Eccentrically Loaded FRP Confined Concrete with Different Wrapping Schemes

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Abstract
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Abstract: This study presents the results of an experimental program on the comparative performance of fiber reinforced polymer (FRP) confined concrete specimens with different wrapping schemes. A total of 32 specimens in four groups were cast and tested under concentric and eccentric axial loads. All specimens were wrapped with the same amount of FRP but with different wrapping schemes, including full wrapping, partial wrapping, and non-uniform wrapping. Specimens in the first group were fully wrapped (Group F). Specimens in the second group were partially wrapped with 30 mm FRP strip spacing (Group P30). Specimens in the third group were partially wrapped with 60 mm FRP strip spacing (Group P60). Specimens in the fourth group were non-uniformly wrapped with a combination of full and partial wrapping (Group FP). Two similar specimens in each group were tested under concentric, 15 mm eccentric, 25 mm eccentric, and 40 mm eccentric axial loads. The test results indicate that fully wrapped specimens outperformed other groups of specimens under both concentric and eccentric axial loads, which were followed by non-uniformly and partially wrapped specimens. With the increase in axial load eccentricity, the performance in all groups significantly decreased. Moreover, with the increase in axial load eccentricity, the failure mode changed from FRP rupture at the compression side to extensive concrete cracking at the tension side. Equations were developed to predict the compressive strength of FRP confined concrete with different wrapping schemes. Experimental and analytical interaction ($P-M$) diagrams were also constructed to investigate the axial and flexural behavior of different groups of specimens.
CE Database subject headings: FRP; Partial; Non-uniform; Concrete; Eccentricity; Interaction diagram.

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Introduction

Fiber reinforced polymer (FRP) has been extensively investigated to provide confinement to concrete due to the advantages of high strength and stiffness to weight ratio as well as superior corrosion resistance. A large number of experimental and analytical studies were conducted in the literature to understand and model the compressive behavior of FRP confined concrete. It was proved that FRP confinement can significantly enhance the performance of concrete under compressive loads (Lam and Teng 2003a, b; Hadi 2006a, b; Hadi et al. 2015; Wang et al. 2016; Wang et al. 2017).

Even though a considerable number of studies were conducted on fully FRP wrapped concrete, only a few studies focused on partially FRP wrapped concrete (Barros and Ferreira 2008; Park et al. 2008; Campione et al. 2015; Pham et al. 2015; Triantafyllou et al. 2015; Saljoughian and Mostofinejad 2016). Partial FRP wrapping requires less FRP materials and can be applied easier and faster than full wrapping (Pham et al. 2015). Moreover, for existing reinforced concrete (RC) columns confined with sparse steel ties, the compressive performance of existing RC columns is expected to be improved by partial FRP wrapping in between the sparse steel ties, as the local buckling of longitudinal steel bars can be effectively constrained by the partial FRP wrapping (Triantafyllou et al. 2015). Furthermore, for existing deteriorated RC columns, partial FRP wrapping onto the deteriorated part of the RC columns can significantly increase the strength and ductility of the columns without consuming excessive FRP materials which otherwise would be required for the full wrapping of the RC columns (Wei et al. 2009). Few studies also investigated the use of composite taps and ropes as the confinement materials for concrete in the form of full or partial wrapping (Rousakis 2014, 2016).
Several research studies investigated the behavior of partially FRP wrapped concrete under axial compressive load (Matthys et al. 2005; Barros and Ferreira 2008; Triantafyllou et al. 2014; Pham et al. 2015). Among these studies, Barros and Ferreira (2008) systematically investigated the confinement efficiency of partially FRP wrapped plain and RC column specimens. It was reported that a significant increase in the load carrying capacity and deformation capacity can be obtained by reducing the FRP strip spacing and reducing the unconfined concrete strength, or increasing the confinement stiffness of FRP jacket (Barros and Ferreira 2008). Pham et al. (2015) investigated the axial compressive behavior of FRP wrapped concrete with different FRP wrapping schemes. In Pham et al. (2015), a non-uniform FRP wrapping scheme with a combination of full and partial FRP wrapping was proposed. It was reported that higher axial compressive strength and axial strain, in comparison with full FRP wrapping scheme, could be obtained by non-uniform FRP wrapping. Moreover, an equation was proposed to predict the compressive strength of partially FRP wrapped concrete.

Concrete columns are often subjected to the combined axial and flexural loads in practical situations. Several studies investigated the behavior of fully FRP wrapped concrete under eccentric loads. It was concluded that the strain gradient effect caused a non-uniform confining pressure which reduced the efficiency of the FRP confinement under eccentric loads (Parvin and Wang 2001; Hadi 2006 a,b; Wu and Jiang 2013). Even though partial FRP wrapping is considered to be promising in some particular applications, studies on partially FRP wrapped concrete under eccentric load are limited. Moreover, none of the previous studies provided information on non-uniformly FRP wrapped concrete under eccentric load. This study investigates the behavior of FRP confined plain concrete specimens with different wrapping schemes under concentric and eccentric axial loads. An experimental program was conducted to
investigate the comparative performance of fully, partially, and non-uniformly FRP wrapped concrete under concentric and eccentric axial loads (eccentricity of 15 mm, 25 mm, and 40 mm). The failure modes, axial load-axial deformation behaviors, ductility capacity, and axial load-bending moment interactions \((P-M)\) of the specimens were investigated. Moreover, an analytical procedure was developed to predict the axial and flexural behaviors of the tested specimens with the aim to better understand the ultimate capacities of all groups of specimens.

**Experimental Program**

**Design of Experiments**

A total of 32 concrete specimens were cast and tested under concentric and eccentric axial loads. All the specimens were 150 mm in diameter and 300 mm in height. Four groups of specimens, with 8 specimens in each group, were divided based on the FRP wrapping schemes. All groups of specimens were wrapped with same amount of FRP but following different wrapping schemes. The aim was to investigate the influence of different wrapping schemes on the behavior of FRP wrapped concrete under concentric and eccentric axial loads. Specimens in the first group were fully wrapped with two layers of carbon fiber reinforced polymer (CFRP), as shown in Fig. 1(a). Specimens in the second group were partially wrapped with four layers of 30 mm wide FRP strips, and the spacing between neighboring FRP strips was 30 mm, as shown in Fig. 1(b). Specimens in the third group were partially wrapped with six layers of 30 mm wide FRP strips, while the spacing between neighboring FRP strips was 60 mm, as shown in Fig. 1(c). Specimens in the fourth group were non-uniformly wrapped, as shown in Fig. 1(d). For the fourth group of specimens, at first, the specimens were fully wrapped with one layer of FRP. Afterwards, two layers of 30 mm wide FRP strips were wrapped onto the first layer of FRP with 30 mm spacing between neighboring FRP strips. It is noted that the amount of FRP for Group P30 and FP
specimens were slightly different from those of Group F and P60 specimens (Fig. 1). This slight
difference was mainly due to the length of the specimen, which made it difficult to maintain
exactly the same amount of FRP. However, it is believed that this slight difference might not
affect the results, since all the specimens were expected to fail in the mid-height region. In the
mid-height region, the wrapping configurations were different, but the amount of FRP were
exactly the same.

For specimens in each group, two identical specimens were tested under the same load
conditions to ensure representative test results. Axial load eccentricities of 0, 15, 25, and 40 mm
were adopted in this study, where zero eccentricity corresponds to concentric axial load. Table 1
lists the detailed test matrix. The specimens have been labelled as: (a) “F”, “P30”, “P60”, and
“FP” represent fully wrapped, partially wrapped with 30 mm FRP strip spacing, partially
wrapped with 60 mm FRP strip spacing, and non-uniformly wrapped specimens, respectively; (b)
“E” and the number afterwards indicate load eccentricity (0 indicates concentric axial load; 15
indicates eccentric axial load with 15 mm eccentricity; 25 indicates eccentric axial load with 25
mm eccentricity; and 40 indicates eccentric axial load with 40 mm eccentricity); and (c) “1” or
“2” indicates the order of the two identical specimens tested under the same axial load conditions.

**Specimen Preparation and Material Properties Test**

The CFRP sheet used in this study was supplied by Nanjing Hitech Composites CO., LTD (2016). The original width of CFRP sheet was 100 mm and the thickness was 0.167 mm per
layer. For fully wrapped specimens, the 100 mm wide CFRP sheet was wrapped onto the top,
middle, and bottom parts of the specimens. Therefore, there was no overlap between the parts, as
each part was 100 mm. In order to obtain the required width of CFRP strip for partially wrapped
specimens, each CFRP strip was precisely cut from the original CFRP sheet using a pair of scissors.

Normal strength concrete with a design compressive strength of 32 MPa was used for casting the specimens. The concrete was supplied by a local concrete provider with a maximum aggregate size of 10 mm. After 28 days of standard curing, the concrete specimens were wrapped with CFRP. A mixture of epoxy resin and hardener at a ratio of 5:1 was used as an adhesive. Preparations of fully and partially FRP wrapped specimens were similar: before the first layer of CFRP was wrapped, the adhesive was evenly spread onto the surface of the specimen and then CFRP was wrapped onto the specimen surface with the fibers oriented in the hoop direction. Immediately after the first layer was wrapped, the adhesive was evenly spread onto the surface of the first layer of CFRP and the second layer was continuously wrapped. The remaining layers of CFRP were wrapped in a similar manner. An overlap of 100 mm was ensured in the last layer of CFRP strips. While for non-uniformly FRP wrapped specimens, the specimens were left for a while until the adhesive was hardened after the one layer full wrapping was conducted. Afterwards, the remaining CFRP strips were wrapped.

Compression tests at 28 days showed that the average compressive strength of the concrete was 37.7 MPa. The tensile properties of CFRP were tested according to ASTM D7565 (ASTM 2010). Five CFRP coupons with 25 mm width and 250 mm length were prepared and tested. For each coupon, three layers of CFRP were glued together using epoxy resin. The coupons were capped at both ends by aluminum plates. Detailed description of the test can be found in Wang et al.
The average nominal thickness of the coupons was 1.18 mm, and the average tensile strength of CFRP was 1674 MPa with an average ultimate strain of 0.016.

**Instrumentation**

The Denison 5,000 kN compression testing machine was used for testing all the specimens. For concentrically and eccentrically loaded specimens, the specimen ends were capped with high-strength plaster to ensure a uniform load distribution. In order to apply eccentric axial load onto the specimens, a set of loading heads were used (Figs. 2 (a) and (b)). Axial deformations of the specimens were measured using two Linear Variable Differential Transducers (LVDTs), which were mounted at the opposite corners between the loading plate and the supporting plate of the Denison testing machine. Therefore, the height of the specimens used to obtain the axial deformations from LVDTs was 300 mm. In order to measure the lateral deflections for the eccentrically loaded specimens, a laser triangulation was used. The laser triangulation was manufactured by Bestech Australia Pty Ltd. (2018). The laser triangulation was positioned onto the bottom loading plate by using a magnetic base and was set up at the mid-height of the specimen, as shown in Fig. 2 (c). For the specimens tested under 15 and 25 mm eccentric axial loads, the laser triangulation was positioned on the tension side. However, as few specimens failed in an explosive manner, the laser triangulation was moved to the compression side for the specimens tested under 40 mm eccentric axial load to prevent the probable damage of the laser triangulation. All the tests were conducted as deflection controlled at a rate of 0.5 mm/min. The readings of the load and LVDTs were taken using a data logging system and were subsequently saved in a control computer.
Experimental Results and Analysis

Specimens under Concentric Axial Load

The failure modes of concentrically loaded specimens are presented in Fig. 3. All concentrically loaded specimens failed due to the brittle rupture of CFRP. For partially FRP wrapped concrete specimens, small cracks were observed on the surface of non-wrapped concrete during the loading. As the load increased, the non-wrapped concrete began to crush and spall off. The spalling of non-wrapped concrete was more severe for specimens with 60 mm strip spacing. The spalling of non-wrapped concrete was then followed by the rupture of the CFRP strips around the mid height of the specimens. For Specimens FP-E0, the one layer CFRP ruptured first, resulting in a small and sudden drop in the axial load. Afterwards, the axial load began to increase again until the three layers CFRP at the mid height of specimens ruptured, causing a fatal failure.

The test results for concentrically loaded specimens are presented in Table 2. The axial load at the elastic limit $P_1$ and the corresponding axial deformation $\Delta_1$, the peak axial load $P_2$ and the corresponding axial deformation $\Delta_2$, the ductility $\mu$, as well as the failure mode, are presented in Table 2. In this study, the definition on the axial load at the elastic limit $P_1$ in Pessiki and Pieroni (1997) was used for specimens that exhibited strain softening response, as shown in Figs. 4 (a) and (b). However, this definition was unable to accurately determine $P_1$ for specimens which exhibited strain hardening response (Dong et al. 2015). In this case, the definition given by Dong et al. (2015) was adopted, as shown in Fig. 4 (c).
The peak axial loads of Specimens F-E0 were the highest among the concentrically loaded specimens, which were on average 68% higher than those of the Specimens P60-E0. Specimens FP-E0 achieved peak axial loads that were on average 52% higher than those achieved by Specimens P60-E0. An average of 46% increase in the peak axial loads compared to Specimens P60-E0 was achieved by Specimens P30-E0. Fig. 5 shows the axial load-axial deformation behavior of concentrically loaded specimens. Since the lateral deflections for concentrically loaded specimens were very small, they were not recorded by using the laser triangulation setup. Moreover, for comparisons, the axial load-axial deformation behavior of plain concrete specimens was also presented. All specimens exhibited similar behavior at the initial stage, while the slope of the second branch varied significantly between different groups of specimens. For plain concrete specimens (P-E0-1, 2), the axial load decreased significantly after the peak axial load and finally lost all the strength with a small axial deformation. Typical bilinear curves for concentrically loaded FRP confined concrete specimens. The slope of the second linear branch for Specimens F-E0 and FP-E0 was almost identical and the highest, followed by those of Specimens P30-E0 and Specimens P60-E0. It is noted that even though extensive concrete cracking occurred for Specimens P30-E0 and P60-E0, the FRP strips prevented the axial load from dropping and ensured continuous increases of the axial load (Campione 2015; Rousakis 2014, 2016). On the other hand, the FRP confinement efficiency was highly dependent on the strip spacing: the less the strip spacing, the higher the confinement efficiency. Even though the load-deformation behavior of Specimens F-F0 was quite similar to the load-deformation behavior of Specimens FP-E0, Specimens FP-E0 failed earlier than Specimens F-E0. A slight drop in the axial load can be observed for Specimens FP-E0, which was due to the rupture of one layer CFRP. Afterwards, the axial load continued to increase slightly until the rupture of three
layers CFRP. For non-uniformly FRP confined concrete specimens, the rupture of one layer CFRP can be used as a suitable indication before the final rupture of the specimens. Moreover, even though Specimens P60-E0 achieved the lowest peak axial loads, the axial deformation was the highest, which was mainly because significant strain localization occurred within the non-wrapped region (Wei and Wu 2016).

Specimens under 15 mm Eccentric Axial Load

The failure modes of specimens under 15 mm eccentric axial load are presented in Fig. 6. Specimens F-E15, FP-E15, and P30-E15 failed by the CFRP rupture at the mid height of the specimens on the compression side. For Specimens FP-E15, the one layer CFRP above and below the mid height of the compression side ruptured first. This was followed by a continuous axial load increase until the rupture of three layers of CFRP at the mid height of the compression side. For Specimens P30-E15, tension cracks occurred within the non-wrapped concrete at the mid height of the tension side. Afterwards, the tension cracks propagated approximately half way through the specimen until the rupture of CFRP strips. The CFRP rupture for Specimen P30-E15-1 was explosive, resulting in the specimen breaking into two halves. The failure of Specimens P60-E15 was due to the propagation of the tension crack from the tension side to the compression side. When the tension crack developed to the compression side, the specimens failed and no CFRP rupture was observed for Specimens P60-E15.

The test results for specimens under 15 mm eccentric axial load are presented in Table 3. The lowest peak axial loads were carried by Specimens P60-E15. Specimens F-E15 achieved the greatest peak axial loads, which were on average 103% higher than those carried by Specimens
The peak axial loads of Specimens FP-E15 and P30-E15 were on average 75% and 47%, respectively, greater than the peak axial loads of Specimens P60-E15. Fig. 7 shows the axial load-axial deformation behavior of Specimens F-E15, FP-E15, P30-E15, and P60-E15. Specimens F-E15, FP-E15, and P30-E15 experienced strain hardening responses after the initial parabolic ascending branches, while strain softening responses were observed in Specimens P60-E15 due to insufficient confinement provided by the sparse CFRP strips. Also, the spalling of non-wrapped concrete may have further resulted in the performance deterioration of partially FRP confined specimens. Even though the peak axial loads of Specimens P30-E15 were significantly less than the peak axial loads of Specimens F-E15 and FP-E15, the deformation capacities of Specimens P30-E15 were even higher, which suggested that the strain localization within non-wrapped region still existed for partially wrapped concrete under small load eccentricities. Moreover, since the failures of Specimens P60-E15 were caused by extensive concrete cracking on the tension side, the ultimate condition was defined when the axial load dropped by 15% of the peak axial load. The corresponding lateral deflections at the ultimate conditions were 9.9 and 9.3 mm, respectively, which were higher than those of other groups of specimens (Table 3). Therefore, the gradual failure for Specimens P60-E15 resulted in a pseudo-ductile behavior compared to other specimens.

**Specimens under 25 mm Eccentric Axial Load**

The failure modes of specimens under 25 mm eccentric axial load are presented in Fig. 8. Specimens F-E25 failed by CFRP rupture at the mid height of the compression side. Specimens P30-E25 failed by a combination of CFRP rupture and concrete tension cracking failure. For Specimens P30-E25, the non-wrapped concrete on the compression side crushed and two
horizontal tension cracks appeared above and below the middle CFRP strip on the tension side. The horizontal tension cracks then started to propagate towards the compression side, which resulted in a gradual decrease in axial load. Almost simultaneously, the CFRP strip at the mid height ruptured and the horizontal tension cracks reached the compression side. Specimens P60-E25 failed due to the propagation of horizontal tension crack initiated at the tension side. Failure occurred when the horizontal crack propagated to the compression side, and no CFRP rupture was observed. Specimens FP-E25 failed by the CFRP rupture on the compression side. The one layer CFRP around the mid height ruptured first, which was followed by the rupture of three layers of CFRP on the compression side.

The test results of specimens under 25 mm eccentric axial load are presented in Table 3. Specimens P60-E25 carried the lowest peak axial loads. Considering Specimens P60-E25 as a basis of comparison, Specimens F-E25 carried the largest peak axial loads, which were on average 70% higher. The peak axial loads carried by Specimens FP-E25 and P30-E25 were on average 48% and 22% greater than the peak axial loads carried by Specimens P60-E25, respectively. The axial load-axial deformation behavior of Specimens F-E25, FP-E25, P30-E25, and P60-E25 are shown in Fig. 9. It was apparent that the post-peak behavior of the specimens varied between different groups of specimens. Specimens F-E25 and FP-E25 presented post-peak ascending branches, whereas Specimens P60-E25 presented post-peak descending branches. The post-peak branches of Specimens P30-E25 were initially ascending before reaching the peak axial load at which the curves transitioned from ascending to descending. It should be noted that for Specimens P30, the CFRP rupture did not occur until the occurrence of descending branch,
which indicated that the confinement provided by the FRP strips was not maximum at peak axial load.

**Specimens under 40 mm Eccentric Axial Load**

The failure modes of specimens under 40 mm eccentric load are presented in Fig. 10. All specimens experienced extensive concrete tension cracks from the tension side to the compression side. For Specimens P60-E40, the propagation of the horizontal tension cracks occurred relatively quickly compared to the other groups of specimens, which resulted in a much quicker failure. For Specimens FP-E40, the tension cracks initiated at the mid height on the tension side. Slight rupture of the one layer CFRP around the mid height of the compression side was observed for Specimens FP-E40, and this slight rupture did not result in the final failure of specimens.

The test results for specimens under 40 mm eccentric load are presented in Table 3. It can be seen that Specimens P60-E40 carried lowest peak axial loads. Specimens F-E40 achieved the greatest peak axial loads, which were on average 27% higher than the peak axial loads carried by Specimens P60-E40. Specimens FP-E40 achieved peak loads which were on average 26% greater than the average peak axial loads of Specimens P60-E40. Specimens P30-E40 carried peak axial loads that were only on average 5% higher than Specimens P60-E40. Fig. 11 shows the axial load-axial deformation behavior of Specimens F-E40, FP-E40, P30-E40, and P60-E40. All specimens presented post-peak descending branches, which suggests the effectiveness of FRP wrapping in terms of providing a strength increase was insignificant for specimens with large load eccentricity. Even though the peak axial loads for Specimens P30-E40 were only
slightly higher than the peak axial loads of Specimens P60-E40, the deformation capacity, especially the lateral deflection capacities of Specimens P30-E40 were significantly higher than those of Specimens P60-E40.

**Influence of Axial Load Eccentricity**

The influence of axial load eccentricity on the increase of peak axial loads of different groups of specimens is shown in Fig. 12. In Fig. 12, the vertical axis is $P_2 / (f_{co} \cdot A_g)$ and the horizontal axis is $e/d$ (Note: $A_g$ is the gross cross section area, and $d$ is the diameter of the confined concrete).

In general, an increase in the axial load eccentricity led to a significant decrease in the peak axial loads of all specimens. At low axial load eccentricity ($e/d = 0.1$), specimens of Groups P30 and P60 experienced a greater decrease (44% and 45%, respectively) in the peak axial loads than the decrease in the peak axial loads in specimens of Groups F and FP (33% and 36%, respectively). However, as the axial load eccentricity increased, the percentage of decrease in the peak axial loads for different groups of specimens was close. Referring to the specimens tested in Groups F, FP and P30, an overall decrease in peak axial loads of 79.4%, 77.4% and 80.5% was observed when the $e/d$ ratio was increased from 0 to 0.27. Similarly, specimens in Group P60 experienced an overall load decrease of 72.7% in the peak axial loads for the same increment in eccentricity. Moreover, it can be observed that as the axial load eccentricity increased, the difference in peak axial loads for specimens in each group decreased. When specimens were subjected to an eccentric axial load with an $e/d$ ratio of 0.27, the peak axial loads carried by specimens in each group were quite close.
It is noted that the tested specimens were not reinforced with steel bars. Hence, the influence of the longitudinal steel reinforcement on the behavior of FRP confined concrete with different wrapping schemes was not reflected in the test results. Also, the size of the tested specimens was relatively small compared to the full-scale columns. Although the size effect on FRP confined concrete was found insignificant in several previous studies (Carey and Harries 2005; Elsanadedy et al. 2012; Thériault et al. 2004), Jamatia and Deb (2017) reported the existence of size effect on the behavior of FRP confined concrete under axial compression. Hence, the experimental results presented in this study should be translated with caution for large FRP confined reinforced concrete columns.

**Ductility Capacity**

Ductility is defined as the ability of structural members to deform plastically without substantial loss of strength. For steel reinforced concrete (RC) column, the ductility is usually calculated as the ratio of the axial deformation at 85% post-peak load divided by the axial deformation at the elastic limit (Pessiki and Pieroni 1997):

\[ \mu = \frac{\Delta_3}{\Delta_1} \]  

where \( \mu \) is the ductility, \( \Delta_3 \) is the axial deformation at 85% post-peak load, and \( \Delta_1 \) is the corresponding axial deformation of the axial load at the elastic limit \( P_1 \).

The above definition of ductility is usually not applicable for FRP confined concrete. For sufficiently FRP confined concrete (Fig. 4 (c)) with strain hardening response, the specimens failed at the peak axial load due to FRP rupture. In this case, it is not reasonable to use the axial deformation at 85% post-peak axial load to calculate the ductility. Another case is that for
insufficiently FRP confined concrete with strain softening response, the axial load at FRP rupture
may be between the peak axial load and 85% post-peak axial load (Fig. 4 (a)). The last case is
that the axial load at FRP rupture is lower than 85% post-peak axial load (Fig. 4 (b)). In different
cases, the definition of ductility should be selected differently to accurately represent the
deformation capacity of specimens.

The ductility capacity of all specimens is summarized in Tables 2 and 3. It can be seen that
Group F specimens obtained higher ductility compared to the other groups of specimens under
both concentric and eccentric axial loads. Even though the average peak axial loads of
Specimens P60-E0 were only 49.3% of those of Specimens F-E0, the ductility capacities were
almost equal. This again indicates that significant strain localization occurred within the non-
wrapped region for partially FRP wrapped concrete. Moreover, with the increase of axial load
eccentricities, the ductility capacities for all groups of specimens decreased. When the applied
axial load changes from concentric axial load to eccentric axial loads of 15 mm, 25 mm and
40mm eccentricities, the decrease of ductility for Group F specimens was 34.2%, 40.8%, and
53.3%, respectively. Similar ductility decrease was obtained for Group FP specimens. However,
the corresponding decreases in ductility were 54.7%, 73.7%, and 83.7%, respectively, for Group
P60 specimens. This indicates that the adverse influence of axial load eccentricity on the
ductility of partially FRP wrapped concrete was more severe than those of fully and non-
uniformly FRP wrapped concrete.

Theoretical Analysis

Compressive Strength Prediction for Concentrically Loaded Specimens
The compressive strength of the concentrically loaded specimens was predicted by using a strength model proposed in this study. The Lam and Teng (2003a) model was selected as the base model because it is one of the most widely accepted models for the predictions of the compressive strength of circular FRP confined concrete, which was highlighted by its implementation into ACI 440.2R-08 (ACI 2008). Although the Lam and Teng (2003a) model has been proven to accurately predict the compressive strength of fully FRP wrapped concrete, the model is not able to account for partial or non-uniform wrapping schemes. In order to account for the reduced confinement effectiveness due to partial wrapping, a confinement effectiveness coefficient $k_j$ is introduced into the Lam and Teng (2003a) model. The following expression was developed for compressive strength prediction of fully and partially FRP wrapped concrete:

$$\frac{f_{cc}}{f_{co}} = 1 + 3.3k_j \frac{f_{l.a}}{f_{co}}$$

where $f_{cc}$ is the compressive strength of confined concrete; $f_{co}$ is the unconfined compressive strength of concrete; $k_j$ is the confinement effectiveness coefficient; and $f_{l.a}$ is the actual lateral confining pressure.

The confinement effectiveness coefficient can be expressed as (Mander et al. 1988; Barros and Ferreira 2008; Pham et al. 2015):

$$k_j = \left(1 - \frac{s}{2d}\right)^2$$

where $s$ is the clear spacing between two adjacent FRP strips and $d$ is the diameter of confined concrete.
The actual lateral confining pressure can be taken according to Equation (4), which was proposed for full and partial FRP wrapping schemes in Barros and Ferreira (2008) and Pham et al. (2015):

$$f_{l,a} = \frac{2E_f t_f \epsilon_{h,up}}{d} \frac{w}{w + s}$$  \hspace{1cm} (4)

where $E_f$ is the elastic modulus of FRP; $t_f$ is the thickness of FRP; $\epsilon_{h,up}$ is the actual hoop rupture strain of FRP; and $w$ is the width of FRP strips.

Using Equations (2), (3) and (4), the compressive strength of concentrically loaded fully and partially FRP wrapped concrete can be predicted. However, further modification was required for specimens with non-uniform wrapping scheme. The non-uniform FRP wrapping was considered to comprise two components, namely, full FRP wrapping and partial FRP wrapping. The confinement provided by the partial FRP wrapping was added to the confinement provided by the full FRP wrapping using the principle of superposition. Therefore, the expression for the compressive strength of concentrically loaded non-uniformly FRP wrapped concrete is as follows:

$$\frac{f_{cc}}{f_{co}} = 1 + 3.3 \frac{f_{l_f} + k_f f_{l_p}}{f_{co}}$$  \hspace{1cm} (5)

where $f_{l_f}$ is the confining pressure provided by the full FRP wrapping; $k_f$ is the confinement effectiveness coefficient, which can be expressed as $(1 - s / 2d)^2$; and $f_{l_p}$ is the confining pressure provided by the partial FRP wrapping.
Strain gauges were attached at the mid-height of the specimen to obtain axial and hoop strains. However, most of the readings of the strain gauges experienced a large scatter due to the poor welding of the wires. Therefore, the recorded strain values were considered not accurate and hence not used. Based on the findings from several studies (Chen et al. 2013; Lam and Teng 2003a; Wu and Jiang 2013), the ACI 440.2R-08 (2008) suggests that the strain efficiency factor to be taken as 0.55. Hence, the actual hoop rupture strain was taken as 55% of the nominal tensile strain of FRP. Considering this strain efficiency factor and a nominal FRP rupture strain of 1.7%, the actual FRP hoop rupture strain was determined to be 0.935%. Equations (2) and (5) were applied to predict the compressive strength of all concentrically loaded specimens in this study. Table 4 compares the experimental and analytical results of all concentrically loaded specimens. It is evident that the proposed equations underestimate the compressive strength of Specimens F-E0, FP-0, and P30-E0, with a maximum error of 17% for Specimens F-E0. However, overestimation was obtained for Specimens P60-E0-2 with a maximum error of 23%. The differences between experimental and analytical results indicate that, with the increase of FRP strip spacing, the strength reduction was more significant than the analytical predictions. In general, the proposed equations can provide reasonable predictions for the compressive strengths of the concentrically loaded specimens.

**Analytical Interaction (P-M) Diagram**

Interaction (P-M) diagrams were constructed to investigate the axial load and bending moment capacity of the specimens. For eccentrically loaded specimens, the bending moment capacity considering the second order moment was calculated by Equations (6):
where $P_u$ indicates ultimate load, $e$ indicates load eccentricity, and $\delta$ indicates lateral deflection at the ultimate load.

The experimental non-dimensional interaction diagrams are shown in Fig. 13. In Fig. 13, the vertical axis is $P_u / f_{co} \cdot A_g$ and the horizontal axis is $M_1 / f_{co} \cdot A_g \cdot d$, where $A_g$ is the gross cross section area, and $d$ is the diameter of the confined concrete. Group F specimens outperformed the other groups of specimens, followed by Groups FP, P30, and P60 specimens. Moreover, with the increase of eccentricity from 25 mm to 40 mm, the differences between the different groups of specimens became less significant, which indicates that the confinement efficiency was less with the increase of eccentricity. It can also be observed that for an eccentricity of 40 mm, the performance of Groups F and FP specimens was comparable and the performance of Groups P30 and P60 was comparable.

In this section, a numerical fiber element method was used to construct the analytical interaction diagrams of concrete specimens (Fam et al. 2003; Yazici and Hadi 2009; Wang et al. 2016). The cross section of concrete specimens was divided into a finite number of small horizontal strips, as shown in Fig. 14. In each layer, the area of concrete core was calculated. With the plain section assumption, the axial strain in each strip was estimated and the axial stress of each component was calculated by the stress-strain model of concrete. The calculated stresses were then integrated over the whole cross section area to obtain the resultant force and the resultant moment. For a given eccentricity $e$, the depth of neutral axis, $d_u$, was first assumed. Based on the assumed neutral axis and the ultimate axial strain at the extreme compression fiber of the section, the resultant force and the resultant bending moment were obtained. Afterwards, the
eccentricity $e'$ was obtained by dividing the bending moment by the force. If the calculated eccentricity $e'$ was the same with the given eccentricity $e$, the calculation was completed and the calculated force and bending moment were the true values. If not, the depth of neutral axis was readjusted. The above procedure was repeated until the calculated eccentricity $e'$ was the same with the given eccentricity $e$. In order to get more accurate prediction results, the width of the strips should be small enough. In this study, the width of the strips was taken as 1 mm. For FRP materials, a linear elastic stress-strain relationship was adopted. The tensile stress carried by the concrete was neglected in this study. For concrete under compression, the stress-strain model proposed by Lam and Teng (2003a) was adopted for the FRP confined concrete subjected to concentric axial load, which can be described by the following expressions:

$$
\sigma_c = E_c \varepsilon - \frac{(E_c - E_s)^2}{4f_{co}} \varepsilon^2 \text{ for } 0 \leq \varepsilon \leq \varepsilon_c \tag{7}
$$

$$
\sigma_c = f_{co} + E_2 \varepsilon \text{ for } \varepsilon \leq \varepsilon_c \leq \varepsilon_{cu} \tag{8}
$$

where $\sigma_c$ and $\varepsilon_c$ are the axial stress and axial strain, respectively; $E_c$ is the elastic modulus of unconfined concrete; $E_2$ is the slope of the linear second portion of the stress-strain curve; and $\varepsilon_{cu}$ is the ultimate axial strain of confined concrete. The parabolic first portion meets the linear second portion with a smooth transition at $\varepsilon_c$:

$$
\varepsilon_c = \frac{2f_{co}}{(E_c - E_s)} \tag{9}
$$

The slope of the linear second portion $E_2$ is given by
\[ E_z = \frac{f_{cc} - f_{co}}{\varepsilon_{cu}} \quad (10) \]

where \( f_{cc} \) is the compressive strength of confined concrete. In this study, the compressive strengths of Groups F, P30, and P60 specimens subjected to concentric axial load were predicted by Equation (2), while the compressive strength of Group FP specimens subjected to concentric axial load were predicted by Equation (5). The ultimate axial strain \( \varepsilon_{cu} \) can be calculated by (Lam and Teng 2003):

\[
\frac{\varepsilon_{cu}}{\varepsilon_{co}} = 1.75 + 12 \left( \frac{f_{cu}}{f_{co}} \right) \left( \frac{\varepsilon_{cu}}{\varepsilon_{co}} \right)^{0.45} \quad (11)
\]

where \( \varepsilon_{co} \) is the compressive strain of concrete corresponding to \( f_{co} \).

Moreover, in order to consider the reduced effectiveness of FRP confinement for concrete core subjected to eccentric load, a variable confinement model was adopted to describe the stress-strain relationship of concrete core under eccentric axial load (Yu et al. 2010). This model is an extension of Teng et al. (2009) model. The only difference is the value of the slope of the second linear portion of the concrete stress-strain curve \( E_z \). For concrete under eccentric axial load, the slope of the second linear portion of the stress-strain curve was calculated as:

\[
E_{2ec} = E_z \frac{d}{d + e} \quad (12)
\]

where \( E_{2ec} \) is the slope of the second linear portion of the concrete stress-strain curve, and \( d \) is the diameter of confined concrete.
It should be noted that the above concrete stress-strain model is only suitable for sufficiently FRP confined concrete with strain hardening response (Bisby and Ranger 2010). For insufficiently FRP wrapped concrete as well as for specimens failed due to concrete cracking, the above concrete stress-strain curve reduces to a stress-strain curve composed of an initial parabola followed by a horizontal straight line (ACI 440.2R 2008; Lam and Teng 2003a; Rocca et al. 2009). The compressive strength equals to the unconfined concrete strength, and the ultimate axial strain was assumed to be 0.003, as suggested in ACI 440.2R (2008). Fig. 15 compares the experimental and analytical interaction diagrams (non-dimensional) of different groups of specimens. For comparison purpose, the bending moment capacity without considering the second order moment was also calculated and presented in Fig. 15:

\[ M_2 = P_2 \cdot e \]  

For Groups F and FP specimens, the analytical interaction diagrams were significantly lower than the experimental P-M₁ interaction diagrams. The difference between the experimental and analytical compressive strength was relatively small (as shown in Table 4), while the analytical bending moment was much lower than the experimental bending moment M₁. For Group P30 specimens, the analytical interaction diagrams were lower than the experimental P-M₁ interaction diagrams, but the difference was not significant. While for Group P60 specimens, the analytical results were significantly higher than the experimental P-M₁ interaction diagrams. In general, by using the proposed fiber element method, conservative predictions can be obtained for Groups F, FP, and P30 specimens, which is safe for the column design. This conclusion was similar to the observations reported in Bisby and Ranger (2010). Nevertheless, the analytical results were significantly higher than the experimental P-M₁ interaction diagrams for Group P60 specimens. This may be because the non-wrapped concrete began to spall off after the unconfined
compressive strength was reached, which may result in the performance deterioration of specimens. However, the spalling of non-wrapped concrete (i.e., loss of cross sectional area) was not taken into consideration by the proposed analytical method. With the increase of the spacing of FRP strips, the spalling of non-wrapped concrete became more severe and thus greater error between experimental and analytical results was observed. Therefore, a more accurate analytical model needs to be developed for partially FRP wrapped concrete to account for the performance deterioration of specimens due to spalling of non-wrapped concrete.

**Conclusions**

Experimental and analytical studies were carried out to investigate the performance of fully, partially, and non-uniformly FRP wrapped concrete under concentric and eccentric axial loads. The following conclusions can be drawn:

1. The axial load carrying capacity of fully FRP wrapped concrete is the highest under both concentric and eccentric axial loads, followed by non-uniformly and partially FRP wrapped concrete. Moreover, the peak axial load of the specimen is significantly reduced with the increase in the axial load eccentricity for all groups of specimens.

2. The failure mode of the specimen is influenced by the axial load eccentricity. The FRP rupture is the main failure mode for specimens tested at lower axial load eccentricities, whereas concrete tension cracking failure is the dominate failure mode for specimens tested at higher axial load eccentricities. The transfer from FRP rupture failure to concrete tension cracking failure occurs at lower axial load eccentricities for partially wrapped specimens than for the fully and non-uniformly wrapped specimens.
3. Equations are proposed to predict the compressive strength of FRP wrapped concrete with different wrapping schemes. As for non-uniformly FRP wrapped concrete, the confinement is composed of two components, namely, confinement provided by full FRP wrapping and confinement provided by partial FRP wrapping. By using the principle of superposition, the compressive strength can be predicted with a reasonable accuracy.

4. Experimental and analytical interaction diagrams are constructed to investigate the behavior of eccentrically loaded specimens. In general, the analytical model reasonably predicts the compressive strengths of Groups F and FP specimens, but underestimates the bending moment capacities. The analytical model overestimates the compressive strengths of Groups P30 and P60 specimens. With the increase of the spacing of FRP strips gaps, the overestimation of bending moment become more significant for partially FRP wrapped concrete. These overestimations occur mainly because the analytical model does not consider the performance deterioration of partially FRP wrapped concrete, which is due to the spalling of non-wrapped concrete.

5. Non-uniform wrapping combines the advantages of full and partial wrapping. Compared to partial wrapping, the non-uniform wrapping provides higher strength and ductility under both concentric and eccentric axial loads. Moreover, for partially FRP wrapped concrete, the non-wrapped concrete may be exposed to harsh environment (e.g., moisture, heat, and impact), which may deteriorate the performance of concrete (e.g., corrosion of inner steel reinforcement and concrete spalling). By wrapping FRP non-uniformly, these adverse effects can be alleviated. Meanwhile, after fewer layers of full wrapping, the remaining layers of partial wrapping can only be applied onto the deteriorated parts of the columns. Therefore, the consumption of FRP may be less than in the case of full wrapping.
Acknowledgments

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References

ACI 440.2R-08. (2008). "Guide for the design and construction of externally bonded FRP systems for strengthening concrete structures." ACI 440.2R-08, American Concrete Institute, Detroit.


### Table 1. Test matrix

<table>
<thead>
<tr>
<th>Specimen</th>
<th>Wrapping scheme</th>
<th>FRP layers</th>
<th>Strip spacing</th>
<th>Test Mode</th>
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<tbody>
<tr>
<td>F-E0-1,2</td>
<td>Full</td>
<td>2 full layers</td>
<td>0</td>
<td>e=0 mm</td>
</tr>
<tr>
<td>F-E15-1,2</td>
<td>Full</td>
<td>2 full layers</td>
<td>0</td>
<td>e=15 mm</td>
</tr>
<tr>
<td>F-E25-1,2</td>
<td>Full</td>
<td>2 full layers</td>
<td>0</td>
<td>e=25 mm</td>
</tr>
<tr>
<td>F-E40-1,2</td>
<td>Full</td>
<td>2 full layers</td>
<td>0</td>
<td>e=40 mm</td>
</tr>
<tr>
<td>P30-E0-1,2</td>
<td>Partial</td>
<td>4 partial layers</td>
<td>30</td>
<td>e=0 mm</td>
</tr>
<tr>
<td>P30-E15-1,2</td>
<td>Partial</td>
<td>4 partial layers</td>
<td>30</td>
<td>e=15 mm</td>
</tr>
<tr>
<td>P30-E25-1,2</td>
<td>Partial</td>
<td>4 partial layers</td>
<td>30</td>
<td>e=25 mm</td>
</tr>
<tr>
<td>P30-E40-1,2</td>
<td>Partial</td>
<td>4 partial layers</td>
<td>30</td>
<td>e=40 mm</td>
</tr>
<tr>
<td>P60-E0-1,2</td>
<td>Partial</td>
<td>6 partial layers</td>
<td>60</td>
<td>e=0 mm</td>
</tr>
<tr>
<td>P60-E15-1,2</td>
<td>Partial</td>
<td>6 partial layers</td>
<td>60</td>
<td>e=15 mm</td>
</tr>
<tr>
<td>P60-E25-1,2</td>
<td>Partial</td>
<td>6 partial layers</td>
<td>60</td>
<td>e=25 mm</td>
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<tr>
<td>P60-E40-1,2</td>
<td>Partial</td>
<td>6 partial layers</td>
<td>60</td>
<td>e=40 mm</td>
</tr>
<tr>
<td>FP-E0-1,2</td>
<td>Non-uniform</td>
<td>1 full layer and 2 partial layers</td>
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<td>e=0 mm</td>
</tr>
<tr>
<td>FP-E15-1,2</td>
<td>Non-uniform</td>
<td>1 full layer and 2 partial layers</td>
<td>-</td>
<td>e=15 mm</td>
</tr>
<tr>
<td>FP-E25-1,2</td>
<td>Non-uniform</td>
<td>1 full layer and 2 partial layers</td>
<td>-</td>
<td>e=25 mm</td>
</tr>
<tr>
<td>FP-E40-1,2</td>
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<td>-</td>
<td>e=50 mm</td>
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### Table 2. Test results of specimens under concentric axial load

<table>
<thead>
<tr>
<th>Specimen</th>
<th>$P_1$ (kN)</th>
<th>$\delta_1$ (mm)</th>
<th>$P_2$ (kN)</th>
<th>$\delta_2$ (mm)</th>
<th>$\delta_3$ (mm)</th>
<th>$\mu$</th>
<th>Failure mode</th>
</tr>
</thead>
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<tr>
<td>F-E0-1</td>
<td>771</td>
<td>1.1</td>
<td>1542</td>
<td>9.1</td>
<td>-</td>
<td>8.9</td>
<td>I</td>
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<tr>
<td>F-E0-2</td>
<td>757</td>
<td>1.1</td>
<td>1612</td>
<td>9.7</td>
<td>-</td>
<td>8.9</td>
<td>I</td>
</tr>
<tr>
<td>FP-E0-1</td>
<td>790</td>
<td>1.3</td>
<td>1450</td>
<td>8.3</td>
<td>-</td>
<td>6.9</td>
<td>I</td>
</tr>
<tr>
<td>FP-E0-2</td>
<td>778</td>
<td>1.2</td>
<td>1414</td>
<td>8.5</td>
<td>-</td>
<td>6.9</td>
<td>I</td>
</tr>
<tr>
<td>P30-E0-1</td>
<td>816</td>
<td>1.4</td>
<td>1375</td>
<td>8.7</td>
<td>-</td>
<td>7.1</td>
<td>I</td>
</tr>
<tr>
<td>P30-E0-2</td>
<td>781</td>
<td>1.5</td>
<td>1378</td>
<td>11.8</td>
<td>-</td>
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<tr>
<td>P60-E0-1</td>
<td>766</td>
<td>1.3</td>
<td>987</td>
<td>9.7</td>
<td>-</td>
<td>8.1</td>
<td>I</td>
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<tr>
<td>P60-E0-2</td>
<td>760</td>
<td>1.2</td>
<td>893</td>
<td>10.8</td>
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<td>I</td>
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<td>P-E0-1</td>
<td>614</td>
<td>0.9</td>
<td>681</td>
<td>1.2</td>
<td>1.6</td>
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<td>-</td>
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<tr>
<td>P-E0-2</td>
<td>601</td>
<td>0.9</td>
<td>664</td>
<td>1.2</td>
<td>1.5</td>
<td>1.7</td>
<td>-</td>
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Note: The failure mode “I” indicates FRP rupture failure.
Table 3. Test results of specimens under eccentric axial load

<table>
<thead>
<tr>
<th>Specimen</th>
<th>$P_1$ (kN)</th>
<th>$\Delta_1$ (mm)</th>
<th>$\delta_1$ (mm)</th>
<th>$P_2$ (kN)</th>
<th>$\Delta_2$ (mm)</th>
<th>$\delta_2$ (mm)</th>
<th>$\Delta_3$ (mm)</th>
<th>$\delta_3$ (mm)</th>
<th>$\mu$</th>
<th>Failure mode</th>
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<tr>
<td>F-E15-1</td>
<td>615</td>
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<td>1053</td>
<td>7.4</td>
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<td>-</td>
<td>5.9</td>
<td>I</td>
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<tr>
<td>F-E15-2</td>
<td>596</td>
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<td>1069</td>
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<td>I</td>
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<td>FP-E15-1</td>
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<td>FP-E15-2</td>
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<td>1.4</td>
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<td>I</td>
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<td>614</td>
<td>3.4</td>
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<td>I</td>
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<td>1.8</td>
<td>0.6</td>
<td>529</td>
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<td>1.5</td>
<td>5.1</td>
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<td>526</td>
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<td>0.7</td>
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<td>I</td>
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<td>FP-E40-1</td>
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<td>235</td>
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<td>0.3*</td>
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<td>-</td>
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</table>

Note: “I” indicates FRP rupture failure; and “II” indicates concrete tension failure. *Lateral displacement data for S60-E40 specimens affected by crushing and spalling of concrete.
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<table>
<thead>
<tr>
<th>Specimen</th>
<th>Experimental compressive strength (MPa)</th>
<th>Analytical compressive strength (MPa)</th>
<th>Average absolute error (%)</th>
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<tr>
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<tr>
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Note: The peak strength of concentrically loaded specimens was predicted by the proposed equations, while the peak strength of eccentrically loaded specimens was predicted by the proposed numerical fiber element method.
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(a) Eccentric loading scheme

\[ \phi = 216 \text{ mm} \]
Clamping plate

\[ \phi = 150 \text{ mm} \]

(b) Eccentric loading mechanism

Specimen
15 mm
Bolts \( \phi = 12 \text{ mm} \)
Adaptor plate
Loading cell 40 mm
Ball joint \( \phi = 25 \text{ mm} \)
Bottom plate \( t = 25 \text{ mm} \)
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