Multiple Fermi pockets revealed by Shubnikov-de Haas oscillations in WTe2

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Abstract
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Keywords
wte2, pockets, multiple, revealed, fermi, shubnikov, de, haas, oscillations

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Multiple Fermi pockets revealed by Shubnikov-de Haas oscillations in WTe$_2$
Multiple Fermi pockets revealed by Shubnikov-de Haas oscillations in WTe$_2$

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**Abstract** – The recently discovered non-saturating and parabolic magnetoresistance and the pressure-induced superconductivity at low temperature in WTe$_2$ imply its rich electronic structure and possible practical applications. Here we use magnetotransport measurements to investigate the electronic structure of WTe$_2$ single crystals. A non-saturating and parabolic magnetoresistance is observed from low temperature to high temperature up to 200 K with magnetic fields up to 8 T. Shubnikov-de Haas (SdH) oscillations with beating patterns are observed, the fast Fourier transform of which reveals three oscillation frequencies, corresponding to three pairs of Fermi pockets with comparable effective masses, $m^* \sim 0.31 \, m_e$. By fitting the Hall resistivity, we infer that they can be attributed to one pair of electron pockets and two pairs of hole pockets, together with nearly perfect compensation of the electron-hole carrier concentration. These magnetotransport measurements reveal the complex electronic structure in WTe$_2$, explaining the non-saturating magnetoresistance.

The peculiar magnetoresistance of the ditelluride WTe$_2$ has attracted intensive research. Extremely large magnetoresistance (XMR) has been measured \cite{1}, suggesting possible applications at low temperatures in high magnetic field and a new avenue for magnetoresistivity. While XMR has also been observed in bismuth \cite{2} and graphite \cite{3}, the magnetoresistance in these materials saturates with increasing field and deviates from a parabolic magnetoresistance (MR) behaviour \cite{3,4}. In addition to XMR, angle-dependent studies revealed that WTe$_2$ also has a large longitudinal linear magnetoresistance \cite{5}. The demonstration of pressure-induced superconductivity in WTe$_2$ \cite{6,7}, further highlights the rich electronic structure that makes this material so interesting.

First-principles calculations suggest the presence of small electron and hole pockets along the Γ-X direction in the Brillouin zone, such that WTe$_2$ is a semimetal \cite{1}. The nearly perfect electron-hole ($n$-$p$) compensation with large carrier mobility in WTe$_2$ has consequently been put forward as the origin of the extremely large and perfectly parabolic MR \cite{1}. A recent angle-resolved photoemission spectroscopy experiment has revealed approximately same-sized electron and hole pockets along the Γ-X direction at low temperature, which supports the idea that the carrier compensation leads to the XMR \cite{8}. In both works, only two pairs of Fermi pockets are reported. We note, however, that the first-principles calculations show that the valence band along the Γ-X direction consists of multiple bands, which may result in multiple hole pockets \cite{1,9}. In addition, a potential second set of electron and hole pockets may form along the Z-U direction, which is parallel to the Γ-X direction but with different $k_z$ \cite{1}. Therefore, it is very crucial to investigate the details of the electronic structure and discern whether extra Fermi pockets are present, and then determine whether the extra electron and hole pockets would affect the $n$-$p$ compensation in relation to the non-saturating parabolic MR.
Next to angle-resolved photoemission spectroscopy (ARPES), quantum oscillations form another powerful method to investigate the electronic structure, which has advantages such as very high $k$-space resolution in all three crystallographic directions and high energy resolution. Quantum oscillations has been extensively used in understanding the band structure of metals [10], revealing the origin of high-temperature superconductivity [11], and probing topological surface states [12–15], bulk Rashba materials [16,17], and Dirac semimetals [18,19].

In this work, we have performed magnetotransport measurement on WTe$_2$ single crystals at various temperatures and magnetic fields. In addition to the observation of large and non-saturating MR in the temperature range between 2.5 and 200 K and in the magnetic field up to 8 T, we observed Shubnikov-de Haas (SdH) oscillations accompanied by beating patterns, indicative of multiple states. The analysis of the SdH oscillations reveals three pairs of Fermi pockets, all having an effective mass around 0.31 $m_e$. The fit of the low-temperature Hall data indicates that the Fermi pockets can be attributed to one electron band and one hole band, which consist of two pairs of hole pockets, although the electrons and holes are nearly perfectly compensated in WTe$_2$.

The WTe$_2$ single crystals used in this work have needle-like shapes with the $c$-axis perpendicular to the surface. The magnetoresistance measurements were performed in a 9 T physical properties measurement system (PPMS) using the four-probe method. The Hall resistance was measured using the six-probe method. All electrical contacts were prepared at room temperature with silver paste. The magnetic field was perpendicular to the $ab$-plane in the magnetotransport measurements. The sample dimensions for these MR and Hall measurements were $3.83 \times 0.26 \times 0.11$ mm$^3$.

Figure 1 shows the temperature dependence of the resistance from 2.5 to 150 K in various magnetic fields, with the resistance plotted in log scale. The resistance shows a strong response to the magnetic field and we find an increment by more than one order of magnitude at low temperatures and applying a field of 8 T. Interestingly, the corresponding magnetoresistance at high temperature is quite small. While the temperature-dependent resistance at 0 and 2 T magnetic field exhibits metallic behaviour, it has an insulating dependence at low temperature in fields larger than 4 T. The “turn-on” temperatures of the magnetic-field–driven metal-insulator–like transition (defined as the temperature where the first derivative of the magnetoresistance with respect to the temperature equals zero) are given in the inset of fig. 1, which shows a linear dependence on the magnetic field and a slope of 6.5 K/T.

Figure 2(a) shows the magnetoresistance at various temperatures, defined by $MR = (R(B) - R(0))/R(0) \times 100\%$, which shows no sign of saturation up to 8 T. The MR reaches around 1850% at a temperature of 2.5 K in a field of 8 T, which is consistent with fig. 1. Below 10 K, the MR decreases slightly with increasing temperature. Above 10 K, the MR decreases dramatically with increasing temperature. The MR is less than 100% above 75 K. Clear
SdH oscillations are observed at 2.5 K, indicating a large carrier mobility. Figure 2(b) presents a log-log plot of the MR at various temperatures. The linear dependence in fig. 2(b) indicates that parabolic MR behaviour is in accordance with what is reported in ref. [1], and our results show that it can persist up to 200 K.

Now, we use the SdH oscillations to analyze the electronic structure of the WTe₂ used in this experiment. In contrast to the SdH oscillations in other systems with a single Fermi pocket, the SdH oscillations in WTe₂ exhibit a beating pattern as shown in fig. 3(a). This indicates that there are two or more Fermi pockets of similar size which are involved in the SdH oscillations. Figure 3(b) shows an oscillation phase shift caused by the multiple Fermi pockets. Since each band with sufficient mobility will give rise to SdH oscillations that oscillate cosinusoidally as a function of 1/B [17], each oscillation peak in fig. 3(a) can be assigned an integer number which corresponds to an oscillation period. The difference between intercepts on the n-axis reveals the oscillation phase shift.

According to the LK formula, the effective mass of carriers can be obtained by fitting the temperature dependence of the normalized FFT amplitudes with a thermal damping factor, \( R_T = \frac{2\pi k_B T m^*}{\hbar eB} \), where \( k_B \) is the Boltzmann constant, \( T \) the temperature, \( m^* \) the effective mass, \( h \) the reduced Planck constant, and \( e \) the elementary charge. The results are shown in fig. 3(e). Since the oscillations observed in the measurement are in the interval from 5 to 8 T, the value of the magnetic field \( B \) is set to 2 T. The Fermi pockets with frequencies \( F_1, F_2, \) and \( F_3 \) are defined as the \( \alpha, \beta, \) and \( \gamma \) Fermi pockets, which are indicated by red, blue, and green dashed lines, respectively. Figure 3(d) shows the second derivative, \( d^2 R_{xx}/dB^2 \), as a function of the magnetic field on the reciprocal scale. The period of the oscillations is visualized by the dash-dotted lines and the solid lines. It can be seen that the period between two solid lines is different from the period between two successive dash-dotted lines. This suggests that the regime between the two solid lines is the node position of the beating pattern. The solid red line is a qualitative fit of the Lifshitz-Kosovich (LK) formula with one electron band and one hole band, as discussed in the two-band model below.

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to 6.5 T. The effective masses for the $\alpha$, $\beta$ and $\gamma$ Fermi pockets yielded by the fits are 0.304, 0.322, and 0.313 $m_e$, respectively.

Now, we discuss the possible origin of the three pairs of Fermi pockets. According to the first-principles calculations, WTe$_2$ is a semimetal with a pair of small electron and hole pockets along the $\Gamma$-X direction in the Brillouin zone, and a potential second set of electron and hole pockets that may form along the $Z$-$U$ direction, which is parallel to the $\Gamma$-X direction but with different $k_z$ [1]. We also note that the valence band along the $\Gamma$-X direction consists of multiple bands [1,9], which may result in multiple hole pockets. In our SdH oscillation measurements, the sizes of the Fermi pockets which are calculated using $A_F = \pi k^2 F = 2eF/h$ are $A_F^e = 0.00953 \, \text{Å}^{-2}$, $A_F^h = 0.00664 \, \text{Å}^{-2}$, and $A_F^\alpha = 0.00953 \, \text{Å}^{-2}$, respectively. Here, $F$ is the frequency of the SdH oscillations, $k_F$ is the Fermi wave vector, and $A_F$ is the cross-sectional area of the Fermi pocket. The small size of the Fermi pockets is consistent with the features of a semimetal and agrees with the ARPES results.

To identify the carrier types of the Fermi pockets, the Hall resistivity ($\rho_{xy}$) was measured up to 8 T from low temperature to room temperature, as shown in fig. 4(a). The negative and linear $\rho_{xy}$ above 200 K indicates that the dominant carrier is of n-type. This is in agreement with the fact that at high temperature, the electron pockets dominate the conduction according to the ARPES experiments [8]. The $\rho_{xy}$ is non-linear at low temperature, however, which indicates that at least two types of carriers are at play. We fit $\rho_{xy}$ at 5 K with using a two-band model, where $\rho_{xy} = \frac{\beta(\mu_1 n_1 + \mu_2 n_2) + (\mu_1 \gamma n_1 + \mu_2 \gamma n_2)}{eB(\mu_1 n_1^2 + \mu_2 n_2^2)}$. Here, $n_1$ and $n_2$ are the carrier densities, and $\mu_1$ and $\mu_2$ are the carrier mobilities for band 1 and band 2, as described below. We have substituted the carrier density calculated from the SdH oscillation, $n = (1/3\pi^2)(2eF/h)^{3/2}$ and found one hole band (band 1) with carriers from the $\alpha$ and $\beta$ pockets ($n_1 = n_\alpha + n_\beta = 1.79 \times 10^{19} \, \text{cm}^{-3}$, where $n_\alpha = 1.33 \times 10^{19} \, \text{cm}^{-3}$ and $n_\beta = 0.658 \times 10^{19} \, \text{cm}^{-3}$, respectively), and one electron band (band 2) with carriers from the $\gamma$ pocket, $n_2 = n_\gamma = -2.42 \times 10^{19} \, \text{cm}^{-3}$, which can give the best fit of the Hall data, yielding $\mu_1 = 1164.5 \, \text{cm}^2\text{V}^{-1}\text{s}^{-1}$ and $\mu_2 = 1045.5 \, \text{cm}^2\text{V}^{-1}\text{s}^{-1}$, respectively. The mobility is very close to the threshold value for observation of SdH oscillations: $\mu B \approx 1$ for a magnetic field from 5 to 10 T. Therefore, the band structure near the Fermi level can be represented as in fig. 4(c), and the three pairs of Fermi pockets are identified as one pair of electron pockets and two pairs of hole pockets. Moreover, the quantum oscillation signal can be qualitatively fit by the LK formula with two oscillation frequencies, one corresponding to the electron pockets, $F_e = F_3$, and the other one corresponding to the two pairs of hole pockets, $F_h \approx (F_1^2 + F_2^2)^{1/2}$, as shown by the solid red line in fig. 3(d). Therefore, the band structure near the Fermi level for the WTe$_2$ measured in this work can be schematically shown in fig. 4(c). The Fermi pockets are schematically represented in fig. 4(d).

Our FFT analysis of SdH oscillations reveals three pairs of Fermi pockets in our samples, instead of the two pairs of pockets reported in previous works [1,8]. Our observations on the multiple Fermi pockets agree with the multiple valence bands obtained by first-principles calculations [1,9]. The fit of the Hall resistivity indicates that one of the three pairs of Fermi pockets consists of electron pockets, while the other two consist of hole pockets, and the carrier densities of electrons and holes are nearly perfectly compensated. Our work suggests that the electronic structure of WTe$_2$ could be even more complicated than the two pairs of electron and hole pockets of approximately the same size, but as long as the electrons and holes are compensated the non-saturating parabolic MR will still persist.

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Additional remark: Three recent works have also revealed multiple Fermi pockets, two from quantum oscillation experiment and one from the ARPES experiment [20–22]. However, the number of Fermi pockets is different in each work including this one, which further indicates the complexity of the electronic structure of WTe$_2$. This may be because the number of Fermi pockets is sensitive to the Fermi level. Future electric gating work may be helpful to clearly clarify the cause.
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