On a CPG-based Hexapod Robot: AmphiHex-II with Variable Stiffness Legs

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Abstract
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Abstract—Amphibious robots have attracted more and more attention from researchers for their broad applications, while it also brings great challenges in designing appropriate propulsion mechanisms and effective control algorithms. In this paper, we reported a newly designed amphibious hexapod robot-AmphiHex-II. This robot possesses six newly designed variable stiffness legs for adapting various complex environments. This novel design of the variable stiffness leg seamlessly incorporates the advantages of both semi-circular walking legs and the swimming flexible flippers. The legs are constructed by rigid fan-shaped frames which work as walking legs for terrestrial locomotion and protect the contained flexible flippers used for aquatic locomotion during terrestrial operations. The stiffness of legs can be adjusted to an effective degree by adjusting the positions of sliders manually. The effect of variable stiffness on locomotion performance was experimentally investigated. Moreover, in order to achieve a smooth and quick gait transition, a Central Pattern Generator (CPG) neural network was introduced to control the system. Different gait generation strategies on land and underwater were demonstrated. A series of field experiments were carried out to evaluate locomotion performance of the AmphiHex-II for terrestrial and aquatic mobility, and the results demonstrate the advantages of the novel leg design and the control system.

Index Terms—Amphibious robot, Variable stiffness legs, CPG control system, Smooth gait transition.

I. INTRODUCTION

DEVELOPPING an amphibious robot is a challenging and fascinating task which has caught much attention of the researchers worldwide. The essential reason to explain this rising enthusiasm is that the amphibious robots possess a broad foreground for various applications in complex environments. To achieve amphibious locomotion in complex environmental conditions, plenty of research has been conducted to propose and develop various interesting propulsive mechanisms or robotic platforms in recent years. A biomimetic method has been used to develop numerous innovative robots. Two representative cockroach-inspired robots, AUQA and RHex series [1, 2], possess outstanding terrestrial locomotion performance. AUQA2 with replaceable flipper legs has been developed to transition between locomotion modes [3]. Snake-like robots, such as ACM-R5 [4], can propel on land and underwater by undulating their bodies, which are another representative amphibious robots [4-6]. Salamander amphibious robot (Salamander Robot) can utilize body undulation and limb walking to transit between terrestrial and aquatic locomotion [7, 8]. Also, a turtle-like robot was designed with a spherical body and four legs with two Degrees of Freedom (DOF), and it is capable of walking on land and cruising underwater [9]. Apart from these, equal attention has also been paid to develop amphibious robots with multiple propulsion mechanisms [10-12]. For example, AmphiRobot-II can demonstrate fish-like swimming and wheeled crawling with both wheel and fin propulsion [10]; Amphibious ‘Whegs’ possesses a combination of legs and propellers, which enables it a good locomotion performance on rough terrains and underwater [11]. Another interesting design of ‘Ninja legs’ enables an amphibious robot to both walk and swim [12]. Additionally, a wide range of other amphibious robots or platforms have been developed [13-18]. However, there exist several problems in traditional amphibious robots, which affect their overall performance. Firstly, owing to utilizing two sets of propulsion mechanism or complex bionic movements to propel, such designs of multi degrees of freedom always require a complex structure and controlling strategy, which limits the applications of the amphibious robots. Secondly, the walking legs (like RHex series) generate limited thrust when used for swimming underwater, while the flippers are obviously unsuitable for terrestrial locomotion. Thirdly, semi-circular legs lack the flexibility in quick turning, and it is only effective in one direction of rotation [19].

To achieve the initial attempt at overcoming the existing problems described above, we had proposed and developed a dynamic hexapod amphibious robot before, AmphiHex-I, with actively transformable flipper-leg composite propulsion mechanisms consist of limit segments [20], since the hexapod locomotion mode has been adopted in many wild robots due to their stronger adaptability to dynamic unknown environments and stability [2], [11], [21-24]. Leg design of this version aimed to incorporate the advantages of semi-circular leg on walking [25, 26] and flipper on swimming underwater [27]. AmphiHex-I can swim underwater and propel on various complex terrains with a good locomotion performance [28-31]. However, the active deformation process from the flexible flipper to the rigid semicircular leg brings more DOFs. And the frail structure of the flipper legs reduce the robot stiffness and cannot protect it from the
obstacles efficiently. Additionally, the active deformation process reduces the flexibility of robot apparently. Thus, when it comes to the turning case, the locomotion of Amphihex-I with curved leg is poor. When the leg counter-rotates in the opposite direction from its original walking mode, the leg behaves like a straight rod and generates great impact, which is absolutely inefficient for locomotion.

For the purpose of a simple robotic configuration, simple control strategy of locomotion and effective locomotion both in terrestrial and underwater maneuvering. Thus, we proposed a new version -Amphihex-II, a hexapod robot with a single, rotary actuator each leg. The highlight of this version is the design of variable stiffness leg, which seamlessly combines the flexible flipper with the rigid fan-shaped leg structure in one propulsion mechanism. This simple multiple leg structure enables Amphihex-II to propel on sandy, muddy terrains, and to swim underwater with an effective performance simultaneously. Rigid fan-shaped leg structure works when the robot conducts the terrestrial operations, while the flexible flipper works effectively when the robot passes through loose, muddy terrains and swim underwater. Besides, this new leg structure makes Amphihex-II easy to pass through the transitional terrains fro m underwater to land. Moreover, the application of the CPGs in the control system benefits the smooth transition between various established gaits, which can consequently improve locomotion performance. The mechanically simple structure ensures the Amphihex-II robot to achieve a variety of locomotion tasks, including walking, running, quick turning, swimming, climbing stairs and pass through amphibious terrains easily.

The reminder of the paper is listed below. Section II presents the detailed design of the Amphihex-II, particularly the variable stiffness leg structure. Section III presents the CPG control system. Section IV presents the application of CPGs in gait generation and transition on land and underwater. Sections V presents the experiments on various terrains and underwater with variable stiffness legs, where the influence of variable stiffness on locomotion performance was discussed. Conclusion remarks and future work are presented in Section VI.

II. AMPHIHEX-II WITH VARIABLE STIFFNESS LEGS

A. Design Approach of Variable Stiffness Leg

Figure 1 displays the configuration of Amphihex-II and structure of variable stiffness leg. The novelty of this newly designed leg reflects on the following aspects: Firstly, this leg design seamlessly incorporates the advantages of a semicircular leg and a flexible flipper, which enables Amphihex-II to achieve amphibious locomotion with only one set of propulsion mechanism. As shown in Figure 1a, the legs are constructed by rigid fan-shaped frames which work as walking legs for terrestrial locomotion and protect the contained flexible flippers used for aquatic locomotion during terrestrial operations. Secondly, fan-shaped leg structure is effective since it provides the advantages of traditional semi-circular walking legs in both two directions, the problem existing in the counter-rotate case of traditional semi-circular walking legs can be solved, which can benefit both turning and backward motions. And the rolling movement of the fan-shaped legs reduces the impact forces that are generated from the contact with ground. Thirdly, the simple structure and motions of legs with only one DOF apparently lead to an easy control strategy. Besides, the sliders are designed for adjusting the compliance of the flexible flipper to adapt to diverse environments.

In this study, tripod gait is usually adopted for walking therefore three of the legs must be able to support the weight of the robot, which is roughly 14 kg with the batteries. For robustness consideration, we designed the leg structure with enough strength so that even one leg can bear the weight of the whole robot. Reducing the mass whilst maintaining the stiffness of the leg appears the primary target of leg structure design, so we chose carbon fiber material to make up the leg frame. The legs with lightweight reduce the motor drain power and energy loss. Also the legs need to be slender so that the drag profile in the direction of the water flow is low. The fan-shape plates are fit parallel to the direction of water flow. Since the plates are slender, legs can easily dig into the soft terrains. Besides, we have added the supporting plates to increase the area of contact between the legs and the terrain and also strengthen the whole structure.

As illustrated in Figure 1a, the main structure of the leg contains fan-shape leg frame, bearing sleeve, and flexible flipper made by a thin steel plate (0.3 mm). In order to achieve variable stiffness, we have set 5 adjustable positions for sliders on the leg frame. By adjusting the position of the sliders (from position 1 to 5) and fixing them with screws or dowels manually, the leg could possess five kinds of stiffness, which allows Amphihex-II to adapt to various complex environments. The interval distance between two adjacent positions is 25 mm. The angel $\alpha$ of the fan-shape leg structure is designed as 60°. Near the middle position of the leg, two support shafts were added to strengthen the structure and protect the leg from break when subjected to severe impacts.

The leg stiffness relies on the position of sliders. As shown in Figure 1b, the slider position divides the whole leg into two parts, the rigid part and the flexible part. As the flexible
flipper is slender, and the strain condition of the flexible flippers during locomotion can be simplified, so we assumed the flexible flipper as a tip-loaded cantilever beam. Based on the Euler-Bernoulli beam theory [32], the stiffness of the flexible flipper and the geometric boundary conditions are given by:

\[ K = \frac{3EI}{L^3}, \quad I = \frac{bh^3}{12} \]  

(1)

\[ V(x) = \frac{P}{EI}x^2 - \frac{3PL}{2EI}(3L - x) \]  

(2)

where \( K \) denotes the stiffness, \( E \) denotes Young’s modulus of the flipper (65 Mn steel), which is 198.6 GPa, \( I \) denotes moment of inertia; \( L \) denotes the length of the flexible part; \( b \) denotes the width of the flexible flipper, which is 40 mm in this study; \( h \) denotes the thickness of the flipper; \( V(x) \) denotes the lateral deflection at a certain position \( x \) to the fixed point; \( P \) denotes the force pressed at the terminal of flipper. According to equation (1), the stiffness for \( P_2 \), \( P_3 \), \( P_4 \) and \( P_5 \) cases are 2, 4.6, 15.6 and 124 times that of \( P_1 \) case, which can be considered as small stiffness, medium stiffness, large stiffness and nearly rigid case, respectively. Also, as shown in Figure 1b, flipper in \( P_1 \) case possesses the highest deflection under the same forces. The distance between the shaft and flipper is 10 mm, which means the shafts hardly interfere the motion of the flipper unless an overlarge deflection appears. In fact, the interference did not be observed during the underwater experiments in Section V.

B. Configuration of AmphiHex-II

One major objective on mechanical design of AmphiHex-II, as shown in Figure 1a, is to improve the frame durability (both in resistance to abrasion and impact) and reduce the overall robot dimension and the weight. Aluminum alloy is chosen to make up the body, and plastic material is chosen to make up the cover. A notable difference is that the dimension (510 x 330 x 10 cm) of AmphiHex-II’s frame is much smaller than the AmphiHex-I’s frame (795 x 388 x 90 cm). As shown in Figure 1a, six motors are placed alternately to reduce the width and make it easy to install. Lateral inter-leg distances are identical, but longitudinal inter-leg distances are slightly greater to fit the internal components. Maxon DC 268219 brushed motors (24 V, 60 W, 8050 rpm, 85.6 mNm, and a 66:1 gear ratio) were chosen as the actuators for its large output torque. Impressed by the tiny volume, we selected the Elmo series motor drive to match our Maxon motors. The upper layer of our control system is a controller board that relays communication between a central CPU (STM 32) and the motor drives, all the communication is conducted through CAN communication protocol. The controller handles the communication of six motors, and the encoders provide the feedbacks of the positions, currents and voltages of motors every 10 ms, which is convenient for a real-time control. We have used two lithium batteries (24 V, 12 Ah) to match our power needs that support six brushed motors and the whole controllers. Besides, the body frame possesses excellent waterproof performance by applying the seal ring between the body and cover, seal rings have also been applied between the walls and the modules and inside the modules. The mass of AmphiHex-II matches approximately to the displacement of robot underwater. Since AmphiHex-II has not equipped sensors to discriminate different terrains at present, we use a remote (RS 232 remote module) to adjust locomotion gait to adapt the environment manually. Thus, in this design, AmphiHex-II can perform various types of maneuvering and swim in water by switching the locomotion gaits. Especially, AmphiHex-II can operate with good locomotion performance when in a backward state, which improves the flexibility of the robot. The comparison of physical specifications of two versions is listed in Table. I.

### Table. I  COMPARISON OF PHYSICAL SPECIFICATIONS

<table>
<thead>
<tr>
<th>Attributes</th>
<th>AmphiHex-II</th>
<th>AmphiHex-I</th>
</tr>
</thead>
<tbody>
<tr>
<td>Size (mm)</td>
<td>510 (L)x330 (W)x100 (H)</td>
<td>795 (L)x388 (W)x90 (H)</td>
</tr>
<tr>
<td>Total weight</td>
<td>14 kg</td>
<td>19 kg</td>
</tr>
<tr>
<td>Ground clearance</td>
<td>120 mm</td>
<td>150 mm</td>
</tr>
<tr>
<td>Length of legs</td>
<td>175 mm</td>
<td>200 mm (curved status)</td>
</tr>
<tr>
<td>Width of legs</td>
<td>50 mm</td>
<td>60 mm</td>
</tr>
<tr>
<td>Weight of legs</td>
<td>0.260 kg</td>
<td>0.324 kg</td>
</tr>
<tr>
<td>Appearance</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

III. CPG-BASED CONTROL SYSTEM

The seamless integration of the flexible flipper and the rigid leg provides high ability for the smooth gait transition in various amphibious environments. In order to achieve a smooth and quick gait transition, the CPG control strategy was chosen for the robot control system. Since CPG has been widely used in robot control, and the rhythmic actions of animals (running, swimming, flying, etc.) produced by biological CPGs can be simulated by coupled nonlinear oscillators [33-36]. Until now, many nonlinear oscillators [37, 38] have been proposed in modeling CPGs for motion control of robots. Among these oscillators, Hopf oscillator is adopted as the pattern generator to build a CPG model for the locomotion control of our robot.

A. Application of Hopf Oscillator

Hopf oscillator model is adopted owing to its prominent features: simple model structure, less required parameters, and stable control system. The harmonic output pattern of Hopf oscillator model has a clear relationship with its parameters that facilitates the easy shaping of the output by modulating corresponding parameters [39]. In this study, the rotary motion of each leg has only one degree of freedom. Thus, rotary speed and the phase of motion come out to be the most significant parameters to be shaped. The Hopf oscillator model can perfectly shape these two parameters that the motion of leg required and generate stable and smooth outputs. The Hopf oscillator model is defined as the following nonlinear differential equations:
B. Analysis and Settings of CPG Parameters

Oscillators keep an opposite phase. By changing values of oscillation.

And oscillator. Multiple couplings imposed on one oscillator i

Terms. Thus, the state vector of the i th Hopf oscillator (X)
can be achieved by a linear combination of other coupling

Where u,i, denotes the output control signals

For three legs of the left

C. CPG-based Control Structure of AmphiHex-II

AmphiHex-II is driven by six motors, so six oscillators are required to generate the locomotion gaits for six legs. As we know, coupling connections between oscillators determine the CPG model. In order to achieve a fast transition performance, we adopt the mutual coupling method, although it requires a higher computational cost. Also, we need to decide the structure of CPGs. When more oscillators are involved, there exist some topological structures of CPGs, which include the chain type, the ring type, the radial type, the fully connected, and the hybrid type. The combination of several structures is a popular approach to a new stable state.

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We can see from Figure 2 that oscillator 1 to 6 correspond to Leg 1 to 6, respectively. Six oscillators are divided into three groups: the front group, the middle group and the rear group. On each side, there are three oscillators that are used to control one side legs, and the oscillators are coupled with the front one with the radial type. Each side can be controlled independently, and only oscillators in the same group have mutual couplings. Besides, an initial zero phase of each oscillator is set to achieve a synchronous start. The locomotion control for left side motion of legs can be expressed as follows:

\[ y_i(t) = u_i, \quad i = 1, 2, 3 \]  

\[ \dot{X}_i = F(X_i) + \varepsilon \begin{bmatrix} u_i \sin \phi_{ij} + v_i \cos \phi_{ij} \end{bmatrix}, i = 2, 3 \]  

Where i denotes the serial number of oscillator, and \( y_i(t) \) denotes the output control signals \( u_i \), for three legs of the left side. The equations that express the control for right side are in a similar form.

Figure 2. CPG-based motion control structure of AmphiHex-II.
IV. GAIT GENERATION AND TRANSITION OF AMPHIHEX-II

In this section, we will introduce the CPG based control method in gait generation and transition. Different strategies in terrestrial and underwater gait generation are also described.

A. Relationship between CPG Outputs and Leg Motions

Before introducing the gait generation strategies, relationship between outputs of oscillators and control signals of motors needs to be demonstrated. Firstly, we have presented the relationship of CPG signals and leg motion on land and underwater. As shown in Figure 3a, if the leg turns clockwise on land, first \( P \) touches the ground and \( Q \) refers to the lift-off. So the rotational circle has been divided into two phase components: the swing phase (\( \theta_1 \)) and the support phase (\( \theta_2 \)). As demonstrated in Section II, the angle \( \alpha \) of fan-shaped frame is 60° and the motion from \( P \) to \( Q \) is a rolling process, so we can obtain that \( \theta_2 \) is 90°. Since time consumption of these two phases are both \( T/2 \), in order to achieve a continuous motion, the rotational speed of leg in the swing phase requires to be set three times as the speed in the support phase. When the robot is swimming underwater, the legs propel like fish flipper. As shown in Figure 3b, the swing process can also be divided into two components: the up-stroke process and down-stroke process. In this case, the angle of \( \theta_0 \) denotes the swing amplitude which is set 30° in this study, and \( \Phi \) denotes the offset phase that represents the start position of legs in different gaits underwater. Point \( M \) and \( N \) denote two boundary positions of the up-stroke and down-stroke, respectively.

![Figure 3. Relationship of CPG signal and leg motion on land and underwater (a) Phase components of one locomotion period on land. ‘SW’ denotes the swing phase and ‘SUP’ denotes the support phase; (b) Phase components of one locomotion period underwater. ‘US’ denotes the up-stroke process and ‘DS’ denotes the down-stroke process.](image)

As described in Section III, the whole control system is a nonlinear system, the outputs of CPG are sinusoidal signals. While the locomotion modes of terrestrial and underwater locomotion are different, legs should conduct rotary motions to achieve terrestrial locomotion and oscillating motions to achieve underwater locomotion. So it is essential to establish the relationship between the CPG outputs \( u_i \) and the control signals of motors on land \( L_i(t) \) and underwater \( W_i(t) \), in which \( i \) denotes the serial number of oscillator and the corresponding motor. As shown in Figure 3a, the rising edge of the output signals wave of oscillator corresponds to the support phase and the declining edge corresponds to the swing phase when AmpHiHex-II is walking on land [45]. The crest and the trough of the signals denote the position marked by \( Q \) and \( P \), respectively. And we set point \( P \) as the start position of \( L_i(t) \), which enables six legs to contact with the ground when the robot is ready for terrestrial locomotion, the relationship of \( u_i \) and \( L_i(t) \) can be defined as equation (8). Similarly, as shown in Figure 3b, the rising edge of the wave denote the position marked by \( M \) and \( N \). Since the oscillating amplitude is 30°, the relationship of \( u_i \) and \( W_i(t) \) can be defined as equation (9).

Thus, the relationship between CPG outputs and motors has been established. Two equations are presented as follow:

\[
L_i(t) = \begin{cases} 
\frac{\pi}{4} (1 + \frac{u_i}{A}), & 0 \leq t < \frac{T}{2} \\
2\pi - \frac{3\pi}{4} (1 + \frac{u_i}{A}), & \frac{T}{2} \leq t \leq T 
\end{cases} \quad (8)
\]

\[
W_i(t) = \Phi + \frac{\pi}{6} \frac{u_i}{A}, \quad 0 \leq t \leq T \quad (9)
\]

B. Gait Generation in Various Environments

Before conducting a locomotion, six legs should be ready at a certain position. For all terrestrial locomotion, point \( P \) illustrated in Figure 3a is the start position, as for the aquatic locomotion, the start position is decided by phase \( \Phi \) in different gaits. Parameters \( \varphi_{ij} \) and \( \Phi \) decide the locomotion gait, and \( f \) decides the locomotion speed.

We can establish a matrix expression to describe the phase setting of a terrestrial locomotion gait. Due to limited space of this paper, we only take the expression of tripod gait for example, which can be defined as follow: (where ‘*’ denotes the undefined values)

\[
\varphi_{i,j} = \begin{bmatrix} \pi & 0 & 0 & 0 \\
0 & \pi & 0 & 0 \\
0 & 0 & \pi & 0 \\
-\pi & 0 & \pi & 0 \\
0 & -\pi & 0 & \pi \\
\pi & 0 & \pi & 0 
\end{bmatrix}_{6 \times 6} 
\quad (10)
\]

It is seen from the matrix that Oscillators 1, 3 and 5 possess the same phase, Oscillators 2, 4 and 6 possess the same phase, while phases of these two groups are opposite. When outputs of Oscillators 1, 3, and 5 are in the rising edge, the outputs of Oscillators 2, 4, and 6 are in the declining edge. Thus, according to the relationship of CPG outputs and locomotion phase shown in Figure 3, we can imagine that while one tripod formed by Legs 1, 3 and 5 are rotating in support phase, the other three legs (Legs 2, 4 and 6) are in swing phase rotating rapidly to be ready for the next support phase, which is exactly the tripod gait. Besides the tripod gait, tetrapod gait and hexapod gait will be adopted when the robot needs to cross over the obstacles (such as the stairs) and passing through specific terrains like muddy terrains which require a
large output of torque. Similar to the tripod gait, we can easily get the phase difference expressions of tetrapod gait and hexapod gait.

When the robot is propelling underwater, swimming gaits correspond to a combination of fixed initial phase offset $\Phi$ and different oscillating motions of flippers. Distinctive offset phase $\Phi$ for various underwater locomotion gaits are presented as follow:

$$
\Phi = \begin{bmatrix}
\Phi_{Cruising} \\
\Phi_{Backward} \\
\Phi_{Turning} \\
\Phi_{Diving}
\end{bmatrix} = \begin{bmatrix}
3\pi/2, i=1, 2, 3, 4, 5, 6 \\
\pi, /2, i=1, 2, 3, 4, 5, 6 \\
\pi/2, i=1, 2, 3, \pi/2, i=4, 5, 6 \\
\pi/4, i=1, 2, 3, \pi/4, i=4, 1, 3, 4, 6 \\
3\pi/4, i=1, 2, 3, 5, \pi/4, i=4, 1, 3, 4, 6
\end{bmatrix}
$$

(11)

where $i$ denotes the serial number of legs. And we only define the right turning case in the expression, the definition of left turning case is opposite. $\Phi$ decides the difference of various underwater locomotion gaits. It’s notable that two middle legs oscillate oppositely to the four corner legs (which means $\varphi_{2, j}=0$, $\varphi_{2, j}=\pi$, $j=1, 3, 4, 6$) in these underwater gaits. This setting can considerably reduce the amounts of pitch, roll, and yaw during the cruising and backward swimming processes, and enables the robot to achieve vertical diving and surfacing processes, as shown in Figure 10. With above descriptions, all the gaits both on terrains and underwater can be generated.

C. Gait Transition with the Application of CPG

The smooth transition process among different gaits is the primary contribution of CPGs. By changing the frequency $f$, the locomotion speed can be changed. Smooth transition among various gaits ensures no jerk or discontinuity in the locomotion, which can benefit the locomotion performance.

Through changing the phase difference $\varphi_{1,i}$, and offset phase $\Phi$, the locomotion gait can be changed, all the gait transition processes are based on this principle. Here we take a typical gait transition processes for example: the transition from hexapod to tripod gait. Figure 4 shows the variation of CPG output signals during the transition process. The blue colored signals denote the control signals of the tripod formed by Leg 1, 3 and 5, red colored signals donate the control signals of the tripod formed by Leg 2, 4 and 6. Two changes happened at 8 and 16 s, respectively. This figure illustrates a process that AmphiHex-II starts with a slow hexapod gait ($f=0.5$ Hz), then transits to slow tripod gait and finally accelerates to fast tripod gait ($f=1$ Hz). Signals in 0–8 s illustrate the slow hexapod gait, signals in 8–16 s illustrate the slow tripod gait, and signals in 16–20 s illustrate the fast tripod gait. When $\varphi_{2, 3}, \varphi_{2, 4}$ and $\varphi_{3, 4}$ have been changed to $\pi$, Leg 1, 3 and 5 rotate gradually to achieve an opposite phase to Leg 2, 4 and 6 to form a tripod gait. The whole transition process sustains about 2 periods, and if the locomotion speed is higher, time consumption of this gait transition will be reduced. We can also see from the figure, both the gait transition process and the accelerating process are smooth thanks to the properties of CPG emulated with non-linear oscillators.
B. Locomotion Gaits on Various Terrains

The RHex series are fast on land (0.6 m/s), but their semi-stairs and complex amphibious areas.

Kinds of terrains including ground, grass, sand, mud, slope, evaluated for achieving various gaits and walking on different amphibious environments.

Frames of AmphiHex II provides a smooth transition ability in the seamless integration of variable stiffness flippers and leg circular legs can generate limited thrust underwater. However, and AmphiRobot-II are 0.44 bl/s and 0.64 bl/s, respectively. [10], locomotion performance of AmphiHex-II is comparable. [47]. The reasons can be considered as following aspects: Although the leg length is shorter than previous version, proper stiffness of the new leg design can achieve higher thrust force in the water; there is no doubt that slimmer body of AmphiHex-II, which generates less dragging forces underwater, also contributes to the higher speed. Analyzing the data, we can also draw a primary conclusion that the locomotion speed underwater can be improved by enhancing the stiffness of flipper, which is conformed to our former study results [46]. Compared with some latest generation of robots, such as Salamander-II [48], RHex, and AmphiRobot-II [10], locomotion performance of AmphiHex-II is comparable. The highest swimming speed underwater of Salamander-II and AmphiRobot-II are 0.44 bl/s and 0.64 bl/s, respectively. The RHex series are fast on land (0.6 m/s), but their semi-circular legs can generate limited thrust underwater. However, the seamless integration of variable stiffness flippers and leg frames of AmphiHexII provides a smooth transition ability in amphibious environments.

B. Locomotion Gaits on Various Terrains

AmphiHex-II with variable stiffness legs has also been evaluated for achieving various gaits and walking on different kinds of terrains including ground, grass, sand, mud, slope, stairs and complex amphibious areas.

As mentioned earlier, robots with semi-circular legs usually cannot conduct turning motion easily because semi-circular legs are always not effective in the counter-rotate case. While
Propelling in soft terrains, such as grassy, sandy, soil and muddy terrains, is also a kind of a challenging task for amphibious robot. As mentioned earlier, the slender fan-shape leg makes it easy to dig into the terrains, and the supporting plate increases the contact area, so AmphiHex-II possesses the capability to propelling in soft terrains. Generally, flippers push away the soft medium, the reactive forces generated by the medium support and propel the robot, which benefits the locomotion performance. Especially, when the robot is propelling in sandy substrates, soft soil terrains and muddy terrains, the stiffness of flipper legs has a significant influence on the locomotion. Sandy substrates can be considered as a granular media with rheological characteristics, and behave like an elastic solid below a critical stress and a fluid above the critical stress. A higher stiffness flippers usually can generate a smaller thrust force to destroy the granular media easily. However, the case is more complicated when the robot is propelling in the muddy terrain. As shown in Figure 8b, the experiment was conducted in the muddy terrain with a 25% water content and two cases of the amount of sticking mud on the leg are presented in Figure 8c. We can see from the red frames in Figure 8c that flipper leg with smaller stiffness tends to carry more mud during the whole rotation period, which is inefficient. To conclude, the flexible flipper must be more compliant to reduce the resistance when the robot is propelling in grassy, sandy, soil terrains, so we can adjust the sliders to position 1 on the leg frame as described in Figure 1 to make the flexible flipper much more compliant. While in the sticky muddy terrain, flipper leg with less compliance is more effective for locomotion.

C. Launching and Landing Locomotion

Simple propulsion method while achieving good landing and launching motion is another highlight of AmphiHex-II. As shown in Figure 9.

D. Swimming Underwater

As mentioned earlier, the flexible flippers play the major role in performing underwater movements with high maneuvering ability. Based on the obtained results in Figure 5, we can see that less compliance of flippers lead to higher propelling speed. Although this would require more energy consumption, what our focus is more on the physical speed that the robot can achieve with flipper legs. Thus, during swimming underwater, we should adjust six legs to be less compliant to achieve higher physical speed, so we can adjust the sliders to position 5 on the leg frame. As shown in Figure 10, AmphiHex-II is capable of achieving many maneuvers including turning, cruising, backward swimming, descending and ascending locomotion underwater by conducting different combinations of various directions and phases of the flipper legs propulsion.
According to the presented analysis and discussions, the adoption of appropriate stiffness of flipper legs to adapt to a specific environment has been summarized in Table II. P2 can be an alternative for P1 case, and P3 can be an alternative for P5 case.

<table>
<thead>
<tr>
<th>Environments</th>
<th>Stiffness</th>
<th>Adjustment</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sand, grassland, soft soil</td>
<td>Small</td>
<td>P1</td>
</tr>
<tr>
<td>Amphibious environment (including water, transition areas and land)</td>
<td>Medium</td>
<td>P2</td>
</tr>
<tr>
<td>Aquatic environment and muddy substrates</td>
<td>Rigid</td>
<td>P3</td>
</tr>
<tr>
<td>Rough terrains</td>
<td>No particular requirements</td>
<td></td>
</tr>
</tbody>
</table>

**VI. CONCLUSION REMARKS AND FUTURE WORK**

In this work, we proposed and evaluated the novel design of variable stiffness legs to be used for a CPG-based amphibious robot. These legs allow robot to conduct various amphibious operations: swimming, walking, passing through transition area or soft terrains and climbing over obstacles. And these legs provide swimming underwater on the surface and maneuverability underwater. We have also verified these legs are suitable for walking on a variety of terrains types by adjusting the stiffness. Except the versatility, achieving amphibious locomotion with only one set of propulsion mechanism and simple control strategy are highlights of this work. Thanks to the introduction of CPG, transition between various gaits is smooth and quick.

The adjustment of the variable stiffness legs to adapt to different environments is manually done in this study. Hence, driving mechanisms for the adjustment of the sliders, and more sensors will be applied in AmphipHex-II in the future to achieve autonomous and adaptive amphibious locomotion, which would also broaden the field applications of AmphipHex-II.

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**REFERENCES**


