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Molecular dynamics simulations of peptides containing an unnatural amino acid: Dimerization, folding, and protein binding

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Abstract

We have performed molecular dynamics (MD) simulations to study the dimerization, folding, and binding to a protein of peptides containing an unnatural amino acid. NMR studies have shown that the substitution of one residue in a tripeptide β -strand by the unnatural amino acid Hao (5-HO₂CCONH-2-MeO-C₆H₃-CO-NHNH₂) modifies the conformational flexibility of the β -strand and the hydrogen-bonding properties of its two edges: The number of hydrogen-bond donors and acceptors increases at one edge, whereas at the other, they are sterically hindered. In simulations in chloroform, the Hao-containing peptide 9 (i-PrCO-Phe-Hao-Val-NHBu) forms a β -sheet-like hydrogen-bonded dimer, in good agreement with the available experimental data. Addition of methanol to the solution induces instability of this β -sheet, as confirmed by the experiments. MD simulations also reproduce the folding of the synthetic peptide 1a (i-PrCO-Hao-Ut-Phe-Ile-Leu-NHMe) into a β -hairpin-like structure in chloroform. Finally, the Hao-containing peptide, Ac-Ala-Hao-Ala-NHMe, is shown to form a stable complex with the Ras analogue, Rap1 A, in water at room temperature. Together with the available experimental data, these simulation studies indicate that Hao-containing peptides may serve as inhibitors of β -sheet interactions between proteins.

Keywords

binding, simulations, peptides, molecular, containing, dynamics, unnatural, amino, acid, dimerization, folding, protein, CMMB

Disciplines

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Molecular Dynamics Simulations of Peptides Containing an Unnatural Amino Acid: Dimerization, Folding, and Protein Binding

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ABSTRACT We have performed molecular dynamics (MD) simulations to study the dimerization, folding, and binding to a protein of peptides containing an unnatural amino acid. NMR studies have shown that the substitution of one residue in a tripeptide β -strand by the unnatural amino acid Hao (5-HO₂CCONH-2-MeO-C₆H₃-CO-NHNH₂) modifies the conformational flexibility of the β -strand and the hydrogen-bonding properties of its two edges: The number of hydrogen-bond donors and acceptors increases at one edge, whereas at the other, they are sterically hindered. In simulations in chloroform, the Hao-containing peptide **9** (i-PrCO-Phe-Hao-Val-NHBu) forms a β -sheet-like hydrogen-bonded dimer, in good agreement with the available experimental data. Addition of methanol to the solution induces instability of this β -sheet, as confirmed by the experiments. MD simulations also reproduce the folding of the synthetic peptide **1a** (i-PrCO-Hao-Ut-Phe-Ile-Leu-NHMe) into a β -hairpin-like structure in chloroform. Finally, the Hao-containing peptide, Ac-Ala-Hao-Ala-NHMe, is shown to form a stable complex with the Ras analogue, Rap1 A, in water at room temperature. Together with the available experimental data, these simulation studies indicate that Hao-containing peptides may serve as inhibitors of β -sheet interactions between proteins. *Proteins* 2004;54:116–127.

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Key words: computer simulation; molecular dynamics; unnatural amino acid; peptide dimerization; peptide folding; peptide-protein binding

INTRODUCTION

The formation of β -sheets involving β -strands from two proteins constitutes an important form of molecular recognition based on hydrogen bonding between amide groups, and represents a general mode of protein–protein interaction.¹ Thus, the formation of intermolecular β -sheets is central to many processes of protein oligomerization, protein aggregation, and peptide–protein binding. For example, HIV-1 protease, an enzyme that plays a critical role in the maturation of HIV (the virus causing AIDS), forms a dimer with β -sheet interactions between two monomers.² A particularly noteworthy example of β -sheet formation between different proteins is the binding of the

Ras oncoproteins to their kinase receptors. Ras oncoproteins act as molecular switches that activate the serine/threonine kinase C-Raf1 (Raf) by binding to its Ras-binding domain (RBD).^{3,4} When oncogenically active Ras exists in the β -sheet form, this results in a constitutive activation of Ras-mediated signaling events and promotion of aberrant growth in more than 30% of all human tumors.⁵ Proteins related to neurodegenerative diseases, such as prion disease,⁶ form insoluble aggregates that are rich in β -sheets. The protease-resistant pathogenic prion protein, PrP^{Sc}, is rich in β -sheets and forms amyloid fibrils, whereas its isoform in healthy cells, the cellular prion protein, or PrP^C, has a flexible N-terminal domain and a C-terminal domain that is largely α -helical.

The edge of a β -strand involved in β -sheet contacts has an alternating array of hydrogen-bond donors and acceptors. Chemical decoys that can mimic these hydrogen-bonding edges provide possibilities for developing new drugs that can block, modulate, or mediate β -sheet interactions between proteins. Peptide derivatives that can block the dimerization of HIV-1 protease⁷ and the self-assembly of β -amyloids^{8,9} have been reported. Nowick and coworkers^{10–13} recently reported the combination of hydrazine, 5-amino-2-methoxybenzoic acid and oxalamide groups with natural peptides that can form a variety of β -sheet-like structures. The combination of hydrazide, 5-amino-2-methoxybenzoic acid and oxalamide groups called Hao can be viewed as an unnatural amino acid that mimics the hydrogen-bonding functionality of one of the edges of a tripeptide β -strand [Fig. 1(A)]. By NMR studies, Nowick et al.¹² found that the tripeptide **9** [i-PrCO-Phe-Hao-Val-NHBu; Fig. 1(B)] forms a β -sheet-like hydrogen-bonded dimer in CDCl₃ solution (with a dimerization constant of about 10⁶ M^{−1}), whereas the control tripeptide **11** (i-PrCO-

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containing peptides do not induce the formation of multiple-strand β -sheets, because the aromatic ring of Hao inhibits β -sheet formation at the other edge of the β -strand. Therefore, Nowick et al.¹² anticipated that Hao-containing peptides may also serve as antagonists to block β -sheet interactions between proteins. They illustrated this through a docking study of Ac-Ala-Hao-Ala-NHMe to the Ras analogue Rap1 A protein.

Molecular dynamics (MD) simulations have been proven successful at reproducing the folding of a number of peptides and have provided insight into some of its principles.^{14–24} Here, we present a series of MD studies of the

TABLE I. Overview of the MD Simulations of the Dimerization, Folding, and Binding of the Hao-Containing Peptides

Simulation label	Solute Peptides/protein	Solvent	Number of Solvent molecules	Temperature [K]	Simulation length [ns]
9 _{dimer}	9 dimer	CHCl ₃	962	303	50
11 _{dimer}	11 dimer	CHCl ₃	654	303	50
9 _{dimer} ^{CH₃OH}	9 dimer	CH ₃ OH/CHCl ₃	115/1033	303	50
1a ₁	1a	CHCl ₃	875	303	100
1a ₂	1a	CHCl ₃	875	303	100
1a ₃	1a	CHCl ₃	875	303	100
Rap1A _{free}	Rap1A	H ₂ O	6618	299	2
Rap1A _{bind}	Rap1 A:Ac-Ala-Hao-Ala-NHMe	H ₂ O	6598	299	2

The three simulations of peptide 1a differ regarding the initial value and strength of the torsional-angle potential energy term for the angle CH22-N-C-N [see Fig. 1 (E)]: Simulations 1a₁ and 1a₃ start with the *trans* conformation, simulation 1a₂ with the *cis* conformation. The strengths of the torsional potential energy term are 33.5 kJ mol⁻¹ for simulations 1a₁ and 1a₂, and 7.11 kJ mol⁻¹ for simulation 1a₃.

dimerization of peptide **9** (i-PrCO-Phe-Hao-Val-NHBu), of the folding of peptide **1a** (i-PrCO-Hao-Ut-Phe-Ile-Leu-NHMe), and of the binding of the peptide Ac-Ala-Hao-Ala-NHMe to the Ras analogue Rap1A, using the GROMOS96 package^{25,26} and the GROMOS96 43A1 biomolecular force field.²⁵ The simulations are summarized in Table I. Results are compared with the available experimental data, and additional information about the structure and function of Hao-containing peptides is provided.

METHODS

MD Simulations

We carried out the simulations and analyses using the GROMOS96 package of programs.^{25,26}

Molecular Model

The molecular models of the unnatural amino acid residue (Hao) and the urea-based turn unit (Ut) were built analogously to building blocks with the same types of groups in the GROMOS96 43A1 force field.²⁵ In this force field, the aliphatic hydrogen atoms are treated, together with the carbon atom to which they are attached as united atoms.²⁶ The force field parameters for Hao and Ut are listed in Tables II and III. The protein, Rap1A, and the natural amino acids in the various peptides were modelled according the standard GROMOS96 43A1 force-field parameters. For solvent chloroform, we used a four-center rigid model by Tironi and van Gunsteren,²⁷ whereas for solvent water, we used the simple point charge (SPC) model.²⁸ After comparing the mixing properties of chloroform and methanol for two different methanol models,^{25,29} we used the standard methanol model of the GROMOS96 43A1 force field²⁵ for the simulation of peptide **9** in the chloroform/methanol mixture. The simulated systems are listed in Table I.

Simulation Setup

For each simulation, the solute was placed at the center of a periodic, truncated octahedral box. The minimum distance from any peptide atom to the square box walls was chosen to be at least 1.8 nm in the initial configuration. We introduced the solvent molecules into the box using a cubic periodic configuration of 216 pre-equilibrated

chloroform or water molecules. The minimum distance between the carbon atom of chloroform or the oxygen atom of water and the non-hydrogen atoms of the solute was set to 0.30 nm and 0.23 nm, respectively. The resulting numbers of solvent molecules in the systems are specified in Table I.

A steepest descent energy minimization of the systems was performed to relax the solute-solvent contacts, whereas the solute atoms were positionally restrained with a harmonic interaction, with a force constant 250 kJ mol⁻¹nm⁻². Next, steepest descent energy minimization of the system without restraints was performed to eliminate any residual strain. The energy minimizations were terminated when the energy change per step became smaller than 0.1 kJ mol⁻¹.

We obtained the initial coordinates of the dimers of the tripeptides **9** [Fig. 1 (B)] and **11** by building a model dimer structure. The initial configuration of peptide **1a** [Fig. 1 (C)] was extended, with all the backbone torsional angles set to 180°. The starting structure for the complex of the Ras analogue Rap1A with the Hao-containing peptide was built from the crystal structure of the Ras-binding domain of the c-Raf1 kinase and the Ras analogue, Rap1A [Protein Data Bank (PDB) code 1gua³¹] by modelling the Hao-containing peptide Ac-Ala-Hao-Ala-NHMe on the complex. All the crystallographically determined water molecules were disregarded. For the dimers of peptides **9** and **11**, and the complex of Rap1A with Ac-Ala-Hao-Ala-NHMe, 200 ps of MD simulation, with distance restraining of the hydrogen-bonded atoms, was performed to relax the complexes, while maintaining the hydrogen bonds. We started the MD simulations by taking the initial velocities from a Maxwellian distribution at 100 K. Solvent and solute were independently weakly coupled to a temperature bath, with a relaxation time of 0.1 ps.³⁰ The systems were also coupled to a pressure bath at 1 atm, with a relaxation time of 0.2 ps, and an isothermal compressibility of 1.0×10^{-3} (kJ mol⁻¹ nm⁻³)⁻¹ for the chloroform simulations, a relaxation time of 0.5 ps, and an isothermal compressibility of 0.7513×10^{-3} (kJ mol⁻¹ nm⁻³)⁻¹ for the water simulations. Bond lengths were constrained using the SHAKE algorithm, with a geometric tolerance of 10^{-4} ,³¹

TABLE II. Force-Field Parameters for the Unnatural Amino Acid Residue Hao

Atom	Description	IAC	Partial charge [e]
N, N1, N9	Amide N	5	-0.28
H, H1, H9	Amide H	18	0.28
C2, C10, C11	Carbonyl C	11	0.38
O2, O10, O11	Carbonyl O	1	-0.38
C3, C8	Aromatic C	11	0.00
C4	Aromatic C	11	0.18
O4	Hydroxyl O	3	-0.36
CH3	Aliphatic CH3-group	14	0.18
C5, C6, C7	Aromatic C	11	-0.10
H5, H6, H7	Hydrogen bound to C	17	0.10
Bond length		b_0 [nm]	K_b [10^6 kJ mol ⁻¹ nm ⁻⁴]
N-N1		0.133	11.8
C10-C11		0.133	11.8
Bond angle		θ_0 [degree]	K_θ [kJ mol ⁻¹]
H-N-N1, H1-N1-N		120.0	390
N-N1-C2		117.0	635
O2-C2-C3		121.0	685
N1-C2-C3		115.0	610
C8-N9-H9		120.0	390
C8-N9-C10		123.0	415
N9-C10-C11		115.0	615
O10-C10-C11, O11-C11-C10		121.0	685
Dihedral angle		$\cos(\delta)$	K_ϕ [kJ mol ⁻¹]
-N-N1-		-1.0	2
-C2-C3-		-1.0	2
-C8-N9-		-1.0	2
-C10-C11-		-1.0	2
Improper dihedral angle		ξ_0 [degree]	K_ξ [kJ mol ⁻¹ degree ⁻²]
N-X-N1-H, N1-C2-N-H1, N9-C8-C10-H9		0.0	0.0510
C2-N1-C3-O2, C10-N9-C11-O10, C11-C10-X-O11		0.0	0.0510

The atom names are defined in Figure 1 (D); the GROMOS96 integer atom code (IAC) defines the Lennard-Jones parameters of the corresponding atoms. Parameters (bond lengths, bond angles, dihedral angles, and improper dihedrals) of carbonyl, amide, benzene, and ether groups (not given) were chosen analogous to GROMOS96 force-field parameters for peptides and noncarbohydrates.²⁵ The functional form of the force field is given in van Gunsteren et al.²⁵ and Scott et al.²⁶

so that the time step for the leapfrog integration could be set to 0.002 ps. For the nonbonded interactions, we used a triple-range method with cutoff radii of 0.8 and 1.4 nm. Outside the longer cutoff radius, we used a reaction field approximation,³² with a relative dielectric permittivity of 5.0 for chloroform and 78.5 for water. Short-range van der Waals and electrostatic interactions were evaluated every time step with a charge-group pairlist. Long-range van der Waals and electrostatic interactions between pairs, at a distance longer than 0.8 nm and shorter than 1.4 nm, were evaluated every fifth time step, at which point the pair list was updated. The center of mass motion of the whole system was removed every 500 time steps, and the trajectory coordinates and energies were saved every 0.5 ps for analysis.

Analysis

A cluster analysis was performed on all the trajectories from the simulations of peptides **9**, **11**, and **1a** with the use of structures saved at 10-ps intervals. Clustering was performed as described in Daura et al.³³ by performing a rotational and translational atom-positional least-squares fit for every pair of structures, using all backbone atoms and calculating the corresponding atom-positional root-mean-square difference (RMSD) for the same set of atoms. The similarity criterion used was an RMSD smaller or equal to 0.06 nm and 0.10 nm, respectively, for the peptides **9/11** and **1a**.

We used as a criterion for the occurrence of a hydrogen bond in a given structure a maximum distance of 0.25 nm

TABLE III. Force-Field Parameters for the Urea-Based Turn Fragment Ut

Atom	Description	IAC	Partial charge [e]
NP, N	Amide N	5	0.00
CG	Aromatic C	11	0.00
CD1, CD2, CE1, CE2, CZ	Aromatic C	11	-0.10
HD1, HD2, HE1, HE2, HZ	Hydrogen bound to C	17	0.10
CH21, CH22, CH23, CH24	Aliphatic CH2-group	13	0.00
CN	Bare C	11	0.36
NC	Bare N	8	-0.36
C	Carbonyl C	11	0.38
O	Carbonyl O	1	-0.38
Bond length		b_0 [nm]	K_b [10^6 kJ mol ⁻¹ nm ⁻⁴]
CH24-CN		0.143	8.18
CN-NC		0.123	16.6
Bond angle		θ_0 [degree]	K_θ [kJ mol ⁻¹]
NP-CG-CD1, NP-CG-CD2, CG-NP-CH21		120.0	780
NP-CH21-CH22, N-CH23-CH24, N-CH22-CH21		109.5	520
CH22-N-CH23		116.0	620
CH22-N-C, CH23-N-C		122.0	700
CH23-CH24-CN		111.0	530
CH24-CN-NC		180.0	401, 244
Dihedral angle		$\cos(\delta)$	K_ϕ [kJ mol ⁻¹]
-NP-CG-		-1.0	2
-NP-CH21-, -N-CH22-, -N-CH23-		-1.0	2
Improper dihedral angle		ξ_0 [degree]	K_ξ [kJ mol ⁻¹ degree ⁻²]
NP-X-CH21-CG, N-CH22-C-CH23, C-N-N-O		0.0	0.0510

The atom names are defined in Figure 1 (E). For further explanation, see footnote, Table II.

between the hydrogen atom and the acceptor atom, and a minimum donor–hydrogen-acceptor angle of 135°.

Interproton distances in the simulations were compared to the experimental nuclear Overhauser enhancement (NOE) intensities. We calculated the former by using r^{-6} averaging over the trajectory structures (where r indicates the actual proton–proton distance), which is the method that corresponds best with the time averaging in the NMR experiment in the case of a small molecule that is tumbling fast compared to internal motions.^{34,35} As we mentioned before, in the GROMOS96 43A1 force field, aliphatic hydrogen atoms are not explicitly treated but are part of united atoms. We thus calculated interproton distances involving the aliphatic hydrogen atoms by defining virtual (for CH₁ and prochiral CH₂) and pseudo (for CH₃) atomic positions for these hydrogen atoms at the time of analysis.²⁶ When comparing the experimental NOE-derived distance with the calculated proton–proton distance, pseudoatom corrections involving equivalent or nonstereo-assigned protons should be included in the upper-bound NOE-derived distances.³⁶

We calculated 3J -coupling constants from the simulations using the Karplus relation:³⁷

$$^3J(H,H) = a \cos^2\theta + b \cos\theta + c. \quad (1)$$

Two sets of parameters a , b , c — $a = 6.40$ Hz, $b = -1.40$ Hz, $c = 1.90$ Hz³⁸ and $a = 7.09$ Hz, $b = -1.42$ Hz, $c = 1.55$ Hz³⁹—were used to calculate $^3J(\text{HN}, \text{HC})$.

RESULTS AND DISCUSSION

Stability of Hao-Containing Peptide Dimers

¹H NMR chemical shift, NOE, and dilution titration studies¹² indicate that Hao derivative **9** [Fig. 1 (B)] forms a remarkably stable β -sheet-like hydrogen-bonded dimer in CDCl₃ solution, while the control peptide **11** (i-PrCO-Phe-Leu-Val-NHBu) self associates very weakly. Backbone atom-positional RMSD of the dimer of peptide **9** with respect to the initial β -sheet structure as a function of time is shown in Figure 2 (lower left panel). At 303.15 K, the dimer structure of **9** in CHCl₃ solution was very stable, with an RMSD value around 0.07 nm with respect to the model-built β -sheet dimer structure. With use of a similarity criterion, a backbone-atom RMSD of less than 0.06 nm, cluster analysis shows that 85% of the trajectory structures belong to the first, most populated cluster. However, some rearrangement of the two chains is observed with respect to the model dimer, especially at the chain termini. The β -sheet structure is characterized by particular NOEs.⁴⁰ The properly averaged interproton distances from simulation are compared with the NOE intensities¹²

Fig. 2. Upper panels: Occurrences of hydrogen bonds as a function of simulation time for the dimer of peptide 9 (left panel) and of peptide 11 (right panel), both in chloroform. A hydrogen bond is assumed to exist if the hydrogen-acceptor distance is smaller than 0.25 nm and the donor–hydrogen-acceptor angle is larger than 135°. Lower panels: Atom-positional RMSD for the backbone atoms from the starting structure of the dimer of peptide 9 (left panel) and the dimer of peptide 11 (right panel).

TABLE IV. Comparison of Experimental NOE Intensities¹²

NOE pair		Simulated distance (r^{-6}) ^{-1/6} [nm]	Pseudoatom correction	Exp. NOE intensity
H atom	H atom			
H-CA(Phe:A)	H-CA(Val:B)	0.236	0.00	S
H-CA(Phe:B)	H-CA(Val:A)	0.236	0.00	S
H-CG2(Val:A)	H-CA(Phe:B)	0.450	0.15	W
H-CG2(Val:B)	H-CA(Phe:A)	0.447	0.15	W
H-CG2(Val:A)	H-CB(Phe:B)	0.524	0.22	W
H-CG2(Val:B)	H-CB(Phe:A)	0.503	0.22	W
H-CG2(Val:A)	HD1(Phe:B)	0.452	0.35	W
H-CG2(Val:B)	HD1(Phe:A)	0.443	0.35	W
H9(Hao:A)	H5(Hao:A)	0.226	0.00	S
H9(Hao:B)	H5(Hao:B)	0.226	0.00	S
H9(Hao:A)	H7(Hao:A)	0.357	0.00	W
H9(Hao:B)	H7(Hao:B)	0.361	0.00	W
H-CA(Val:A)	H(NHBu:A)	0.216	0.00	S
H-CA(Val:B)	H(NHBu:B)	0.217	0.00	S
H-CA(Val:A)	H(Val:A)	0.278	0.00	W
H-CA(Val:B)	H(Val:B)	0.278	0.00	W

(S: strong, M: medium, W: weak), with the corresponding r^{-6} -averaged hydrogen–hydrogen distances from the MD trajectory for the dimer of peptide 9 in chloroform. The pseudoatom corrections are taken from Fletcher et al.³⁶ The two molecules forming the dimer are indicated by A and B.

in Table IV. The strong NOEs between the Phe and Val α -protons, and weaker NOEs between the Val γ protons and the Phe α , β , and δ protons cannot be easily explained by intramolecular contacts, but they are wholly consistent with dimeric structures. The four available 3J -coupling

constants extracted from the NMR spectrum are compared in Table V, with the average coupling constants calculated from the structures of the trajectory at 303.15 K. These coupling constants provide further evidence for a β -strand-like conformation.⁴⁰ The presence of the interchain hydro-

TABLE V. Comparison of Experimental 3J -Coupling Constants¹²

3J -coupling pair		$^3J_{\text{cal}}$		$^3J_{\text{exp}}$
H atom	H atom	[Hz]	[Hz]	[Hz]
H-N(Phe:A)	H-CA(Phe:A)	8.7	9.0	8.4
H-N(Phe:B)	H-CA(Phe:B)	8.7	9.0	8.4
H-N(Val:A)	H-CA(Val:A)	7.5	7.6	9.6
H-N(Val:B)	H-CA(Val:B)	7.5	7.6	9.6

3J -coupling constants are calculated with the Karplus relation, Eq. (1), and averaged over the MD trajectory for the dimer of peptide 9 in chloroform. The two sets of parameters used in the Karplus relation are $a = 6.40$ Hz, $b = -1.40$ Hz, $c = 1.90$ Hz³⁸ (left column) and $a = 7.09$ Hz, $b = -1.42$ Hz, $c = 1.55$ Hz³⁹ (middle column).

gen bonds NH(Hao:A)-O11(Hao:B), N9H9(Hao:A)-O2(Hao:B), NH(NHBu:A)-O(i-PrCO:B), NH(Hao:B)-O11(Hao:A), N9H9(Hao:B)-O2(Hao:A), and NH(NHBu:B)-O(i-PrCO:A), which are characteristic for the dimer structure, was inferred from the chemical-shift measurements for the corresponding protons.¹² These hydrogen bonds were found to be long-lived in the simulation [Fig. 2, upper left panel]. Two intrachain hydrogen bonds, N1H1(Hao:A)-O4(Hao:A) and N1H1(Hao:B)-O4(Hao:B), appear intermittently [Fig. 2, upper left panel]. For these hydrogen bonds, the percentages of occurrence in the simulation are listed in Table VI.

In agreement with the experimental data, the dimer structure of the control peptide **11** turned out to be less stable in the simulation. After 11 ns, the RMSD value increases significantly, and around the same time, the interstrand hydrogen bonds, which are characteristic for the (antiparallel) dimer structure, are lost [Fig. 2, right panels]. Interestingly, after 45 ns, several new hydrogen bonds are formed, and the RMSD from the antiparallel β -sheet starting structure decreases significantly. The newly formed hydrogen bonds are indicative of a parallel β -sheet structure.

Experimentally, the addition of the competitive polar solvent CD₃OD to CDCl₃ has been observed to weaken the dimerization of **9**. Before simulating this ternary mixture, simulations of binary mixtures of CHCl₃ and CH₃OH were performed to investigate the properties of two different models of CH₃OH: the model available with the standard GROMOS96 force field,²⁶ and the more recently developed model by Walser et al.²⁹ The mixing enthalpy at 308 K and the density of the binary mixture at 298 K as a function of $x_{\text{CH}_3\text{OH}}$, the fraction of methanol, are shown in Figure 3, together with the available experimental data.^{41,42} The GROMOS96 model reproduces the mixing enthalpy to within 0.4 kJ mol⁻¹, with a deviation in the density of up to 5% for pure methanol. The newer model yields a very accurate density profile but a deviation of up to 0.7 kJ mol⁻¹ for the enthalpy of mixing. Because the two models represent the experimental data rather well, either could be used in the simulation of the ternary mixture. But because we were interested in mixtures at low methanol fractions, we chose the standard GROMOS96 CH₃OH model to study the effect of mixing a polar cosolvent on the stability of the Hao-containing peptide 9 in chloroform.

Figure 4 shows the backbone-atom RMSD of the trajectory structures with respect to the starting antiparallel β -sheet-like dimer structure. Addition of 10% CH₃OH makes the **9** dimer less stable, and dissociation and reassociation of the two chains is observed. The polar solvent CH₃OH can establish hydrogen bonds with the solute, in competition with interstrand hydrogen bonds.

Folding of Peptide 1a into a β -Hairpin

For molecule **1a** [Fig. 1 (C)], we performed three simulations that differ in the starting configurations and the force constants of the torsional angle (CH22-N-C-N) [Fig. 1 (E)] in the urea-based turn unit (Ut). The initial values of this torsional angle in simulations 1a₁, 1a₂, and 1a₃ are *trans*, *cis*, and *trans*, respectively, with the force constants 33.5, 33.5, and 7.11 kJ mol⁻¹, respectively. In the NMR-derived model structure, this torsional angle adopts a *cis* configuration. The value of this torsional angle as function of simulation time is shown in the three upper panels of Figure 5 for simulations 1a₁, 1a₂, and 1a₃, respectively. In the simulations with a higher barrier for the torsional rotation, no transition between the *trans* and *cis* conformation was observed during 100 ns of simulation. To observe *cis-trans* transitions, the torsional barrier was lowered, resulting in several transitions, with an isomerization time of the torsional angle CH22-N-C-N of about 10 ns. The atom-positional RMSDs from the NMR model structure for the backbone atoms of **1a** in the three simulations are displayed in the lower panels of Figure 5. In all three simulations, folding is observed. In simulation 1a₃, both folding and unfolding occur. The β -hairpin-like structure is formed by a turn stabilized by four hydrogen bonds: NH(Hao)-O(Leu), NH(Leu)-O2(Hao), N9H9(Hao)-O(Phe), and NH(Phe)-O11(Hao) [Fig. 5, middle panels]. NH(Hao)-O(Leu), NH(Leu)-O2(Hao), and N9H9(Hao)-O(Phe) were found to be long-lived in all three simulations, although out-of-register hydrogen bonding was observed in the first part of simulation 1a₃. The NH(Phe)-O11(Hao), which is near the turn, is found to exist only if the torsional angle CH22-N-C-N adopts the *cis* conformation, as shown in Figure 5 (upper and middle panels).

The 15 NOEs from the rotating-frame Overhauser enhancement spectroscopy (ROESY) spectrum¹¹ and the corresponding NOE distances calculated from the simulations, which are indicative of a β -hairpin-like structure, are listed in Table VII. The one NOE that has experimentally been labeled as strong (s) shows the shortest distance in the simulation. The five NOEs that have experimentally been classified as medium strong (m) are satisfied in all three simulations, except for the HD1-CD1(Ut)-HN(Phe) upper-bound distance, which is only satisfied by the structures from simulations 1a₂ and 1a₃. This interatomic distance strongly depends on the conformation of the torsional angle CH22-N-C-N. In the simulation 1a₁, this torsional angle stays *trans*; therefore, the interatomic distance between HD1-CD1(Ut) and HN(Phe) is larger than inferred from the experimental data. The 10 NOEs that have experimentally been labeled weak (w) show average distances compatible with the experimental data.

TABLE VI. Fraction of Hydrogen Bonds in the Simulations of the Dimers of Peptide 9 and 11 in Chloroform

Dimer of 9			Dimer of 11		
Hydrogen bond			Hydrogen bond		
Donor	Acceptor	%	Donor	Acceptor	%
NH(Hao:A)	O11(Hao:B)	95	NH(Phe:A)	O(Val:B)	8
N1H1(Hao:A)	O4(Hao:A)	24	NH(Val:A)	O(Phe:B)	7
N9H9(Hao:A)	O2(Hao:B)	93	NH(Phe:B)	O(Val:A)	17
NH(NHBu:A)	O(i-PrCO:B)	88	NH(Val:B)	O(Phe:A)	5
NH(Hao:B)	O11(Hao:A)	94	NH(Leu:A)	O(Phe:B)	6
N1H1(Hao:B)	O4(Hao:B)	24	NH(NHBu:A)	O(Val:B)	3
N9H9(Hao:B)	O2(Hao:A)	93	NH(Phe:B)	O(i-PrCO:A)	6
NH(NHBu:B)	O(i-PrCO:A)	88	NH(Val:B)	O(Leu:A)	3

A hydrogen bond is assumed to exist if the hydrogen-acceptor distance is smaller than 0.25 nm and the donor-hydrogen-acceptor angle is larger than 135°. The two molecules forming the dimer are indicated by A and B.

Fig. 3. Comparison of the mixing enthalpy at 308 K and the density at 298 K of binary mixtures of CHCl_3 and CH_3OH for two different molecular models (the standard GROMOS96 43A1 force field²⁶ and the more recently developed model²⁹) as a function of the fraction of methanol $x_{\text{CH}_3\text{OH}}$, with experimental data.^{41,42}

Figure 6 shows a superposition of the NMR model structure derived with the use of experimental NOE intensities¹¹ and the central-member structures from the most populated clusters from simulations 1a₁, 1a₂, and 1a₃. The backbone-atom positional RMSD between the central-member structures and the NMR model structure are 0.09 nm, 0.06 nm, and 0.07 nm, respectively. The first, most populated, cluster in the three simulations incorporates approximately 84%, 91%, and 51% of the ensemble.

Docking of a Hao-Containing Peptide to the Ras Analogue Rap1A

MD simulations of both the protein, Rap1A, and the protein-peptide complex, Rap1A:Ac-Ala-Hao-Ala-NHMe,

in water were performed to evaluate the stability of the protein-peptide complex. As a measure of structural stability, RMSDs from the starting structure were calculated based on a superposition of all C_α atoms of protein Rap1A. As shown in the lower panel of Figure 7, the overall C_α RMSD of Rap1A stays between 0.15 and 0.20 nm in both the Rap1A and the Rap1A:Ac-Ala-Hao-Ala-NHMe simulations, indicating a stable protein structure. The intermolecular hydrogen bonds between Rap1A and the Ac-Ala-Hao-Ala-NHMe peptide are shown in the upper panel of Figure 7. Although the hydrogen bond between the C-terminal end of the peptide and a protein sidechain (Asp:38) is lost after 1.6 ns, the backbone-backbone hydrogen bonds between protein and peptide

Fig. 4. Atom-positional RMSD for the backbone atoms from the starting structure of the dimer of peptide 9 in pure CHCl_3 , and in a 10/90% $\text{CH}_3\text{OH}/\text{CHCl}_3$ solution.

Fig. 5. Upper panels: Dihedral angle $\text{CH}_{22}\text{-N-C-N}$ as a function of simulation time for the three simulations of the peptide 1a. Middle panels: Occurrence of hydrogen bonds as a function of simulation time for this peptide. A hydrogen bond is assumed to exist if the hydrogen-acceptor distance is smaller than 0.25 nm and the donor-hydrogen-acceptor angle is larger than 135° . Lower panels: Atom-positional RMSD from the NMR model structure for the backbone atoms of this peptide. The three simulations differ regarding starting conformation and potential energy term for the mentioned dihedral angle (see footnote, Table I).

that form the β -sheet are stable during the simulation. The complex is stabilized by the interactions between one of the β -strands of Rap1A and the Hao-containing β -strand-like structure. Figure 8 shows a snapshot of

the Rap1A:Ac-Ala-Hao-Ala-NHMe complex at time 1 ns. The four protein residues that form hydrogen bonds with the peptide are shown explicitly together with the peptide. Indeed, the artificial peptide provides an alter-

TABLE VII. Comparison of Experimental NOE Intensities¹¹

NOE pair		Simulated distance $\langle r^{-6} \rangle^{-1/6}$			Pseudoatom correction	Exp. NOE intensity
H atom	H atom	1a ₁	1a ₂	1a ₃		
H5-C5(Hao)	H-CA(Ile)	0.228	0.238	0.249	0.00	S
H5-C5(Hao)	H-CG1(Ile)	0.390	0.428	0.415	0.00	W
H5-C5(Hao)	H-CD(Ile)	0.489	0.495	0.513	0.04	M
H5-C5(Hao)	H-N(Leu)	0.309	0.310	0.336	0.00	W
H-CH(N-ter)	H-CH3(C-ter)	0.379	0.364	0.393	0.04	W
H-CH(N-ter)	H-CB(Leu)	0.382	0.398	0.428	0.00	W
H-CH(N-ter)	H-CD1(Leu)	0.566	0.584	0.578	0.15	W
H-CH(N-ter)	H-CG(Leu)	0.439	0.467	0.463	0.07	W
H-CH31(N-ter)	H-CH3(C-ter)	0.489	0.474	0.481	0.19	M
H-CH31(N-ter)	H-CG(Leu)	0.596	0.617	0.592	0.22	W
H-N(Hao)	H-N(Leu)	0.324	0.316	0.349	0.00	W
H1-N1(Hao)	H-N(Leu)	0.492	0.486	0.531	0.00	W
H9-N9(Hao)	H-N(Phe)	0.422	0.347	0.384	0.00	W
H9-N9(Hao)	HD1-CD1(Ut)	0.521	0.461	0.443	0.20	M
HD1-CD1(Ut)	H-N(Phe)	0.664	0.517	0.557	0.20	M

(S: strong, M: medium, W: weak), with the corresponding r^{-6} averaged hydrogen–hydrogen distances from the three MD simulations for the peptide 1a in chloroform. The pseudoatom corrections are taken Fletcher et al.³⁶ The three simulations differ regarding starting structure and torsional-angle potential energy of the angle CH22-N-C-N (see footnote, Table I).

Fig. 6. (A) Superposition of the NMR model structure with the central-member structure of the first, most populated, cluster in the simulation 1a₁ (population, 84%; structure at time, 40.99 ns; 0.09 nm RMSD). The C atoms are in purple in the NMR model structure, and yellow in the central-member structure of the first cluster. The N, O, and H atoms are in blue, red, and cyan, respectively. (B) Superposition of the NMR model structure with the central-member structure of the first, most populated, cluster in the simulation 1a₂ (population, 91%; structure at time, 65.27 ns; 0.06 nm RMSD). (C) Superposition of the NMR model structure with the central-member structure of the first, most populated, cluster in the simulation 1a₃ (population, 51%; structure at time, 66.43 ns; 0.07 nm RMSD).

Fig. 7. Upper panel: Occurrence of the hydrogen bonds between the protein Rap1A and peptide Ac-Ala-Hao-Ala-NHMe. A hydrogen bond is assumed to exist if the hydrogen-acceptor distance is smaller than 0.25 nm and the donor-hydrogen-acceptor angle is larger than 135° . The hydrogen bonds: NTHT(C-ter)-OD2(Asp:38), NTHT(C-ter)-OD1(Asp:38), N9H9(Hao:2)-O (Ser:39), C5H5(Hao:2)-OG(Ser:39), NH(Gln:43)-OT(N-ter), NH(Arg:41)-O2(Hao:2), and NH(Ser:39)-O1(Hao:2) are present in 60%, 55%, 52%, 17%, 35%, 89%, and 52%, respectively, of the configurations. Lower panel: RMSD from the starting structure for all the C_α atoms of the protein Rap1A (PDB code: 1gua).

Fig. 8. Snapshot of the Rap1A and the peptide Ac-Ala-Hao-Ala-NHMe in the simulation of the complex in water at 1 ns. The four protein residues—Asp38, Ser39, Arg41, and Gln43—are shown in full, together with the peptide.

nating pattern of hydrogen-bond donors and acceptors that matches that of the target β -strand in Rap1A.

CONCLUSIONS

MD simulations, including an explicit treatment of the solvent, have been used to study in atomic detail the

dimerization, folding, and binding to a protein surface of peptides containing the unnatural amino acid Hao [Fig. 1(D)]. The peptide **9** [Fig. 1(B)] is found to dimerize strongly in chloroform, as was observed in NMR studies. Compared to the natural tripeptide **11**, peptide **9** is longer and can form six intermolecular hydrogen bonds. The key structural unit Hao imparts a β -strand-like conformation to the peptide that contains it and facilitates its dimerization through β -sheet interactions. Compared to natural amino acids, Hao is conformationally more constrained. Artificial β -hairpin-like structures, such as that adopted by **1a** [Fig. 1 (C)], can be obtained for hybrid peptides consisting of the tripeptide mimic Hao, the turn segment, and a tripeptide part. In the β -hairpin **1a**, Hao serves as a template that organizes the tripeptide part into a β -hairpin that in turn can form β -sheet contacts on one edge. In this sense, Hao confers both structure (folding into β -hairpin-like conformations) and function (β -sheet blockage) to the peptides that contain it. Because of the high-energy torsional barrier in the urea-based turn segment, starting from the extended conformation, **1a** was not able to fold into the NMR-derived model structure within 100 ns. In the simulation **1a**₂, starting from the *cis* conformation of the torsional angle CH22-N-C-N, **1a** did fold to the experimentally derived structure, with an RMSD of 0.06 nm between the central-member structure of the first, most populated, cluster and the NMR model structure. Reduction of the torsional barrier allowed the folding to occur

within 100 ns. The peptide, Ac-Ala-Hao-Ala-NHMe, was found to form a rather stable complex with the protein, Rap1A. One of the edges of this simple peptide provides an alternating pattern of hydrogen-bond donors and acceptors that finds its counterpart in a β -strand at the surface of Rap1A, forming an intermolecular β -sheet. As suggested by Nowick et al.,¹² Hao-containing peptides may hold promise as inhibitors to block β -sheet interactions between proteins.

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