\partial E_m} \\ &= Q_{ijkl} P_k \varepsilon_{lm} + Q_{ijkl} P_l \varepsilon_{km}, \end{aligned} \quad (2)$$

where ε_{ij} is the dielectric permittivity, and i, j, k, l , and $m = 1, 2$, or 3 . Equation (1) is used as the expression of strain (S_{ij}). Equation (2) indicates that the piezoelectric coefficients of these ferroelectrics originate from the electrostrictive effect, spontaneous polarization, and the dielectric response. Figure 1 shows that the piezoelectric coefficients can be recognized as the slope of the electrostrictive strain versus the electric field. Thus, we can conclude that the high piezoelectric response in ferroelectrics is established on the electrostrictive effect and is associated with a large “bias polarization” (spontaneous polarization). The electrostrictive effect plays a key role in the electromechanical behavior in ferroelectrics, investigations on which will benefit the exploration of high-performance piezoelectrics. In this paper, the investigations on the electrostrictive effect are surveyed, focusing on ferroelectric-related materials. First, the measurement methods of the electrostrictive effect are given and compared. Second, the origin of electrostriction is discussed for ionic crystals. Then, the relationships between the electrostriction and the crystal structure, dielectric response, elastic property and thermal expansion are surveyed. The electrostrictive properties of the ferroelectric materials are investigated with respect to temperature, composition, ferroelectric phase, and orientation. Finally, the contribution of electrostriction to the piezoelectric activity is discussed in detail for perovskite ferroelectrics, and we outline a possible approach for improving the piezoelectricity through the electrostrictive effect.

II. THE DETERMINATION OF THE ELECTROSTRICTIVE COEFFICIENTS

To determine the electrostrictive coefficients, five approaches have been proposed in the literature. These are based on the strain-polarization/electric field curves, dielectric permittivity-stress curves, the piezoelectric effect for the

FIG. 1. Schematic plot of the relationship between electrostriction and piezoelectric effects. Due to the high “bias polarization,” an ac electric field can induce ac strain with the same frequency of electric field.

FIG. 2. The polarization-electric field, strain-electric field, and strain-polarization loops for linear dielectrics. Reprinted with permission from G. Viola, T. Saunders, X. Wei, K. B. Chong, H. Luo, M. J. Reece, and H. Yan, *J. Adv. Dielectr.* **3**, 1350007 (2013). Copyright 2013 World Scientific Publishing Company.²⁷

FIG. 3. The polarization-electric field, strain-electric field, and strain-polarization loops for nonlinear dielectrics (taking [001] oriented PMN crystal as example).

ferroelectrics, the lattice parameters, and the dielectric permittivity under a DC-biased electric field.

A. Electrostrictive coefficients measured by strain versus the polarization/electric field

According to Eq. (1), the electrostrictive coefficients Q and M can be determined by measuring the strain-polarization (S-P) and strain-electric field (S-E) curves, respectively. The S-P and S-E curves are accepted as a method to determine the electrostrictive coefficients for materials with a high dielectric response, where the strains can be accurately measured.

Figures 2 and 3 show the measured results for a $\text{BaBi}_2\text{Nb}_2\text{O}_9$ ceramic and an [001] oriented PMN single crystal, respectively.^{26,27} A linear relationship between the polarization and electric field was observed in Fig. 2(a), indicating that the $\text{BaBi}_2\text{Nb}_2\text{O}_9$ ceramic is a linear dielectric material. The strain followed a quadratic function with respect to both the electric-field and polarization, as shown in Figs. 2(b) and 2(c). On the contrary, PMN crystals are nonlinear dielectrics. Figure 3(a) shows the polarization saturation at high fields that deviate from a linear relationship. For nonlinear dielectrics, the electrostrictive strain is not a quadratic function of the electric field but follows a quadratic relation with respect to the polarization (Figs. 3(b) and 3(c)). Thus, the Q coefficient is preferred over the M coefficient, for the investigation of the electrostrictive effect. For this reason, the following discussions on ferroelectrics focus on the Q coefficients.

To determine the Q coefficients in ferroelectrics, domain reorientation (or domain wall motion) and electric field-induced phase transitions should be avoided. Figure 4 shows the phenomenon of domain reorientation in tetragonal ferroelectric crystals for the Q_{33} measurements along the [001] direction. For this condition, the contribution of 180° ferroelectric domain switching contributed to the strain and polarization is $2d_{33}E$ and $2P_s$, respectively, as shown in Fig. 4(a).

Generally, $2d_{33}E$ was much smaller than $4P_s^2Q_{33}$; thus the presence of the 180° ferroelectric domain switching mitigates the measured Q value. On the contrary, the 90° ferroelastic domain switching made the measured Q_{33} larger than the real value of the lattice deformation. This was caused by polarization variations along the perpendicular direction, which was not considered in the measurement. Overall, domain switching impacted the electrostrictive coefficient measurements. Ferroelectric phase transitions also affected the measured results, because the direction of the spontaneous polarization varied during the ferroelectric phase transitions. To eliminate the impact of the domain wall motion

FIG. 4. Schematic figure of domain reorientation effect on determination of longitudinal electrostrictive coefficient Q_{33} , where 90° and 180° domain reorientations are considered. In figure (a), the d_{33} , E , and P_s are piezoelectric coefficient, coercive field, and spontaneous polarization, respectively. The S_3 and S_1 are the spontaneous strain along c and a crystallographic axes, respectively.

FIG. 5. The strain-polarization loops for [001] oriented PMN, PMN-0.28PT, and PZN crystals, being measured at 25, 150, and 150 °C, respectively. Reprinted with permission from Appl. Phys. Lett. **102**, 152910 (2013). Copyright 2013 AIP Publishing LLC.²⁶

and phase transition, the S-P curves should be measured at high temperatures (higher than the Curie temperature, T_C) and at high electric fields, because no ferroelectric domains exist in the paraelectric phase above the T_C , meanwhile, the domains could be clamped by high electric fields, increasing the difficulty in the domain switching.

Figure 5 shows the electrostriction results for [001] oriented PMN, PMN-0.28PT, and PZN crystals at temperatures above the temperature of maximum permittivity (T_m).²⁶ The S-P curves exhibited hysteretic behavior, which can be separated into hysteretic and reversible regions. The hysteretic region in the S-P curves can be attributed to either the micro-domain reorientation in relaxor materials (micro-domains exist at temperatures above T_m) or the electric-field-induced micro-macro domain transition.^{28,29} It should be noted here that the hysteretic region was also related to the measurement condition. For example, PMN-0.1PT thin film does not show obvious hysteretic S-P behavior at the temperatures above T_m .³⁰ The difference between the results of Fig. 5 and Ref. 30 can be attributed to the substrate clamping effect of thin film and different measurement conditions (frequency and amplitude of electric field). The strain and polarization induced by the intrinsic lattice contribution at a high electric field accounts for the reversible S-P curve. By fitting the experimental data using $S_{33} = Q_{33}P_3^2$, the electrostrictive coefficient Q_{33} can be determined with respect to the amplitude

of the electric field, as given in Fig. 6. In the electric field range of 10–80 kV/cm, the measured Q_{33} values for [001] oriented PMN-0.28PT, PZN, and PMN crystals increased with the electric field increasing, being in the ranges of 0.037–0.053 m^4/C^2 , 0.043–0.060 m^4/C^2 , and 0.018–0.027 m^4/C^2 , respectively. This was because the micro-domain reorientation (180°) reduced the measured Q value at low electric fields, while the measured Q approached the intrinsic value (lattice) at high electric fields.

B. Electrostrictive coefficients measured using the dielectric permittivity versus the applied stress

Determination of electrostrictive coefficients from the relationship between dielectric permittivity and applied stress was based on the converse effect of electrostriction. The direct effect of electrostriction was given in Eq. (1) from which the electrostrictive coefficient Q_{ijkl} can be expressed as follows:

$$Q_{ijkl} = \frac{1}{2} \frac{\partial^2 S_{ij}}{\partial P_k \partial P_l}. \quad (3)$$

Based on the elastic Gibbs free energy [Eq. (4)] and changing the order of differentiation in the free energy equation, Eq. (3) was transformed to Eq. (5) (Refs. 31 and 32)

$$dG_1 = -S_{ij}dX_{ij} + E_i dP_i - SdT, \quad (4)$$

$$Q_{ijkl} = -\frac{1}{2} \frac{\partial^3 G_1}{\partial X_{ij} \partial P_k \partial P_l} = -\frac{1}{2} \frac{\partial^2 E_k}{\partial X_{ij} \partial P_l} = -\frac{1}{2} \frac{\partial \chi_{kl}}{\partial X_{ij}}, \quad (5)$$

where G_1 is the elastic Gibbs free energy, X_{ij} is the stress, S is the entropy, T is the temperature, and χ_{kl} is the inverse dielectric permittivity. Using the same method, the coefficient M_{ijkl} can be expressed as

$$dG = -S_{ij}dX_{ij} - P_i dE_i - SdT, \quad (6)$$

$$M_{ijkl} = -\frac{1}{2} \frac{\partial^3 G}{\partial X_{ij} \partial E_k \partial E_l} = \frac{1}{2} \frac{\partial^2 P_k}{\partial X_{ij} \partial E_l} = -\frac{1}{2} \frac{\partial \epsilon_{kl}}{\partial X_{ij}}, \quad (7)$$

where G is the Gibbs free energy and ϵ_{kl} is the dielectric permittivity. Equations (5) and (7) describe the converse effect of

FIG. 6. (a) Strain-polarization loops for [001] oriented PMN-0.28PT measured at various amplitudes of electric field. (b) The electrostrictive coefficient Q_{33} with respect to the amplitude of electric field for [001] oriented PMN, PMN-0.28PT, and PZN crystals. Reprinted with permission from Appl. Phys. Lett. **102**, 152910 (2013). Copyright 2013 AIP Publishing LLC.²⁶

FIG. 7. Determination of Q_h for KMnO_3 via converse electrostrictive effect. Reprinted with permission from K. Rittenmyer, A. S. Bhalla, and L. E. Cross, *Ferroelectrics Lett. Sec. 9*, 161 (1989). Copyright 1989 Taylor & Francis.³³

electrostriction. According to Eq. (5), the Q coefficients can be written as follows:

$$Q_{33} = -\frac{1}{2} \frac{\partial \chi_{33}}{\partial X_{33}}, \quad (8)$$

$$Q_{31} = -\frac{1}{2} \frac{\partial \chi_{11}}{\partial X_{33}}. \quad (9)$$

In addition, for crystals with cubic symmetry, the hydrostatic electrostrictive coefficient Q_h can be written as³³

$$Q_h = -\frac{1}{2} \frac{\partial \chi_{11}}{\partial p}, \quad (10)$$

where p is the applied hydrostatic pressure. Equations (8)–(10) were successfully employed to determine the Q coefficients for materials with low electrostrictive strains. In these materials, it was difficult to accurately measure the S-P

curves. Based on this approach, the Q_h coefficient for KMnO_3 was determined, as shown in Fig. 7.^{11,33}

It is important to note that Eqs. (4)–(10) are only applicable for linear systems. In ferroelectric materials, the inverse dielectric permittivity and stress may not follow a linear relationship because of nonlinear phenomena such as the depolarization, domain wall motion, and phase transitions.³² Thus, the effects of the nonlinear phenomena should be minimized under the applied stress/hydrostatic pressure to accurately measure the Q coefficients in ferroelectrics. Figure 8 presents the stress-dependent dielectric properties for PMN-xPT crystals.^{34,35} In single domain crystals, the stress perpendicular to the poling direction was found to stabilize the polarization state; at this time, the depolarization or domain wall motion was difficult to be induced. For this condition, the measured Q_{33} coefficients were almost the same values as those measured from the S-P curves, as shown in Figs. 8(a) and 8(b). On the contrary, strong nonlinear phenomena existed when the compressive stress was along the poling direction, where a drastic increase in χ_{33} was caused by depolarization of the crystal, as shown in Fig. 8(c). For the case of hydrostatic pressure, χ_{kl} and the pressure followed a linear relationship at low pressures, and the obtained Q_h was close to that derived from the piezoelectricity of the crystal. At high level of hydrostatic pressure, however, ferroelectric phase transition may be induced, leading to nonlinear characteristics; the measured Q_h deviates from the real value; therefore, great attention needs to be paid to this method for determination of electrostrictive coefficients of ferroelectrics.

C. Electrostrictive coefficients determined using the piezoelectric coefficients

For ferroelectric single crystals, the electrostrictive coefficients can be calculated from the piezoelectric coefficients, dielectric permittivities, and spontaneous polarization, based on Eq. (2). For perovskite crystals with $3m$, $mm2$, and $4mm$

FIG. 8. Stress dependence of inverse dielectric permittivity for PMN-xPT crystals. (a) The stress along $[110]$ direction was applied to $[111]$ poled PMN-0.28PT rhombohedral crystals. The coefficient Q_{33} along $\langle 110 \rangle$ direction can be determined. (b) The stresses along $[100]$ and $[110]$ directions were applied to $[001]$ poled PMN-0.37PT tetragonal crystals. The coefficient Q_{33} along $\langle 100 \rangle$ and $\langle 110 \rangle$ directions can be obtained. (c) The stress along $[001]$ direction was applied to $[001]$ poled PMN-0.37PT tetragonal crystals. (d) The hydrostatic pressure dependence of inverse dielectric permittivity for $[001]$ poled PMN-0.28PT. The red arrows represent the poling/single domain directions of the crystals. The blue arrows represent the direction of the applied stress. The dash lines are the fitting slope of reciprocal susceptibility χ_{33} vs. stress.

symmetries, detailed information on their calculations is given in the Appendix.

With this method, high temperature and high field (electric field or stress) measurements were not required. The full set of electrostrictive coefficients can be easily determined because the full set of piezoelectric coefficients can be derived using conventional approaches, such as resonance, ultrasonic, and the Berlincourt methods.³⁶ For ferroelectric ceramics, reliable information could not be derived using this method because the extrinsic contributions of the piezoelectric and dielectric properties from the domain wall motion (which is a nonlinear phenomenon) are quite high, being 10%–40%. Of particular importance is that the domain walls can be eliminated by poling along the direction of the spontaneous polarization in ferroelectric crystals. Thus, this method was preferred for ferroelectric crystals rather than ceramics.

D. Electrostrictive coefficients determined from the lattice parameters

The spontaneous strain in ferroelectrics can be inferred from the lattice parameters. The Q coefficients can be obtained as the ratio between the spontaneous strain and the square of the spontaneous polarization. Berlincourt and Jaffe provided reliable Q coefficients for BT crystal with this method³⁷

$$Q_{33} = S_3/P_3^2 = 0.0075/0.26^2 = 0.111 \text{ m}^4/\text{C}^2, \quad (11)$$

$$Q_{31} = S_1/P_3^2 = 0.0030/0.26^2 = 0.044 \text{ m}^4/\text{C}^2, \quad (12)$$

where Q_{33} and Q_{31} are the electrostrictive coefficients for the BT crystals (in the standard coordinate system with $4mm$ symmetry), S_3 and S_1 are spontaneous strains, and P_3 is the spontaneous polarization.

Based on this notation, the Q_{ijkl} coefficients for PZT and doped PMN single crystals were determined, where the lattice parameters were measured by powder diffraction (either X-ray or neutron diffraction).^{38–41} The nonlinear phenomena were neglected in this approach as no electric field or stress was applied for this method.

E. Electrostrictive coefficients determined from the dielectric permittivity under a DC-biased electric field

Based on the theoretical Debye model, Pattnaik and Toulouse developed an expression for the dielectric permittivity involving the electrostrictive coefficient M with a cubic symmetry, as given in Eqs. (13) and (14) (Ref. 42)

$$\varepsilon'(\omega) = \frac{\varepsilon_s + \varepsilon_\infty \omega^2 \tau^2}{\omega^2 \tau^2 + 1} - \frac{1}{s_{11}^E} \frac{4E_0^2 M_{13}^2}{\omega^2 \tau^2 + 1} (1 - Y_r - \omega \tau Y_i), \quad (13)$$

$$\varepsilon''(\omega) = \frac{(\varepsilon_s - \varepsilon_\infty) \omega \tau}{\omega^2 \tau^2 + 1} - \frac{1}{s_{11}^E} \frac{4E_0^2 M_{13}^2}{\omega^2 \tau^2 + 1} (\omega \tau - \omega \tau Y_r + Y_i), \quad (14)$$

where $\varepsilon'(\omega)$ and $\varepsilon''(\omega)$ are the real and imaginary dielectric permittivities, respectively, ε_s and ε_∞ are the static and

infinite frequency limits of the permittivities, respectively, ω is the angular frequency, τ is the relaxation time, s_{11}^E is the elastic constant, E_0 is the DC bias field, Y_r and Y_i are proportional to the mechanical strain. Detailed information on the coefficients Y_r and Y_i are given in Ref. 42. The electrostrictive coefficient M_{13} can be extracted using Eqs. (13) and (14).^{42,43} The issue with this method was whether or not a simple Debye model is available for the studied dielectrics.

In this section, the experimental methods for determining the electrostrictive coefficients were surveyed. The methods used to determine the electrostrictive coefficients are summarized in Table I, where the characteristics and issues with each method are presented. It should be noted that the electrostrictive coefficients for ferroelectrics can also be determined using a first-principle approach, where the calculated electrostrictive coefficients for LiNbO₃ and BaTiO₃ crystals were reported to be in good agreement with the measured results.^{44,45}

III. THE ORIGIN OF ELECTROSTRICTION

Electrostriction is present in all crystal symmetries because it is a fourth rank polar tensor. Electrostriction is a measure of the polarization induced by ions shifting away from their natural equilibrium positions, giving rise to variations in the lattice parameters (strain). In centrosymmetric crystals, the induced shifts of equivalent ions almost cancel each other out, while the difference in the shifts because of potential anharmonicity generates strain.³ The typical potential of an ion-pair is shown in Fig. 9, where the energy required to compress the ion-pair (U_C) is higher than the energy required to extend the ion pair (U_E).^{46,47} Based on the potential characteristics, the relative displacement between positive and negative ions (polarization) is prone to occur via extension of the lattice instead of compression, as shown in Fig. 10. As a consequence, the longitudinal electrostrictive coefficient Q_{33} is generally positive for ionic crystals.⁴⁸

A quantitative analysis on the above phenomenon, proposed by Uchino *et al.*,⁴⁹ is presented in this section. The potential energy of the ion pair is the simplest rigid ion model with +q and −q ions and can be written as

$$\Delta U = U(r) - U(r_0) = f(r - r_0)^2 - g(r - r_0)^3, \quad (15)$$

where r is the distance between a cation and its nearest-neighbor anion and r_0 is the equilibrium position. $U(r)$ and $U(r_0)$ are the potentials for the nearest neighbors separated by distances of r and r_0 , respectively. The first and second terms in the energy potential are the harmonic and anharmonic components, respectively, where the high order terms were ignored. The coefficients f and g are associated with the crystal structure and the characteristics of the ions (charge and radius). Under an electric field, the average induced strain $\langle x_1 \rangle$ and polarization P_1 can be calculated using Boltzmann distribution

$$\langle x_1 \rangle = (3gq^2/4f^3r_0)E_1^2, \quad (16)$$

$$P_1 = (q^2/4fr_0^3)E_1, \quad (17)$$

TABLE I. The characteristics of various methods for electrostrictive coefficients determination.

Methods	Advantages	Issues	Preferable materials	Examples
Measured by strain-polarization/electric field	The most common method, including the detail strain-field information	Domain switching can affect the value of electrostrictive coefficients	Materials with high dielectric constant or high elastic compliance constant	Perovskite ferroelectrics, polymers
Measured by dielectric permittivity versus applied stress	A good supplemental to the first method, which is generally used to determine the hydrostatic electrostrictive coefficient Q_h	Nonlinear phenomena, such as depolarization and phase transition, should be avoided upon stress	Materials with low dielectric constant and low elastic compliance constant	Fluorite perovskites, CaF_2
Calculated based on piezoelectric coefficients	Can be used to determine the full Q matrix of ferroelectric crystals	The piezoelectricity of the studied materials should be only from electrostriction	Ferroelectric single crystals with parent phase of centro symmetry	PbTiO_3 , BaTiO_3 , PMN-PT, LiNbO_3 single crystals
Calculated based on lattice parameters	No requirement of high electric field/stress	This method is only available for ferroelectric materials	Ferroelectric materials	BaTiO_3 , PbTiO_3 , PZT
Measured by dielectric permittivity under dc bias electric field	The electrostrictive coefficients can be easily derived from dielectric properties	Dielectrics must obey Debye model	...	/

FIG. 9. Schematic figure of the pair potential in ionic crystal, where r_0 represents the equilibrium distance between positive and negative ions.

where q is the charge of the ions. Consequently, the electrostrictive coefficient Q_{11} is given by

$$Q_{11} = 12gr_0^5/fq^2. \quad (18)$$

It can be seen from Eq. (18) that a high g/f corresponds to a high Q_{11} , where the g/f ratio represents the comparison between the anharmonic and harmonic energy components. The coefficients f and g are both positive; thus, the longitudinal coefficient Q_{11} is also a positive coefficient.

Similar to the electrostrictive effect, Maxwell stress contributes to the strain, which is also proportional to the square of the electric field/polarization. As an electric field is applied to the electrodes on the dielectrics, the electrostatic force resulting from the free charges squeezes or stretches the materials. This electrostatic force is called the Maxwell stress and occurs in all insulators with an electric field applied to the deposited electrodes.⁵⁰ The longitudinal strain for dielectrics induced by a Maxwell stress is given by

$$S_M = -\frac{1}{2}s\varepsilon E^2, \quad (19)$$

where S_M is the longitudinal strain induced by the Maxwell stress, s is the elastic compliance of the material, ε is the dielectric permittivity. The difference between the strains induced by electrostriction and the Maxwell stress is that the former is caused by the potential anharmonicity of the ionic crystal, while the latter originates from free charges on the electrodes. However, in S-E loop measurements, these two

FIG. 10. Rigid model of ionic crystal to illustrate the electrostrictive effect. The lattice parameter variations are given under three potential energy conditions, for the same relative displacement between positive and negative ions (noted as l). (a) original state for crystal with zero polarization; (b) in the case of $U_C > U_E$, l is induced by the extension of lattice; (c) in the case of $U_C < U_E$, l is induced by the compression of lattice; (d) in the case of $U_C = U_E$, l exists without varying the lattice parameter.

contributions are generally mixed with each other. When determining the electrostrictive coefficient Q , if the strain induced by Maxwell stress is not separated from the total strain, the contribution of the Maxwell stress to the apparent electrostrictive coefficients (M_M or Q_M) can be written as follows:

$$M_M = \frac{S_M}{E^2} = -\frac{1}{2} s \varepsilon, \quad (20)$$

$$Q_M = \frac{M_M}{\varepsilon^2} = -\frac{1}{2} \frac{s}{\varepsilon}. \quad (21)$$

It can be seen from Eqs. (20) and (21) that the longitudinal electrostrictive coefficient induced by the Maxwell stress is negative. The contribution of the Maxwell stress is significant in materials with either a large elastic compliance (such as soft polymers) or a low dielectric constant (such as CaF_2) [as expressed in Eq. (21)],¹¹ while it can be ignored in ferroelectric crystals and ceramics.

IV. ELECTROSTRICTION WITH RESPECT TO THE MICROSCOPIC AND MACROSCOPIC CHARACTERISTICS

The values of the electrostrictive coefficients for various dielectrics span many orders of magnitude. The longitudinal

coefficients Q_{33} and Q_{11} for soft elastomers are on the order of $10^4 \text{ m}^4/\text{C}^2$, while those for perovskite ferroelectrics are about 10^{-1} to $10^{-2} \text{ m}^4/\text{C}^2$, as listed in Table II.^{11,37,51–56} The electrostrictive Q coefficients have been analyzed with respect to the microstructures and macroscopic properties of the materials.

In this section, we focus on the hydrostatic electrostrictive coefficients Q_h , because the available Q_h data for various dielectrics were more comprehensive in comparison with other coefficients (such as Q_{11} , Q_{12}).

A. Microscopic characteristics versus the electrostrictive effect

The microscopic characteristics, including the ionic radius, ionic charge, and crystal structure, are believed to be the dominant factors for electrostriction. As listed in Table II, the crystals with similar microscopic characteristics exhibited similar Q values. In the simplest rigid model, the effect of the microscopic characteristics can be symbolized by the coefficients r_0 , f , g , and q in Eq. (18). For crystals with the formulas ABO_3 and ABF_3 , the coefficients r_0 , f , and g were assumed to be of the same order because they have the same perovskite structure. Thus, the difference in the Q values between the ABO_3 and ABF_3 crystals was dominated by the difference in the valences q of the ions. The valence

TABLE II. The electrostrictive coefficients for various types of dielectrics. (The electrostrictive coefficients of crystals are measured in their respective standard coordinate systems.) Unit of Q is m^4/C^2 .

Oxygen perovskite		Q_{11}	Q_{12}	Q_{44}	References
Measured in the coordinate system, whose X, Y, and Z axes are along [100], [010], and [001] directions, respectively	BaTiO_3	0.11	−0.045	0.059	37 and 45
	PbTiO_3	0.09	−0.03	0.034	51
Ilmenite		Q_{33}	Q_{31}	Q_{44}	52 and 53
Measured in the coordinate system, whose X, Y, and Z axes are along $[1\bar{1}0]$, $[112]$, and $[111]$ directions, respectively	LiNbO_3	0.016	−0.003	0.065	52 and 53
	LiTaO_3	0.021	−0.005	0.059	52 and 53
Fluorite structure		Q_{11}	Q_{12}	Q_{44}	11 and 54
Measured in the coordinate system, whose X, Y, and Z axes are along [100], [010], and [001] directions, respectively	CaF_2	−0.48	−0.48	1.99	11 and 54
	BaF_2	−0.33	−0.29	1.46	11 and 54
	SrF_2	−0.33	−0.39	1.90	11 and 54
Fluoride perovskites		Q_{11}	Q_h		55
Measured in the coordinate system, whose X, Y, and Z axes are along [100], [010], and [001] directions, respectively	KMnF_3	0.51	0.22		55
	KMgF_3	...	0.24		55
	KZnF_3	...	0.28		55
Sodium chloride structure		Q_{11}	Q_h		49 and 56
	LiF	0.57	0.32		49 and 56
	NaF	...	0.46		49 and 56
	NaCl	...	1.44		49 and 56
PVDF		Q_{11}	Q_h		
	PVDF	−12 ^a	−2.4		11
	P(VDF-TrFE)	−13 ^a	−2.5		8
Elastomers		Q_{11}	Q_h		
	Polyurethane	−1100 ^a	−850		14
	fluoroelastomer	−6200 ^a	...		14

^aThe Q data for polymers are calculated by equation $Q_{11} = S/P^2$, which is the apparent electrostrictive coefficient including the contribution of Maxwell stress.¹⁴

TABLE III. The hydrostatic electrostrictive coefficients and Curie constant for perovskite materials. Unit of Q_h is m^4/C^2 , unit of C is 10^5 K , and unit of $Q_h C$ is $10^3 \text{ m}^4/\text{K}/\text{C}^2$.

Polar type	Order type	Materials	Q_h	C	$Q_h C$	References
Ferroelectric	Order	BaTiO ₃	0.02	1.5	3.0	37
		PbTiO ₃	0.022	1.7	3.7	51
		SrTiO ₃	0.047	0.77	3.6	62
		KTaO ₃	0.052	0.5	2.6	63
Relaxor	Partially order	Pb(Sc _{1/2} Ta _{1/2})O	0.0083	3.5	2.9	64
	Disorder	PMN	0.006	4.7	2.8	2
		PZN	0.0066	4.7	3.1	65
Antiferro	Order	PbZrO ₃	0.02	1.6	3.2	66
		Pb(Mg _{1/2} W _{1/2})O ₃	0.062	0.42	2.6	67
Nonpolar	Order	BaZrO ₃	0.023			7
	Disorder	(K _{3/4} Bi _{1/4})(Zn _{1/6} Nb _{5/6})O ₃	0.0055			7
		0.856SrTiO ₃ -0.144Bi _{2/3} TiO ₃	0.013			7
		K _{0.5} Na _{0.5} NbO ₃ -SrTiO ₃	0.004–0.007			79

ratio between F^- and O^{2-} was 1:2. Thus, the electrostrictive coefficient for ABF_3 was expected to be about four times larger than that for ABO_3 , which is in good agreement with the measured results listed in Table II. Sundar and Newnham presented detailed expressions for the coefficients f and g according to the Born-Mayer potential with which the electrostrictive coefficient Q was accurately calculated for a LiF crystal giving the value of $0.53 \text{ m}^4/\text{C}^2$, which is consistent with the experimental result.⁵⁷

The effects of the microscopic characteristics on the electrostrictive coefficient Q were further demonstrated with the degree order of the B-site cations in perovskite materials. Table III shows that the magnitude of the electrostrictive coefficient strongly depends on the level of order-disorder in the B-site cation arrangement. It was concluded that the electrostrictive coefficient Q increased with the order level of the B-site cations, from disordered to partially ordered, and then to ordered structures. A schematic crystallographic model, proposed by Uchino, can be used to explain this phenomenon (Fig. 11).³ In this model, a large “rattling” space was expected for the smaller B-site cations (B2) in the disordered structures, because the larger B-site cations (B1) prop open the lattice framework. Meanwhile, less “rattling” space was expected in the ordered arrangement where the neighboring oxygen atoms were densely packed around the smaller B ions (B2). When an electric field was applied to the disordered perovskites, the B2 cations with a large rattling space could easily shift without distorting the octahedron framework. Therefore, a larger polarization and lower strains were expected for unit magnitude of the electric field, resulting in smaller electrostrictive coefficients and larger dielectric permittivities. On the contrary, in the ordered perovskites with a very small rattling space, the B2 ions could not move without distorting the octahedron, leading to a smaller dielectric permittivity and larger electrostrictive coefficients.

To obtain accurate electrostrictive coefficients from the microscopic characteristics, more complicated models have been proposed.^{58–62} Though microscopic characteristics are the dominant factor for the Q values, the relationship between the electrostriction and macroscopic properties, such as the

dielectric properties, elastic properties, and thermal expansion, were also established for evaluation of the electrostriction.

B. Macroscopic characteristics versus the electrostrictive effect

1. Dielectric and elastic responses versus the electrostrictive effect

Figure 12 shows $\log(Q_h)$ as a function of $\log(s/\epsilon)$ for various materials, including ceramics and polymers, where a linear relationship was observed, demonstrating that the electrostrictive coefficient Q_h was proportional to s/ϵ . Using a simple atomistic model, Newnham *et al.*^{1,11} proposed a relationship between dielectric/elastic and the electrostrictive

FIG. 11. A tentative crystallographic model, showing order and disorder structures in perovskite crystals. (a) The condition of B-site cations ordered; (b) the condition of B-site cations disordered; (c) the projection of oxygen-octahedron, where the oxygen ions are not plotted in the figure. Reprinted with permission from K. Uchino, S. Nomura, L. E. Cross, R. E. Newnham, and S. J. Jang, *J. Mater. Sci.* **16**, 569 (1981). Copyright 1981 Springer.³

FIG. 12. Hydrostatic electrostrictive coefficient Q_h as a function of the ratio of elastic compliance to dielectric permittivity for dielectrics with large elastic compliance or small dielectric constant. Reprinted with permission from R. E. Newnham, V. Sundar, R. Yimnirun, J. Su, and Q. M. Zhang, *J. Phys. Chem. B* **101**, 10141 (1997). Copyright 1997 American Chemical Society.¹¹

effects. As an electric field is applied, the cations and anions in a crystal structure are displaced in opposite directions by Δr . This displacement is responsible for the electric polarization, dielectric permittivity, and the electrostrictive strain. To the first approximation,^{1,11} the electrostrictive coefficient is written as

$$Q = \frac{x}{P^2} \sim \frac{\Delta r}{(\Delta r)^2} = \frac{1}{\Delta r} \sim \frac{1}{\varepsilon}, \quad (22)$$

where ε is the dielectric permittivity, x is the strain, and P is the polarization. For a certain electric field, a larger Δr corresponds to a larger ε .

The electrostrictive coefficients were also closely associated with the elastic compliance s . Through the converse effect, electrostriction is proportional to the change in the inverse dielectric permittivity χ with stress X , which is expressed as

$$Q \sim \frac{\Delta\chi}{X} \sim \frac{x}{(x/s)} = s, \quad (23)$$

where Q is the electrostrictive coefficient, $\Delta\chi$ is the variation of χ on the stress X , and x is the strain on the stress X . To the first approximation, $\Delta\chi$ is proportional to the relative variations in the lattice parameters.

Combining Eqs. (22) and (23), the electrostrictive coefficient Q is thought to be proportional to s/ε . For materials with a similar elasticity, the dielectric permittivity can be used to evaluate the level of the electrostrictive effect. Figure 13 illustrates Q_h as a function of the dielectric constant for perovskite materials, where $\log(Q_h)$ follows a linear relationship against $\log(\varepsilon)$, as the elastic constants are of the same order for these materials.

For ferroelectric-related materials, the Curie-Weiss constant C can be used to evaluate the level of the electrostrictive coefficients, because the dielectric permittivity is sensitive to temperature and phase transition points. According to thermodynamic analysis, the product of the electrostrictive

FIG. 13. Hydrostatic electrostrictive coefficient Q_h as a function of the dielectric constant in perovskite materials. Reprinted with permission from R. E. Newnham, V. Sundar, R. Yimnirun, J. Su, and Q. M. Zhang, *J. Phys. Chem. B* **101**, 10141 (1997). Copyright 1997 American Chemical Society.¹¹

coefficient Q_h and the Curie-Weiss constant C was constant for all perovskite ferroelectrics.³ Table III gives the experimental data for $Q_h C$, including ferroelectrics, relaxors, and antiferroelectrics, where $Q_h C$ was $(3.1 \pm 0.5) \times 10^3 \text{ m}^4 \text{K/C}^2$ for perovskite ferroelectric materials.^{2,7,37,51,63-68}

2. Thermal expansion versus the electrostrictive effect

The electrostriction and thermal expansion originate from similar mechanisms (i.e., potential anharmonicity), as such the thermal expansion and electrostrictive coefficients are thought to be interrelated.³ Based on the similar manner in deducing the electrostrictive coefficients (Sec. III), the thermal expansion can be written as⁴⁷

$$\alpha = \frac{3gk_B}{4f^2r_0}, \quad (24)$$

where k_B is Boltzmann's constant and r_0 is the distance between a cation and its nearest-neighbor anion at equilibrium. f and g are the harmonic and anharmonic components, respectively. Similar to electrostriction, the thermal expansion coefficient was zero when the anharmonic effect was ignored ($g = 0$).

The thermal expansion coefficient α against the hydrostatic electrostrictive coefficient Q_h for various dielectrics with cubic symmetry is plotted in Fig. 14, based on the reported results.³ From this figure, the empirical relation can be written as $\alpha = 4.2 \times 10^{-5} Q_h^{0.5}$, which can be used to evaluate the electrostrictive effect from the thermal expansion coefficient.

In this section, the relationships between electrostriction and the macroscopic characteristics were reviewed for dielectric materials. Although the relationships could be used to evaluate the electrostrictive effect in dielectrics, they did not give accurate results. Some important factors were not considered, such as the crystal anisotropy, boundary conditions, and phase transitions. For ferroelectric materials, the effects of the domain walls, domain configurations,⁶⁹⁻⁷³ and

FIG. 14. Hydrostatic electrostrictive coefficient Q_h with respect to thermal expansion coefficient for various dielectrics with cubic symmetry. Reprinted with permission from K. Uchino, S. Nomura, L. E. Cross, R. E. Newnham, and S. J. Jang, *J. Mater. Sci.* **16**, 569 (1981). Copyright 1981 Springer.³

the poling conditions⁷⁴ on the electrostriction should also be considered.

V. ELECTROSTRICTION IN PEROVSKITE FERROELECTRICS

Extensive investigations on the electromechanical properties of ferroelectric single crystals, ceramics, and thin films have been a focus because their electric field-induced strains and piezoelectricity are much higher in comparison with other non-ferroelectric counterparts. In this section, the electrostrictive effects of perovskite ferroelectrics are discussed.

The reported electrostrictive coefficients for various perovskite ferroelectrics are listed in Table IV,^{3,75–84} including

the data for single crystals and ceramics. The properties of single crystals are very important for materials exploration, as they allow for easy interpretation of the polycrystalline ceramic properties. On the other hand, some crystals are difficult to be grown; their ceramic counterparts can be used to evaluate the single crystal properties. The difference in the electrostrictive effect between single crystals and polycrystalline ceramics is discussed here.

For perovskite ferroelectric materials, the longitudinal electrostrictive coefficients Q_{33} of the polycrystalline ceramics and thin films are generally much smaller than those of $\langle 100 \rangle$ oriented single crystals. This phenomenon can be attributed to the following two factors. First, the strong anisotropy of electrostriction presents in perovskite crystals, which will be discussed in Sec. VC. Second, it is difficult to eliminate the contribution of the domain wall motion in polycrystalline ceramics during the electrostriction measurements. As a result, the measured data for the polycrystalline materials include contributions from the domain wall motion and grain orientation. In addition, for ferroelectric thin films, the values of the electrostrictive coefficients were expected to be further affected by substrate clamping, which generally decreased the Q coefficients.⁸⁵ It should be noted that when compared with the electrostrictive coefficient Q_{33} , the hydrostatic coefficient Q_h was independent of the orientation for perovskite ferroelectric materials.⁸⁶ Meanwhile, Q_h was generally determined by measuring the inverse of the dielectric permittivity under hydrostatic pressure, where the influence of the domain wall was quite small when compared with the high field measurements. Thus, the hydrostatic electrostrictive coefficient Q_h of the polycrystalline ceramics was found to be the same to that of the single crystals.

TABLE IV. The electrostrictive coefficients for perovskite crystals and ceramics; the coordinate system for crystals is the standard coordinate of cubic phase (X: [100], Y: [010], Z: [001]).

Crystals	Electrostrictive coefficients (m^4/C^2)				References
	$Q_{11}^C = Q_{1111}^C$	$Q_{12}^C = Q_{1122}^C$	$Q_{44}^C = 2Q_{1212}^C$	$\frac{Q_{11}^C - Q_{12}^C}{Q_{44}^C}$	
PMN-0.28PT	0.055	-0.024	0.021	3.8	26
PMN-0.32PT	0.056	-0.022	0.019	4.1	26
PMN-0.37PT	0.056	-0.024	0.018	4.4	26
PbTiO ₃	0.089	-0.030	0.034	3.2	51
BaTiO ₃	0.110	-0.045	0.059	2.6	37
Pb(Yb _{1/2} Nb _{1/2})O ₃	0.082				77
Pb(Zn _{1/3} Nb _{2/3})O ₃	0.063	-0.25	0.24	3.7	This work
Pb(Mg _{1/3} Nb _{2/3})O ₃	0.027	-0.01	0.01	3.7	3 and 84
(Bi _{1/2} Na _{1/2}) _{1-x} Ba _x Zr _y Ti _{1-y} O ₃	0.023–0.04				78
Ceramics					
PbZr _{0.52} Ti _{0.48} O ₃		-0.007~ -0.016			75
La doped 0.65PbZrO ₃ -0.35PbTiO ₃ (molar percentage of La is 7%–10%)	0.018–0.022	-0.008~ -0.0012			76
PMN-0.1PT	/	-0.009			4
Bi _{0.5} Na _{0.5} TiO ₃ -K _{0.5} Na _{0.5} NbO ₃	0.015–0.018				80
Bi _{0.5} Na _{0.5} TiO ₃ -BaTiO ₃ -K _{0.5} Na _{0.5} NbO ₃	0.021–0.026				81
Bi _{0.5} Na _{0.5} TiO ₃ -BaTiO ₃	0.022				82
Bi _{1/2} (Na _{0.82} K _{0.18}) _{1/2} TiO ₃	0.023				83
K _{0.5} Na _{0.5} NbO ₃ -SrTiO ₃	0.004–0.007				79

FIG. 15. The temperature dependence of electrostrictive coefficient Q of $\text{Bi}_{0.5}(\text{Na}_{0.82}\text{K}_{0.18})_{0.5}\text{TiO}_3$ and PZT ceramics. After Refs. 83 and 87.

In the following sections, the effects of the ferroelectric phase transition and crystal orientation on electrostrictive coefficients Q are evaluated. The electrostrictive coefficients Q are discussed for perovskite ferroelectrics with respect to electromechanical properties, such as the electric field-induced strain and piezoelectric coefficients, in order to find alternative ways to enhance the piezoelectric activity.

A. Electrostrictive effect versus ferroelectric phase transitions

The phase transition point in perovskite ferroelectrics, around where the dielectric and piezoelectric responses generally show peak values, has been extensively studied over the last 70 years. In this section, the electrostrictive coefficients Q of perovskite ferroelectrics are discussed with respect to the phase transition points (induced by temperature or composition).

1. Polymorphic phase transition (PPT, phase transitions induced by temperature)

For typical ferroelectrics, such as BaTiO_3 , PbTiO_3 , and LiNbO_3 , the electrostrictive coefficients Q are

temperature-independent. This notation is generally accepted based on thermodynamic analysis.⁵¹ Meanwhile, the Q coefficients calculated from first principles at 0 K were consistent with the results measured at room temperature,^{44,45} again revealing that the effect of temperature on the Q coefficients is minimal for classical ferroelectrics. From the experimental aspect, the temperature-independent electrostrictive coefficients Q were also observed in PZT and $\text{Bi}_{0.5}(\text{Na}_{0.82}\text{K}_{0.18})_{0.5}\text{TiO}_3$ ferroelectric systems, as shown in Fig. 15.^{83,87}

To understand the temperature dependence of the electrostrictive behavior in relaxor/relaxor-PT single crystals, related parameters, including the piezoelectric coefficient, dielectric constant, spontaneous polarization, and electrostrictive coefficients, as a function of the temperature were investigated for single-domain PMN- x PT crystals, as shown in Fig. 16. The large variations in the dielectric and piezoelectric coefficients are closely associated with the PPT, where the increase in the dielectric and piezoelectric properties for PMN-0.28PT and PMN-0.32PT crystals with increasing temperature was attributed to the crystals approaching a PPT (T_{R-T} and T_{O-T} are 95 °C and 80 °C, respectively), while the decrease in the dielectric and piezoelectric responses for PMN-0.37PT occurred because the PPT of PMN-0.37PT was below room temperature (~ -45 °C).²¹ The spontaneous polarization decreased with increasing temperature, caused by the pyroelectric effect.⁸⁸ Of particular significance is that the electrostrictive coefficients of the PMN- x PT crystals were insensitive to temperature and PPT, regardless of the strong temperature dependence of the piezoelectric/dielectric properties. The temperature-independent electrostrictive coefficients Q_{11} and Q_{12} were also observed in PMN crystals, as shown in Fig. 17.

It should be noted that the reported data for the PMN, PMN-PT, and $\text{Bi}_{0.5}(\text{Na}_{0.82}\text{K}_{0.18})_{0.5}\text{TiO}_3$ systems were below the T_C . At temperatures above T_C (or above the Burns temperature T_B for relaxor ferroelectrics; for PMN and PMN-PT crystals, $T_B \sim 300$ °C²⁹), the electrostrictive coefficient Q_{11} was found to decrease linearly with increasing temperature for BaTiO_3 and tin modified lead zirconate (PZS) crystals (Fig. 18),^{89,90} which can be explained using the phenomenological theory.⁹¹

FIG. 16. The temperature-dependent properties, (a) piezoelectric coefficient d_{15} , (b) dielectric constant ϵ_{11} , (c) spontaneous polarization P_s , and (d) electrostrictive coefficient Q_{1313} for single domain PMN-0.28PT, PMN-0.32PT, and PMN-0.37PT crystals. The coefficients of rhombohedral, orthorhombic, and tetragonal crystals were measured in the standard coordinates of $3m$, $mm2$, and $4mm$ symmetries, respectively. The PPTs of PMN-0.28PT, PMN-0.32PT, and PMN-0.37PT crystals are 93, 80, and -45 °C, respectively. Reprinted with permission from Appl. Phys. Lett. **102**, 152910 (2013). Copyright 2013 AIP Publishing LLC.²⁶

FIG. 17. The temperature dependence of electrostrictive coefficient Q of PMN crystals. Reprinted with permission from J. Appl. Phys. **51**, 1142 (1980). Copyright 1980 AIP Publishing LLC.²

2. Morphotropic phase boundary (MPB, phase transitions induced by composition)

The MPB is an important characteristic for many perovskite ferroelectric solid solutions as it accounts for the enhanced dielectric, elastic, and piezoelectric properties. In this section, the effect of MPB on electrostriction is surveyed for perovskite ferroelectrics.

As listed in Table IV, the Q coefficients were found to have similar values for compositions around the MPBs in PMN-PT and $\text{Bi}_{0.5}\text{Na}_{0.5}\text{TiO}_3$ - BaTiO_3 - $\text{K}_{0.5}\text{Na}_{0.5}\text{NbO}_3$ systems. However, Fig. 19 outlines the Q coefficients for the PZ- x PT crystals, exhibiting a slight increase around the MPB composition.⁵¹ This was thought to be associated with the domain wall motion or phase transition during the electrostrictive measurements, because the Q values for the PZT crystals were inferred from the measurements on the polycrystalline ceramics.

The electrostrictive coefficients ($Q_{11}^C - Q_{12}^C$)⁹² of [001] poled PMN- x PT and PZN- x PT crystals are derived from the data in Refs. 2, 18, 52, and 93–97 and plotted in Fig. 20. The electrostrictive coefficients of the relaxor-PT crystals generally increase with increasing PT content, with no abnormal phenomenon observed around the MPB. Enhancement of the electrostrictive coefficient ($Q_{11}^C - Q_{12}^C$) with increasing PT content was attributed to the enhancement in the ordering degree of the relaxor-PT crystals by increasing the PT

FIG. 19. The composition dependence of Q coefficients for PZ- x PT crystals, where x represents the PT concentration.

content, as discussed in Sec. IV. Vikhnin *et al.* theoretically explained the increase in the electrostrictive coefficient Q as a function of the PT content by considering the quasi-local Ti-O stretching mode in PMN-PT solid solutions.⁶¹ It should be noted that for PZN- x PT crystals with $x=0.08$ and 0.12 , the electrostriction was comparable to that of the PT crystals, while the electrostrictive coefficients ($Q_{11}^C - Q_{12}^C$) for the PMN- x PT crystals were much lower than those of PT crystals, even in the composition range of $x=0.26$ – 0.42 . This result revealed that the B-site ordering degree for the PZN- x PT crystals was higher than that for the PMN- x PT crystals at the MPB composition.

Overall, the influences of the PPT and MPB on the Q electrostrictive coefficients were minimal in comparison with the effects on the dielectric and piezoelectric properties in perovskite ferroelectrics. This demonstrates that the magnitude of the electrostrictive coefficient does not strongly depend on various phases (ferroelectric, antiferroelectric, or non-polar phases) and phase transitions. For perovskite ferroelectrics, the phase transition (ferroelectric, antiferroelectric, paraelectric) is accompanied by atomic displacements that are dominated by motion of the B cations in the oxygen octahedron network.³² From the respect of crystal structure, the difference between the paraelectric, antiferroelectric, and various ferroelectric phases is reflected in the displacement of ions, including the direction and magnitude of the displacement. However, it is important to note that the

FIG. 18. The temperature dependence of electrostrictive coefficient Q for (a) BT and (b) PZ and PZS single crystals at the temperature above their respective T_C s. (a) Reprinted with permission from W. Pan, Q. Zhang, A. S. Bhalla, and L. E. Cross, J. Am. Ceram. Soc. **71**, C-302 (1998). Copyright 2005 John Wiley and Sons.⁹⁰ (b) Reprinted with permission from I. Jankowska-Sumara, K. Roleder, A. Majchrowski, and J. Zmija, J. Adv. Dielectr. **1**, 223 (2011). Copyright 2011 World Scientific Publishing Company.⁸⁹

FIG. 20. Composition dependence of electrostrictive coefficient for relaxor-PT crystals. The data of PMN, PZN, PZN-0.045PT, PZN-0.07PT, PZN-0.08PT, PZN-0.12PT, PMN-0.42PT, and PT crystals are from Refs. 2, 18, 51, 87–91.

displacements are relatively small in perovskite structures, being $<5\%$ of the lattice parameter, revealing that the ion-pair potential energy and lattice parameters [the parameters in Eq. (18)] were not greatly affected by these small displacements. As a result, electrostriction in perovskite crystals is not sensitive to the ferroelectric phases and phase transitions.

B. Orientation dependence of electrostriction

The orientation dependence of the electrostrictive coefficients Q_{33}^* ⁹⁸ for BT and PMN-0.28PT crystals were calculated by the axis transformation using the data in Table IV,

as shown in Fig. 21. The maximum electrostrictive coefficient Q_{33}^* was along the $\langle 100 \rangle$ direction, while the moderate and minimum values were along the $\langle 110 \rangle$ and $\langle 111 \rangle$ directions, respectively. Similar anisotropic behavior was observed in PMN-0.32PT, PMN-0.37PT, and other perovskite crystals, due to the fact that the anisotropic factors $(Q_{11}^C - Q_{12}^C)/Q_{44}^C$ is much larger than 1 for those crystals, as listed in Table IV (Q_{33}^* will be an isotropic coefficient if $(Q_{11}^C - Q_{12}^C)/Q_{44}^C = 1$). Similar anisotropic behavior was also reported in other ionic crystals possessing oxygen octahedral structures (LiNbO_3 , LiTaO_3 , KNbO_3 , and $\text{Ba}_2\text{NaNb}_5\text{O}_{15}$ crystals), as listed in Table V.⁵⁴ As demonstrated in Ref. 53, the anisotropy of the electrostriction in perovskite crystals led us to believe that it is inherently associated with the oxygen octahedra.

Figure 22 shows the variation in the oxygen octahedral structure as polarization appeared along different crystallographic directions. When a B-site cation moves along the $[001]$ direction, an oxygen anion O_1 will be “pushed” upward to release the energy that originated from compressing the distance of B- O_1 , as shown in Fig. 22(b). Consequently, the lattice parameter along the $[001]$ direction is elongated by d . The strain along the $[001]$ direction can be expressed as d/a . Figure 22(c) shows the scenario where a B-site cation moves along the $[110]$ direction. In this case, the oxygen O_3 and O_4 anions will move along the $[110]$ or $[\bar{1}\bar{1}0]$ directions to release the B- O_3 and B- O_4 pair potential because the direction of B-O bond ($\langle 100 \rangle$) is not parallel to the $[110]$ direction. It should be noted that the electrostrictive coefficient Q_{33}^* along the $[110]$ direction is reduced by the motion of the O_3/O_4 ions along the $[\bar{1}\bar{1}0]/[\bar{1}\bar{1}0]$ directions, because the $[\bar{1}\bar{1}0]/[\bar{1}\bar{1}0]$

FIG. 21. The orientation dependence of electrostrictive coefficient Q_{33}^* for BT and PMN-0.28PT crystals. (a) Three-dimensional figure for PMN-0.28PT, (b) cross section of $(1\bar{1}0)$ plane for PMN-0.28PT, (c) three-dimensional figure for BT crystal, (d) cross section of $(1\bar{1}0)$ plane.

TABLE V. Q^p are electrostrictive coefficients normalized to those of the perovskite-oxide structure. Data are from Ref. 53.

Crystals	Electrostrictive coefficients (m^4/C^2)			
	Q_{11}^p	Q_{12}^p	Q_{44}^p	$\frac{Q_{11}^p - Q_{12}^p}{Q_{44}^p}$
$\text{Ba}_2\text{NaNb}_5\text{O}_{15}$	0.11	-0.019	0.029	4.4
LiNbO_3	0.096	-0.039	0.024	5.6
LiTaO_3	0.085	-0.033	0.033	3.6

directions are perpendicular to the $[110]$ direction. Analogous to the $[110]$ direction, a similar scenario occurs for the $[111]$ direction, as shown in Fig. 22(d). As a B-site cation moves along the $[111]$ direction, the oxygen ions can move along the directions perpendicular to $[111]$ direction to release the B-O pair potential, which mitigates the Q_{33}^* along the $[111]$ direction. The difference between the $[111]$ and $[110]$ directions is that in the former, the oxygen ions are easier to move along the perpendicular direction to release the compression energy. This is because the angle between the $[111]$ and B-O chain directions is 54° , which is larger than the angle between the $[110]$ and B-O bond directions (45°). Based on this approach, electrostrictive anisotropy of perovskite crystals has been explained qualitatively, which is related to the oxygen octahedral structure. The maximum electrostrictive coefficient Q_{33}^* was along the $\langle 100 \rangle$ direction because the B-O chains align along the $\langle 100 \rangle$ direction. Using the same approach, the electrostrictive anisotropy for specific crystals can be explained. For example, for fluoride perovskite crystals, the maximum longitudinal electrostrictive coefficient Q_{33}^* is along the $\langle 100 \rangle$ directions, as the B-F chains align along this direction; while maximum Q_{33}^* is along the $\langle 111 \rangle$ directions for the fluorite crystal CaF_2 , as the

Ca-F chains align along the $\langle 111 \rangle$ directions, as shown in Fig. 23.

In addition to the longitudinal electrostrictive coefficient Q_{33}^* , the other electrostrictive coefficients for perovskite crystals also showed strong anisotropic behavior. Two examples are: (a) In the coordinate system shown in Fig. 24(a), the Q_{32}^* coefficient was positive, indicating that the extensions occurred simultaneously parallel and perpendicular to the applied electric field⁸⁶ and (b) the maximum shear coefficient for the perovskite crystal is presented in the coordinate system shown in Fig. 24(b), being equal to $Q_{1313}^* = \frac{1}{2}(Q_{11}^p - Q_{12}^p)$.

C. Electrostrictive coefficient Q versus the electromechanical properties

1. Electrostrictive coefficient Q versus the electric field-induced strain

In general, an electric field-induced strain can be written as

$$S = g \cdot P(E) + Q \cdot P^2(E) + \dots, \quad (25)$$

where the first and second terms represent the piezoelectric and electrostrictive strains, respectively, $P(E)$ is the electric field-induced polarization and g is the piezoelectric voltage coefficient. The strains related to the high order of P were ignored in Eq. (25). For piezoelectric crystals without ferroelectricity, the piezoelectric strain is usually much higher than the electrostrictive strain, such as in quartz crystals. On the contrary, based on the phenomenological theory, the strain in ferroelectrics with centrosymmetric parent phases is induced by the electrostriction only.³² These ferroelectrics include LiNbO_3 , BaTiO_3 , PbTiO_3 , KNbO_3 , and other related materials. Thus, Eq. (25) can be expressed as Eq. (26) for these materials

$$S = QP^2(E) \sim Q\varepsilon^2 E^2, \quad (26)$$

where ε is the dielectric permittivity. In Eq. (26), the anisotropy and nonlinear properties for the dielectric response were not considered. Based on Eq. (26), the figure of merit used to evaluate the level of strain induced by a certain electric field is $Q\varepsilon^2$. It was observed that a large Q coefficient does not necessarily give rise to large electric field-induced strains, because a high Q coefficient generally corresponds to a low dielectric permittivity, as discussed in Sec IV B 1 ($Q \propto 1/\varepsilon$). It was reported that the Q coefficient in the relaxor ferroelectric PMN was about one fifth that of a typical ferroelectric BT, while the dielectric permittivity of PMN was 5–10 times higher than that in BT. Thus, PMN exhibited a superior electric field-induced strain when compared with BaTiO_3 . In addition, perovskite materials generally showed a larger electric field-induced strain because the dielectric permittivity for perovskites is significantly higher than other ionic crystals.

It should be noted that domain switching can also be used to enhance the electric field-induced strain in ferroelectric crystals. Interesting results were reported for $[001]$ oriented BT crystals with Mn dopants or preloaded stress in

FIG. 22. The deformation of oxygen-octahedral structure with different polarization directions. (a) Zero polarization; (b) polarization along $[001]$ direction; (c) polarization along $[110]$ direction; (d) polarization along $[111]$ direction. The red arrows for oxygen ions indicate that the oxygen ions move along the polarization direction. The purple arrows for oxygen ions indicate that oxygen ions move along the direction perpendicular to the polarization direction.

FIG. 23. The relationship of crystal structure and orientation dependent electrostriction for fluoride crystal. (a) The structure of fluoride crystal; (b) the orientation dependence of Q_{33}^* for CaF_2 . Input data are from Ref. 11.

which $\sim 1\%$ strain was induced with an electric field.^{99–101} With a decrease in the applied electric field, Mn dopants or preloaded stress made the domains switch back to the directions that were perpendicular to the applied electric field, as shown in Fig. 25. Theoretically, the maximum strain induced by domain switching in [001] oriented tetragonal crystals can be expressed as $S_3 = (Q_{11} - Q_{12})P_s^2$ (as depicted in Fig. 25), which is much larger than that induced by lattice deformation. Through domain switching, the level of maximum strain is only related to the electrostrictive coefficients and the spontaneous polarization and not to the dielectric permittivity. However, the strain induced by domain switching is generally accompanied by a large hysteresis, limiting its potential application in electromechanical devices.

2. Electrostrictive coefficient Q versus piezoelectric activity

Analogous to the electric field-induced strain, the intrinsic piezoelectricity of ferroelectrics with centrosymmetry parent phases comes from the electrostrictive effect. Compared with the extrinsic contribution (domain wall motion), the electrostrictive contribution showed low hysteresis and high stability with respect to the frequency and electric field.^{69,70,102} In addition, the sign of the piezoelectric coefficient d can also be determined by the sign of the electrostrictive coefficient Q . For example, the longitudinal piezoelectric coefficient d_{33} has a positive value for ferroelectric crystals and ceramics, whereas d_{33} has a negative value for ferroelectric polymers,

FIG. 24. Schematic of coordinate system and corresponding polarization and electrostrictive strains for perovskite crystals. (a) Positive Q_{3322} coefficient; (b) maximum Q_{1313} coefficient.

because the electrostrictive coefficient was positive for ionic crystals and negative for polymers. Furthermore, the anisotropy of the electrostriction plays an important role in the piezoelectric anisotropy in ferroelectric crystals. To illustrate this scenario, the detailed relationship between the piezoelectric and electrostrictive coefficients are given for relaxor-PT crystals, whose parent phase and symmetry were cubic and $m\bar{3}m$, respectively.

According to Eq. (2) and the transformation of the coordinate system, the piezoelectric coefficient and dielectric permittivity for [001] poled rhombohedral crystals can be written as

$$\epsilon_{33}^{[001]} = \frac{1}{3}(\epsilon_{33}^R + 2\epsilon_{11}^R), \quad (27)$$

$$\begin{aligned} d_{33}^{[001]} &= 2P_s^C(\epsilon_{33}^C Q_{33}^C + 2\epsilon_{31}^C Q_{31}^C) \\ &= \frac{2\sqrt{3}}{3}P_s^R \left[\left(\frac{2}{3}\epsilon_{11}^R + \frac{1}{3}\epsilon_{33}^R \right) Q_{33}^C + 2 \left(\frac{2}{3}\epsilon_{33}^R - \frac{1}{3}\epsilon_{11}^R \right) Q_{31}^C \right], \end{aligned} \quad (28)$$

where the symbols R and C indicate the rhombohedral $3m$ and cubic $m\bar{3}m$ coordinate systems in which the property coefficients were measured (see details in the Appendix). An important characteristic in the relaxor-PT crystals is that the transverse dielectric permittivity ϵ_{11} is much higher than the

FIG. 25. Schematic for [001] oriented tetragonal BT crystal under electric field and preload stress. The dashed arrows represent the polarization directions. P_s is the spontaneous polarization, S_1 and S_3 are the spontaneous strain along a and c axes of tetragonal BT crystal, respectively. As shown in this figure, domains are aligned along [001] direction with applying E-field of [001] direction, while the domains will switch back to the four possible directions as the E-field removed, where the polarizations are perpendicular to the preload stress ([001] direction). For Mn-doped BT crystals, similar domain switching will occur due to the internal bias field.

longitudinal dielectric permittivity ϵ_{33} .²⁰ Thus, Eqs. (27) and (28) can be simplified for relaxor-PT crystals as

$$\epsilon_{33}^{[001]} \approx \frac{2}{3} \epsilon_{11}^R, \quad (29)$$

$$d_{33}^{[001]} \approx \frac{2\sqrt{3}}{3} P_s^R \epsilon_{33}^{[001]} (Q_{33}^C - Q_{31}^C), \quad (30)$$

where $\epsilon_{33}^{[001]}$ is the longitudinal dielectric permittivity for [001] poled rhombohedral crystals, ϵ_{11}^R is the transverse dielectric permittivity measured in the standard coordinate system for rhombohedral $3m$ symmetry (see details in the Appendix), and P_s^R is the spontaneous polarization of the rhombohedral crystals. Based on the same approximation, the piezoelectric coefficient d_{33} of [001] poled orthorhombic relaxor-PT crystals and [111] poled tetragonal relaxor-PT crystals can be written as

$$d_{33}^{[001]} \approx \frac{2\sqrt{2}}{2} P_s^O \epsilon_{33}^{[001]} (Q_{33}^C - Q_{31}^C), \quad (31)$$

$$d_{33}^{[111]} \approx \frac{2\sqrt{3}}{3} P_s^T \epsilon_{33}^{[111]} (Q_{33}^R - Q_{31}^R), \quad (32)$$

where Q_{33}^R and Q_{31}^R are the electrostrictive coefficients measured in the standard coordinate system for a rhombohedral $3m$ symmetry.⁹²

As expressed in Eqs. (30)–(32), the longitudinal piezoelectric response of domain engineered relaxor-PT crystals is proportional to the product of the longitudinal dielectric permittivity ϵ_{33} and the electrostrictive coefficient $(Q_{33} - Q_{31})$. In Eqs. (30)–(32), the coefficient d_{33} was not only attributed to the longitudinal Q_{33} but also to the transverse electrostriction Q_{31} , because the polarization direction changed as the applied electric field deviated from the polar direction for domain engineered crystals. Table VI gives the piezoelectric coefficients, dielectric permittivities, and electrostrictive coefficients for the domain-engineered PMN-xPT crystals.¹⁰³ The piezoelectric coefficients for [001] poled rhombohedral and orthorhombic crystals were found to be much higher than those of [111] poled orthorhombic and tetragonal counterparts, though the latter possessed higher dielectric constants. This phenomenon can be explained by the anisotropy of the electrostriction, where the highest electrostrictive coefficients Q_{33}^* were observed along the $\langle 100 \rangle$ directions in perovskite crystals. Thus, the high longitudinal piezoelectric response in perovskite crystals is expected in the $\langle 100 \rangle$ poled domain-engineered rhombohedral or

orthorhombic crystals, because both the dielectric permittivity and electrostrictive coefficient are enhanced. On the contrary, for $\langle 111 \rangle$ and $\langle 110 \rangle$ poled domain-engineered tetragonal crystals, the dielectric permittivity is enhanced, but the electrostrictive coefficient greatly decreased. As a result, the piezoelectric coefficient in $\langle 111 \rangle$ poled tetragonal crystals doesn't benefit significantly from the engineered domain configuration, since d_{33}^*/d_{33} is much smaller in comparison with their rhombohedral and orthorhombic counterparts, as listed in Table VI.

3. Can piezoelectric activity be improved with electrostriction?

Ferroelectric materials with a perovskite structure, including BT, PZT ceramics, and PMN-PT, PZN-PT, PIN-PMN-PT single crystals, have been extensively studied as they have a high piezoelectricity.^{20,104} At the present time, efforts in increasing the intrinsic piezoelectric activity of ferroelectrics are mainly focused on the dielectric response. To improve the dielectric response, ferroelectric phase transitions (MPB and PPT)^{105–108} and donor dopants are two generally accepted approaches for use in ferroelectric crystals/ceramics.^{109,110} Furthermore, an electron-irradiated method was applied to the poly(vinylidene fluoride-trifluoroethylene) copolymer P(VDF-TrFE) to enhance the dielectric property.⁸ Development over the last 60 years has shown that there is limited room left to further enhance the piezoelectric response in ferroelectrics using these approaches. Meanwhile, it should be noted that the piezoelectricity was enhanced at the cost of the piezoelectric stabilities by these approaches, including the thermal and field (electric field and stress) stabilities.¹⁰³ Section IV B discussed the figure of merit used to evaluate the piezoelectric coefficient d for perovskites, which is the product of the dielectric constant and the electrostrictive coefficient, leading to the conclusion that the piezoelectric response could be improved by enlarging the electrostrictive effect. The importance of this approach has not attracted its deserved attention. One reason is that tuning the electrostrictive coefficients Q is difficult when compared with the dielectric constant, because Q is not sensitive to the phase transformation (PPT or MPB). Second, the electrostrictive coefficient Q increased at the cost of decreased dielectric constant (Eq. (22)), where $\log(Q)$ and $\log(\epsilon/\epsilon_0)$ followed a near-linear relationship, as discussed in Sec. IV B. Figure 26 plots the Q_{33}^* as a function of $\epsilon_{33}^*/\epsilon_0$ and $Q_{33}^*(\epsilon_{33}^*/\epsilon_0)$ for the domain-engineered PMN-xPT crystals, based on the data listed in Table VI, where the factor $Q_{33}^*(\epsilon_{33}^*/\epsilon_0)$ is proportional to the longitudinal piezoelectric

TABLE VI. Electromechanical properties of domain engineered PMN-xPT crystals. d_{33} is the piezoelectric coefficient of single domain crystal along its polar direction. d_{33}^* is the longitudinal piezoelectric coefficient of domain engineered crystals (along their respective nonpolar directions). Data are from Refs. 103 and this work.

Crystals	Phase	Poling direction	$\epsilon_{33}^*/\epsilon_0$	d_{33}^* pC/N	Q_{33}^* m ⁴ /C ²	Q_{31}^* m ⁴ /C ²	d_{33}^*/d_{33}
PMN-0.28PT	Rhombohedral	[001]	5 200	1700	0.055	−0.024	13
PMN-0.32PT	Orthorhombic	[001]	5 500	1800	0.056	−0.022	9
PMN-0.32PT	Orthorhombic	[111]	9 000	700	0.014	−0.004	3.5
PMN-0.37PT	Tetragonal	[111]	10 000	900	0.015	−0.004	2

FIG. 26. Dielectric constant $\epsilon_{33}^*/\epsilon_0$ and $Q_{33}^*\epsilon_{33}^*/\epsilon_0$ as a function of electrostrictive coefficient Q_{33}^* for domain engineered PMN-xPT crystals. Solid circles indicate the experimental data listed in Table VI, while the hollow circles are predicted data. By linear fitting of $\log(Q_{33}^*)$ vs. $\log(\epsilon_{33}^*/\epsilon_0)$, the dielectric constants $\epsilon_{33}^*/\epsilon_0$ and $Q_{33}^*\epsilon_{33}^*/\epsilon_0$ for PMN-PT crystal system were predicted with coefficient Q_{33}^* being 0.09 (typical value of PT crystal) and 0.11 m^4/C^2 (typical value of BT crystal), respectively.

coefficient. It was observed that $Q_{33}^*(\epsilon_{33}^*/\epsilon_0)$ (the piezoelectric response) could be enhanced by increasing the electrostrictive coefficient Q_{33}^* , even the dielectric constant showed a contrary trend. From Fig. 26, the piezoelectric response of PMN-PT crystals was expected to increase by 40%–60%, with the electrostrictive coefficient approaching the values of the classical ferroelectric perovskite crystals, such as BaTiO_3 and PT crystals. The above discussion suggests that the improved piezoelectric activity in domain-engineered relaxor-PT crystals can be realized by enhancing the electrostrictive coefficient. A possible approach to increase the electrostrictive effect in relaxor-PT crystals is to control the degree of ordering for the A/B cations, which can be tuned by varying the charge, mass, and size of A/B site cations. In addition, a thermal annealing process has been reported to benefit the ordering degree in perovskite systems.^{111,112} Of particular significance is that the enhancement of the electrostrictive coefficients does not sacrifice the piezoelectric stability (including thermal and field stability), as the high piezoelectric activity is not induced by the MPB or PPT, which is promising from the application viewpoint.

In this section, improvement in the piezoelectric activity was discussed from the intrinsic aspect. It should be noted that the piezoelectricity of ferroelectrics could be improved from the extrinsic contribution (domain wall motion), which accounts for up to 50% of the piezoelectricity in ferroelectric ceramics. However, the intrinsic contribution, which essentially enhances the piezoelectric activity from one material system to another, is the dominant factor in improving the piezoelectric activity. For example, in perovskite-structured ferroelectrics, the intrinsic contribution exhibits a drastic increase from BaTiO_3 (100 pC/N) to PMN-PT (2000 pC/N) via PZT (500 pC/N). In contrast to the domain wall motion, enhancement in the intrinsic piezoelectricity does not lead to hysteresis in the strain vs electric-field response.¹⁰⁸

VI. CONCLUSIONS AND FUTURE PERSPECTIVES

In this review, the measurement techniques and the origins of electrostriction in ionic crystals were surveyed. The relationship between electrostriction and crystal structure, and the empirical rules for the electrostrictive coefficient Q versus thermal expansion, dielectric constant, and elastic constant were discussed, with emphasis on the perovskite ferroelectrics, because of their high-electrostriction-induced piezoelectric activity.

Electrostriction plays a critical role in the electromechanical properties of ferroelectrics and is worthy of further investigation. Therefore, tuning the electrostrictive coefficient is of particular importance for exploring next-generation high-performance electromechanical materials. In the following, some interesting research topics related to the electrostriction in perovskite materials are proposed: (1) Establish a model to accurately describe electrostriction in ionic crystals, incorporating the anisotropy, defects, ordering degree, and other microscopic characteristics. (2) Explore the maximum value of the electrostrictive coefficient Q for perovskite crystals and other ferroelectric systems. To solve this issue, theoretical calculations such as the first-principle method, which provides consistent data for BT and PT crystals, can be employed. (3) Analyze the effects of the A-site cations on electrostriction for perovskite crystals, from the viewpoint of the order-disorder structures. (4) Investigate the relationship between the electrostriction and domain size/domain wall density for ferroelectrics.

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APPENDIX: THE CALCULATION OF ELECTROSTRICTIVE COEFFICIENT BASED ON PIEZOELECTRIC COEFFICIENT

The coordinate systems for perovskite-ferroelectric crystals with rhombohedral, orthorhombic, and tetragonal structures and the determination process of the electrostrictive coefficients via piezoelectric response are presented.

For $3m$ symmetry, the three principal axes (X, Y, and Z) are along $[1\bar{1}0]$, $[11\bar{2}]$, and $[111]$, respectively. In this coordinate system, the electrostrictive coefficients are noted as Q_{ijkl}^R . The detailed relations between piezoelectric coefficients and electrostrictive coefficients can be written as follows:

$$d_{333}^R = 2P_3^R \epsilon_{33}^R Q_{3333}^R, \quad (\text{A1})$$

$$d_{311}^R = 2P_3^R \epsilon_{33}^R Q_{3311}^R, \quad (\text{A2})$$

$$d_{113}^R = 2P_3^R \epsilon_{11}^R Q_{1313}^R. \quad (\text{A3})$$

Based on Eqs. (A1)–(A3), the electrostrictive coefficients Q_{3333}^R , Q_{3311}^R , and Q_{1313}^R can be determined.

To compare the electrostrictive properties of crystals with various ferroelectric phases, the values of electrostrictive coefficients are generally transformed to the principal axes of the parent cubic phase of perovskite crystal. The X, Y, and Z axes of cubic phase are along [100], [010], and [001] directions, respectively. In this coordinate system, there are three independent electrostrictive coefficients: Q_{11}^C , Q_{12}^C , and Q_{44}^C , where $Q_{11}^C = Q_{1111}^C$, $Q_{12}^C = Q_{1122}^C$, and $Q_{44}^C = 2Q_{1212}^C$ (note: some references use the equation $Q_{44}^C = 4Q_{1212}^C$ ¹¹³). By axis transformation,¹ the Q_{ijkl}^R can be expressed as

$$Q_{3333}^R = \frac{1}{3}(Q_{11}^C + 2Q_{12}^C + 2Q_{44}^C), \quad (A4)$$

$$Q_{3311}^R = \frac{1}{3}(Q_{11}^C + 2Q_{12}^C - 2Q_{44}^C), \quad (A5)$$

$$Q_{1313}^R = Q_{2323}^R = \frac{1}{3}(Q_{11}^C - Q_{12}^C + \frac{1}{2}Q_{44}^C). \quad (A6)$$

Thus, the electrostrictive coefficients Q_{11}^C , Q_{12}^C , and Q_{44}^C can be calculated based on Eqs. (A4)–(A6).

For $mm2$ symmetry, the three principal axes (X, Y, and Z) are along [011], [100], and [011], respectively. In this coordinate system, the electrostrictive coefficients are noted as Q_{ijkl}^O . The detailed relations between piezoelectric coefficients and electrostrictive coefficients can be written as follows:

$$d_{333}^O = 2P_3^O \epsilon_{33}^O Q_{3333}^O, \quad (A7)$$

$$d_{113}^O = 2P_3^O \epsilon_{11}^O Q_{1313}^O, \quad (A8)$$

$$d_{223}^O = 2P_3^O \epsilon_{22}^O Q_{2323}^O. \quad (A9)$$

The relationship between the electrostrictive coefficients Q_{ijkl}^O and Q_{ijkl}^C can be expressed in Eqs. (A10)–(A12)

$$Q_{3333}^O = \frac{1}{2}(Q_{11}^C + Q_{12}^C + Q_{44}^C), \quad (A10)$$

$$Q_{1313}^O = \frac{1}{2}(Q_{11}^C - Q_{12}^C), \quad (A11)$$

$$Q_{2323}^O = \frac{1}{2}Q_{44}^C. \quad (A12)$$

For $4mm$ symmetry, the three principal axes (X, Y, and Z) are along [100], [010], and [001], respectively, being same to the principal axes of cubic phase. Thus, the electrostrictive coefficients can be directly noted as Q_{ijkl}^C . The detailed relations between piezoelectric coefficients and electrostrictive coefficients can be written as follows:

$$d_{333}^T = 2P_3^T \epsilon_{33}^T Q_{3333}^T, \quad (A13)$$

$$d_{311}^T = 2P_3^T \epsilon_{33}^T Q_{3311}^T, \quad (A14)$$

$$d_{113}^T = 2P_3^T \epsilon_{11}^T Q_{1313}^T. \quad (A15)$$

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