2017

Progress in indentation study of materials via both experimental and numerical methods

Mao Liu
*University of Wollongong*, ml818@uowmail.edu.au

Jhe-yu Lin
*University of Tokyo*

Cheng Lu
*University of Wollongong*, chenglu@uow.edu.au

Anh Kiet Tieu
*University of Wollongong*, ktieu@uow.edu.au

Kun Zhou
*Nanyang Technological University*

*See next page for additional authors*

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Liu, Mao; Lin, Jhe-yu; Lu, Cheng; Tieu, Anh Kiet; Zhou, Kun; and Koseki, Toshihiko, "Progress in indentation study of materials via both experimental and numerical methods" (2017). *Faculty of Engineering and Information Sciences - Papers: Part B*. 888.


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Disciplines
Engineering | Science and Technology Studies

Publication Details

Authors
Mao Liu, Jhe-yu Lin, Cheng Lu, Anh Kiet Tieu, Kun Zhou, and Toshihiko Koseki

This journal article is available at Research Online: https://ro.uow.edu.au/eispapers1/888
Review

Progress in Indentation Study of Materials via Both Experimental and Numerical Methods

Mao Liu 1,2,*, Jhe-yu Lin 1, Cheng Lu 2, Kiet Anh Tieu 2, Kun Zhou 3,*, and Toshihiko Koseki 1

1 Department of Materials Engineering, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-8656, Japan; 3ig275@gmail.com (J.L.); koseki@material.t.u-tokyo.ac.jp (T.K.)
2 School of Mechanical, Materials and Mechatronic Engineering, University of Wollongong, Wollongong, NSW 2522, Australia; chenglu@uow.edu.au (C.L.); ktieu@uow.edu.au (K.A.T.)
3 School of Mechanical & Aerospace Engineering, Nanyang Technological University, 50 Nanyang Avenue, Singapore 639798, Singapore
* Correspondence: ml818@uowmail.edu.au (M.L.); kzhou@ntu.edu.sg (K.Z.)

Academic Editor: Ronald W. Armstrong
Received: 19 June 2017; Accepted: 9 August 2017; Published: 13 October 2017

Abstract: Indentation as a method to characterize materials has a history of more than 117 years. However, to date, it is still the most popular way to measure the mechanical properties of various materials at microscale and nanoscale. This review summarizes the background and the basic principle of processing by indentation. It is demonstrated that indentation is an effective and efficient method to identify mechanical properties, such as hardness, Young’s modulus, etc., of materials at smaller scale, when the traditional tensile tests could not be applied. The review also describes indentation process via both experimental tests and numerical modelling in recent studies.

Keywords: indentation; mechanical properties; hardness; nanoscale; experiment; modelling

1. Introduction

Indentation tests were first performed by a Swedish iron mill’s technical manager Brinell who used spherical balls from hardened steel ball bearings or made of cemented tungsten carbide as indenters to measure the plastic properties of materials in 1900 [1–4]. Brinell’s testing approach is schematically shown in Figure 1a. Brinell also proposed the following formula to determine the hardness

\[ H_B = \frac{2P}{\pi D (D - \sqrt{D^2 - d^2})} \]  

here \( H_B \) is the Brinell hardness; \( P \) is the load; \( D \) is the diameter of the ball indenter and \( d \) is the diameter of residual area of the impression.

Brinell’s work was then followed and improved by Meyer in 1908 [5]. In his work, the hardness \( (H) \) is calculated by the load \( (P) \) divided by the projected area \( (A) \), namely

\[ H = \frac{P}{A} \]  

In 1922, the Vickers test was carried out and commercialized by the Firth-Vickers company [6]. A square-based pyramid diamond indenter with a 136° semi-angle was used instead of a ball indenter, as shown in Figure 1b. The Vickers hardness \( (H_V) \) is defined as the load divided by the surface area of the impression, namely

\[ H_V = 1.8544 \frac{P}{d_V^2} \]  

where \( d_V \) is the length of diagonal of the surface area.
While the indentation tests could be quickly performed on a small area without destroying the whole sample. Another significant finding is that the hardness is load-dependent, which was proposed by Meyer through ball indentation experiments on a wide range of metals [7]. For a given ball size, the diameter of the impression after unloading was found to be related to the applied load by the following empirical relationship:

\[ P = C d^n \]  

(4)

here \( P \) is the applied load; \( C \) is a constant of proportionality; the exponent \( n \) is the well-known Meyer index and \( d \) is the diameter of the residual area of the impression after unloading. When the \( n \)-value is less than 2, according to Equations (2) and (4), the hardness increases with decreasing the load. While the \( n \)-value is larger than 2, the hardness decreases with decreasing the load. If the Meyer index equals to 2, the hardness is a constant, namely load-independent. For most metals that can be work hardened by the indentation process, \( n > 2 \) [7]. Therefore, the Meyer index has been found to be strongly dependent on the work hardening of the tested material and to be independent of the size of the ball indenter [5]. Meyer [5] also found that the same hardness using balls of different diameters could be obtained only if the indentations were geometrically similar, namely with the same ratio \( d/D \).

Tabor’s work [8] performed in 1948 represents a landmark in the understanding of the indentation process. He qualitatively described the procedure how an indentation by a ball initially led to elastic deformation, then to plastic flow associating with work hardening, and finally on removal of the load to elastic recovery. In 1951, Tabor [1] had proven that the indentation hardness (\( H \)) could be related to the yield stress (\( \sigma \)) of the material by an equation based on the theory of indentation of a rigid perfectly plastic solid, namely

\[ H = C\sigma \]  

(5)

where \( C \) is a constant, which depends on the geometry of the indenters. For the strain-hardened materials and the materials which consequently have no definite yield stress, the stress measured at a representative strain \( \varepsilon_r \) can be used as \( \sigma \) [9]. The representative strain denotes the strain at where the corresponding stress can be regarded as the yield stress during tensile deformation for the materials without definite yield stress. The value of the representative strain is relevant to the geometry of the indenter. For instance, \( \varepsilon_r \approx 0.08 \) for a Vickers diamond indenter.

Tabor [7] started taking an interest in the indentation response of polymers and of macroscopically brittle materials in the studies of their frictions. In the following couple of years, Tabor and
King [10] reported the method of estimating the yield pressure on polyethylene, PMMA (Polymethyl methacrylate), PTFE (Polytetrafluoroethylene), and halocarbon polymer via Vickers hardness measurements. Subsequently, Pascoe and Tabor [11] reported a range of polymers obeyed Meyer’s laws. The single-crystal rock salt was also investigated by King and Tabor [12] with Vickers indentations, by which, they found the values of yield stress from the indentation matched well with the compression experiments.

In 1960s, indentation at high temperature was investigated by Atkins and Tabor [13]. They studied the mechanical properties of single crystals of MgO at temperatures of 600 °C to 1700 °C via the mutual indentation hardness technique. It was found that the short-time hardness decreased when the temperature increased.

Conventional indentation tests have the length scale of the penetration in microns or millimetres. In the mid-1970s, the indentation technique was applied to measure the hardness of small volumes of material, such as thin film. The length scale of the penetration is usually in nanometres. Therefore, this new technique is called nanoindentation. Apart from the penetration length scale, the distinguishing feature of nanoindentation testing is the indirect measurement of the contact area [14]. In conventional indentation tests, the contact area is directly measured from the residual impression area. In nanoindentation test, the residual impression area is too small to be directly measured. Therefore, the contact area is determined by the measured penetration depth in nanoindentation.

Since 1980s, especially after 1990s, extensive experimental studies of nanoindentation have been performed on many different types of materials. This review will provide the systematic description of indentation study of materials via both experimental and numerical methods. The contents of this article can be summarized as follows. The first section provides the background necessary for understanding the mechanics of indentation and hence for understanding its applications in materials science. The second part reviews methods of mechanical properties characterization and measurement and follows with application to experimental measurement reported in the literature. Next, we discuss the numerical study of deformation mechanism of materials induced by indentation. We follow with a comprehensive review of the models involved in texture and indentation size effect prediction, ranging in length scale from the meso- and micro- to the nanoscale, and a critical assessment of their performance.

2. Nanoindentation Facilities

The most famous manufacturers of nanoindentation equipment include Keysight Technologies (Santa Rosa, CA, USA), Micro Materials Ltd. (Wrexham, UK), Fischer-Cripps Laboratories Pty Ltd. (Killarney Heights, Australia), Hysitron Inc. (Eden Prairie, MN, USA), and Anton Paar (Ashland, VA, USA). The iconic products of these manufacturers are shown in Figure 2. The working theories of different representative instruments are given in Figure 3. All of these instruments include three principal parts, namely indenter, load application, and capacitive sensor for measuring the displacements of the indenter. For instance, in Figure 3a, the load is applied by an electromagnetic coil which is connected to the indenter shaft by a series of leaf springs. The deflection of the springs is a measure of the load applied to the indenter, and the displacement usually can be measured by a capacitive sensor.

![Figure 2. Cont.](image-url)
The conical indenter has a sharp, self-similar geometry. Normally, the cone angle is either 60° or 90°, and the tip radii are 0.7, 1, 2, 5, 10, 20, 50, 100 and 200 μm [16]. The applications of conical indenter are extensive, including scratch testing, wear testing, nano-scale 3D imaging capturing and tensile, and compression tests on MEMS (Microelectromechanical systems). Berkovich indenter is the most frequently used indenter for indentation tests. The most noticeable feature of Berkovich indenter is that it is a three-sided pyramid which can be ground to a point, making it easy to maintain a self-similar geometry to micro-scale or nano-scale. The radius is about 150 nm when it is new and will become 250 nm 12 months later. The applications of Berkovich indenter are much more extensive, such as bulk materials tests, thin films tests, polymers tests, scratch testing, wear testing, MEMS tests and in situ imaging. The Vickers indenter is a four-sided pyramid and suitable for measuring mechanical properties on the very small scale, such as nano-scale as the line of conjunction at the tip limits the sharpness of tip for determination of hardness for very shallow indentation. The recommended applications include bulk materials tests, films and foils tests, scratch testing and wear testing.
The fracture toughness can be obtained directly from indent crack length measurements, as shown in Figure 5.

The reason is, the contact stresses with spherical indenter are initially small and produce only elastic deformation, and with increasing indentation depth, a transition from elastic to plastic deformation can be captured. The parameters of all these indenters are listed in Table 1. Here, A denotes the projected area; R represents the contact radius of the indent pressed by spherical indenter; h is the contact indentation depth; θ represents the semi angle of indenters; a is the effective cone angle and β denotes the geometry correction factor.

**Table 1. Parameters of different indenters [17].**

<table>
<thead>
<tr>
<th>Indenter Type</th>
<th>Projected Area</th>
<th>Semi Angle (θ)</th>
<th>Effective Cone Angle (a)</th>
<th>Intercept Factor</th>
<th>Geometry Correction Factor (β)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sphere</td>
<td>A = π2Rhₚ²</td>
<td>N/A</td>
<td>N/A</td>
<td>0.75</td>
<td>1</td>
</tr>
<tr>
<td>Berkovich</td>
<td>A = 3hₚ²tan²θ</td>
<td>65.3°</td>
<td>70.2996°</td>
<td>0.75</td>
<td>1.034</td>
</tr>
<tr>
<td>Vickers</td>
<td>A = 4hₚ²tan²θ</td>
<td>68°</td>
<td>70.32°</td>
<td>0.75</td>
<td>1.012</td>
</tr>
<tr>
<td>Knoop</td>
<td>A = 2hₚ²tanθtanθ₂</td>
<td>θ₁ = 86.25°, θ₂ = 65°</td>
<td>77.64°</td>
<td>0.75</td>
<td>1.012</td>
</tr>
<tr>
<td>Cube-corner</td>
<td>A = 3hₚ²tan²θ</td>
<td>35.26°</td>
<td>42.28°</td>
<td>0.75</td>
<td>1.034</td>
</tr>
<tr>
<td>Conical</td>
<td>A = nhₚ²tan²a</td>
<td>a</td>
<td>a</td>
<td>0.72</td>
<td>1</td>
</tr>
</tbody>
</table>

3. Application of Nanoindentation in Materials

In 1992, Oliver and Pharr [18] proposed a method to measure the Young's modulus based on the indentation load-displacement curve, which was frequently used until now. Subsequently, they [19] provided a update of how to implement the method to make the most accurate measurements as well as the discussion of its limitations. Kucharski and Mroz [20] presented a new procedure for determining the plastic stress—strain curve by means of a cyclic spherical indentation test in 2007, which constitutes a ground-breaking improvement with respect to the traditional method. Kruzic et al. [21] improved the indentation techniques of evaluating the fracture toughness of biomaterials and hard human bones although accurately measuring the fracture toughness of brittle materials can be quite challenging. The fracture toughness can be obtained directly from indent crack length measurements, as shown in Figure 5.
Huber and Tsakmakis [22] proposed that nanoindentation tests can be used to identify effects of kinematic hardening on the material response. They also indicated that the identification may rely on the measurement of the opening of the hysteresis loop produced in the indentation load-displacement curve as shown in Figure 6. It is obvious that each material has a unique opening diagram indicating the corresponding effect of kinematic hardening.

Durban and Masri [23] in 2007 found that the nanoindentation test data with conical indenter over a range of cone angles can be used to reconstruct the axial stress-strain curve. Mata et al. [24] modified the previous hardness formulation within the elastic-plastic transition derived for solids by Hill [25] in 1950 and Marsh [26] in 1964 as it did not exhibit strain hardening.

Application of nanoindentation tests to determine the mechanical properties of surface coatings is another milestone. Normally, the investigations of the mechanical properties of the coatings are
difficult as the traditional compression and tensile tests are unable to apply well at very small scales. Rodriguez et al. [27] performed depth sensing indentation in plasma sprayed $\text{Al}_2\text{O}_3$-13% $\text{TiO}_2$ nano-coatings in order to determine the Young’s modulus and hardness. It was found the mechanical properties were dramatically enhanced in the nanostructured coating compared to the conventional one, which is shown in Figure 7. Swain, Menčik and their coworkers [28;29] investigated the application of five approximation functions (linear, exponential, reciprocal exponential, Gao’s, and the Doerner and Nix functions) for determining the Elastic modulus of thin homogeneous films. By conducting various experimental testes, they found that generally the Gao analytical function is able to predict the indentation response of film/substrate composites. For determining the thin film modulus from experimental data, satisfactory results can also be obtained with the exponential function, while linear function can only be used for thick films where the relative depths of penetration are small. For determing the hardness of thin films, Jönsson and Hogmark [30] built a physical model which was verified for chromium films on four different substrate materials.

**Figure 7.** Young’s modulus and hardness vs. total penetration depth for both coatings [27]. Reproduced with permission from J. Rodriguez et al., Acta Materialia; published by Elsevier, 2009.

Thin water film was studied by Opitz et al. [31] in 2003. It was believed that the thin water films which covered most of the micro-scale and nano-scale surfaces could be particularly important for microelectromechanical systems (MEMS) and the upcoming nanoelectromechanical systems (NEMS), as they played a critical role in defining the micro- and nano-tribological properties of a system. Kim et al. [32] presented a nanoindentation method to measure the Poisson’s ratio of thin films for MEMS applications. In their test, a double-ring-shaped sample was designed to conduct the measurement of the Poisson’s ratio as shown in Figure 8. The load-deflection data of the double ring sample after nano-indenter loading was analysed to obtain the Poisson’s ratio. Lou et al. [33] investigated the mechanical behaviour of LIGA (an acronym of the German words “lithographie, galvanoformung, abformung”) nickel MEMS structures which were developed for applications in micro-switches and accelerometers via the nanoindentation method. Both Berkovich and Cube-corner indenter were used to conduct the nanoindentation tests and study the effects of residual indentation depth on the hardness of LIGA Ni MEMS structures between the micro-scale and nano-scales. Almost no apparent size dependence has been found for LIGA Ni films indented by a Berkovich indenter. In contrary, the hardness dramatically increased with decreasing residual indent depth for films indented by the Cube-corner indenter.
Indentation tests were also used to evaluate adhesion strength of the thermal barrier coatings (TBCs) which were used to improve the performance and efficiency of advanced gas turbines [34–38]. Interfacial strength was one of the most important properties in TBCs, and traditional tensile method was found to be restricted due to the size dependence. Yamazaki et al. [39] used the indentation method to investigate the interfacial strength of TBC which was subjected to thermal cycle fatigue. An indent was made directly at the interface on the polished surface of the sample as shown in Figure 9. The crack length and the diagonal length of the indentation were measured using SEM right after indentation as shown in Figure 10. The typical interfacial crack initiated by the indentation test in Figure 10a showed the crack mainly propagated in the ceramic top coat near the interface. Even after 500 thermal cycles with the formation and growth of TGO (thermally grown oxide) layer shown in Figure 10b, the crack propagated only in the ceramic top coat too.

![Figure 8. Top view of the double ring sample [32]. Reproduced with permission from Jong-Hoon Kim et al., Sensors and Actuators A: Physical; published by Elsevier, 2003.](image1)

![Figure 9. Schematic illustration of the instrumented indentation test equipment [39]. Reproduced with permission from S. Kuga et al., Procedia Engineering; published by Elsevier, 2011.](image2)

![Figure 10. Typical interfacial cracks initiated by the indentation test: (a) for 0 thermal cycles (As-sprayed); (b) after 500 cycles [39]. Reproduced with permission from S. Kuga et al., Procedia Engineering; published by Elsevier, 2011.](image3)
The dependence of nanoindentation piling-up patterns and of micro-textures on the crystallographic orientation was studied by Wang et al. [40] using high purity copper single crystal with three different initial orientations. The indentation tests were performed on a Hysitron nanoindentation setup using a conical indenter to avoid symmetries. The results are shown in Figure 11. Four-, two-, and sixfold symmetrical piling-up patterns were captured on the surface of (001), (011) and (111) initial oriented single crystal, individually, which could be explained in terms of the strong crystallographic anisotropy of the out-of-plane displacements around the indenter.

![Figure 11](image1.png)

**Figure 11.** Experimentally observed contour plots of the pile-up patterns on (a) (001), (b) (011) and (c) (111) oriented copper single crystal surfaces after indentation with a conical indenter [40]. Reproduced with permission from Y. Wang et al., Acta Materialia; published by Elsevier, 2004.

With the development of focused ion beam milling of site-specific electron transparent foils, the investigation of cross-sections of nanoindentations with the transmission electron microscope (TEM) or electron backscatter diffraction has recently become feasible [41]. Lloyd [42] and his colleagues combined nanoindentation and TEM to survey the deformation behaviour in a range of single crystal materials with different resistances to dislocation flow as shown in Figure 12. The principal deformation models included phase transformation (silicon and germanium), twinning (gallium arsenide and germanium at 400 °C), lattice rotations (spinel), shear (spinel), lattice rotations (copper) and lattice rotations and densification (TiN/NbN multilayers). Generally, the residual impresses were sectioned through the tip of the indent with the thin foil normal approximately parallel to either [110] or [100] zone axis.

![Figure 12](image2.png)

**Figure 12.** (a) Schematic illustrating how the indents were sectioned in the FIB to allow examination with a TEM; (b) Secondary electron FIB image of the final stages of preparation of a thin foil through a 50 mN indent in silicon [42]. Reproduced with permission from S.J. Lloyd et al., Proceedings of the Royal Society A; published by The Royal Society, 2005.
The indents in (001) silicon at loads of 30 mN and 60 mN are shown in Figure 13. It was found a transformed region was under the area of the Berkovich indenter in both cases, and a crack was originating at the base of the transformed region in the case of 60 mN.

Shear bands were captured in spinel crystals, which are shown in Figures 14 and 15. It was found the shear band spacing increased with increasing distance from the indent tip, and the spacing on the steep side of the indent was a little smaller for the large load. Lloyd [43] concluded that the increase of the shear band spacing with distance far away from the indenter tip indicated there was a limit to the amount of displacement occurring through any shear band due to strain hardening. Consequently, a high concentration of shear bands was close to the indenter tip where had the largest vertical displacements, while a low density of slip bands was sufficient to accommodate the relatively small vertical displacement in the region far away from the indenter tip.
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Figure 14. (a) Bright field image of an 80 mN indent in spinel with an inset diffraction pattern; (b) Bright field image of a 60 mN indent in spinel showing the region of shear bands under the indent more clearly; (c) Schematic illustrating the principle components of the deformation pattern in spinel [42]. Reproduced with permission from S.J. Lloyd et al., Proceedings of the Royal Society A; published by The Royal Society, 2005.

Figure 15. Slip band spacing in spinel as a function of distance from the indenter tip (see Figure 14b) for the 50 mN and 80 mN indents. The error in measurement of the shear band spacing is approximately 10 nm [42]. Reproduced with permission from S.J. Lloyd et al., Proceedings of the Royal Society A; published by The Royal Society, 2005.

Lattice rotation angles around an axis perpendicular to the [110] zone axis were investigated [42] and are shown in Figure 16. It was found the rotations only occurred in the region immediately below the indent impression. The greatest rotations were quite near the indent tip and the magnitude of rotation angles decreased significantly with the increasing distance from the indent tip along the surface on the shallow side.
Figure 16. (a) Bright field image of a 50 mN indent in spinel with lattice rotations (in degrees) at selected positions indicated; (b,c) are dark field images of the surface of the same indent taken using streaks from either side of the 004 reflection [42]. Reproduced with permission from S.J. Lloyd et al., Proceedings of the Royal Society A; published by The Royal Society, 2005.

The indentation-induced plastic zones below indentations in copper single crystals, with depths ranging from 250 nm to 250 μm, were examined by Rester et al. [44] via the implementation of focused ion beam (FIB) and electron backscatter diffraction (EBSD) techniques. Two or three distinguishable regimes shown in Figure 17 were captured by analysing scanned orientation micrographs. Meanwhile, the changes in the evolution of the microstructure were reflected in the hardness curve shown in Figure 18. Regime α described the impression which is smaller than 300 nm, in which no significant orientation changes are observed by EBSD (Figure 17a). Regime β describes the indentation depth between 300 nm and 30 μm, which is characterized by regions having noticeable changes of the orientation (Figure 17c,d). It was also found that the orientation differences increase with growing indentation depth in this regime. Regime γ is associated with indentation depth larger than 30 μm exhibiting a typical substructure of FCC (face centered cubic) single crystal of pure metals during indentation. Therefore, Rester et al. [44] concluded that the hardness of a material varies with the size of the indent impression and the source size becomes the dominant effect only for very small impressions (i.e., in regime α).

Figure 17. Cont.
Figure 17. Misorientation maps of indentations in copper for loads of (a–d) 0.5, 1, 10, 300 mN; (e) 10 N and (f) 100 N [44]. Reproduced with permission from M. Rester et al., Scripta Materialia; published by Elsevier, 2008.

Figure 18. Logarithmic plot of the hardness versus the indentation depth for loads ranging from 40 μN to 100 N. The arrows mark the hardness values of imprints investigated in course of this work [44]. Reproduced with permission from M. Rester et al., Scripta Materialia; published by Elsevier, 2008.

Zaafarani et al. [45] investigated texture and microstructure below a conical nano-indent in a (111) oriented Cu single crystal using 3D EBSD. The tests were performed using a joint high-resolution field emission scanning electron microscopy/electron backscatter diffraction (EBSD) set-up coupled with serial sectioning in a focused ion beam system in the form of a cross-beam 3D crystal orientation microscope (3D EBSD) as shown in Figure 19.

The EBSD tests conducted in sets of subsequent (112) cross-section planes exhibited a pronounced deformation-induced 3D patterning of the lattice rotations below and around the indent, which are shown in Figure 20.
Figure 17. Misorientation maps of indentations in copper for loads of (a–d) 0.5, 1, 10, 300 mN; (e) 10 N and (f) 100 N [44].

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Figure 19. (a) Joint high-resolution field emission SEM/electron backscatter diffraction (EBSD) set-up together with a focussed ion beam (FIB) system in the form of a cross-beam 3D crystal orientation microscope for conducting 3D EBSD measurements by serial sectioning (Zeiss); (b) Schematic of the joint FIB/EBSD set-up; (c) Schematic of the FIB sectioning geometry [45]. Reproduced with permission from N. Zaafarani et al., Acta Materialia; published by Elsevier, 2006.
4. Nanoindentation Size Effect of Materials

Over the past several decades, with the development of new technologies, people felt that it was very important to understand how materials perform at small scales because the mechanical properties are significantly different from those at macro-scales. Therefore, a great number of researchers became interested in micro- and nano-scale deformation phenomena which also made them try to look for a new method to examine these physical phenomena at ever-decreasing length scales. In the field of the mechanical behaviour of materials, one of the more interesting small-scale phenomena is an increase in yield or flow strength that is often observed when the size of the test sample is reduced to micro-meter and sub-micrometer dimensions [46]. Pharr et al. [46] believed such size-dependent increases in strength were due to unique deformation phenomena which could be observed only when the sample dimensions approached the average dislocation spacing and when plastic deformation was controlled by a limited number of defects.

In the metal micro-forming process, grain size, grain orientation and material’s dimension are the important influence factors for the material’s deformation. It is reported that when the dimension of the material is downscaled to a much smaller scale, the mechanical properties are significantly different from those on the macro-scale, which is called ‘size effect’ [47]. Size effect is an interesting and important topic for the development of micro-forming technologies. Recently, numerous experiments have shown that metallic materials display noticeable size effects once the size of non-uniform plastic deformation zone associated their characteristic length size are on the order of microns [47]. Fleck et al. [48] found a dramatic increase of plastic work hardening when the wire’s diameter decreased from 170 µm to 12 µm via doing thin copper wire’s torsion experiments. Stolken and Evans [49] observed that the plastic work hardening increased significantly when the nickel beam thickness was decreased from 50 µm to 12.5 µm while doing a micro-bend test. Gau et al. [50] found that the conventional concept of spring-back cannot be applied on brass sheet metal when its thickness is less than 350 µm by studying...
the spring-back behaviour of brass in micro-sheet forming. Geiger et al. [51] and Kals and Eckstein [52] have conducted compression tests, tension tests, and bending tests, respectively, in order to study how the material properties change due to size effect. Saotome et al. [53] carried out investigations in micro-deep drawing, and found that the relative punch diameter (punch diameter related to the sheet thickness) has a significant influence on the limit draw ratios (LDR).

The indentation size effect (ISE) is often observed for materials that are indented with geometrically self-similar indenters like pyramidal or conical tips (see Figure 21) [46]. In general, the hardness, H, defined as the load on the indenter normalized with the projected contact area of the hardness impression (see Figure 21), should be independent of the depth of penetration, h. However, over the past 60 years, it was observed that there were significant variations of hardness with respect to penetration depth, especially when the depths decreased to less than a few micro-meters [54–60]. In addition, two types of indentation size effects have been reported. One is the normal ISE (the tip is pyramidal or conical)—the hardness increases with decreasing penetration depths, according to the expression “smaller is stronger” (see Figure 21). Another one is the reverse ISE (the tip is spherical) [55,56,61], which displayed that the hardness decreases with increasing depths. However, for the reverse ISE, it was observed that the hardness also increases with the decreasing of tip radius. The reverse ISE is thought to be derived from testing artefacts such as vibration in the testing system or problems with accurate imaging and measuring the sizes of hardness impressions at dimensions approaching the limits of optical microscopy [46].

Although classical descriptions of the ISE show a decrease in hardness for increasing indentation depth (Figure 22), recently new experiments [62] have shown that after the initial decrease, hardness increases with increasing indentation depth. After this increase, eventually the hardness decreases with increasing indentation (Figure 23). This phenomenon is very prominent for copper, but not noticeable for aluminium.

![Figure 21. Indentation size effect (ISE) (a) for geometrically self-similar indenters such as a conical or pyramidal tip (b) [46]. Reproduced with permission from George M. Pharr et al., Proceedings of Annual Review of Materials Research; published by Annual Reviews, 2010.](image-url)
Figure 21. Indentation size effect (ISE) (a) for geometrically self-similar indenters such as a conical or pyramidal tip (b) [46].

Figure 22. Visualization of the ISE: hardness decreases with increasing indentation depth for cold-worked polycrystalline copper [62]. Reproduced with permission from G.Z. Voyiadjis et al., Acta Mechanica; published by Springer, 2010.

Figure 23. Visualization of the ISE with the incorporated hardening effect. For \( h < h_1 \), hardness decreases, for \( h_1 < h < h_2 \), hardness increases and for \( h > h_2 \), hardness decreases again [62]. Reproduced with permission from G.Z. Voyiadjis et al., Acta Mechanica; published by Springer, 2010.

There are different theories to explain ISE. The most popular theory is based on strain gradient plasticity which is a class of continuum theories aimed to bridge the gap between classical plasticity and dislocation. This theory assumes that the flow stress of metals depend on the density of statistically stored dislocations (SSD) which relate to effective strain, and the density of the geometrically necessary dislocations (GND) which relate to the strain gradient. Dislocations are generated, moved and stored during the process of plastic deformation. The process of storing dislocation is also a process of strain hardening. It is assumed that dislocations become stored because they either accumulate by randomly trapping each other or they are required for compatible deformation of various parts of the material. When they randomly trap each other, they are often known as the statistically stored dislocation [63], whereas when they are required for the compatibility purpose, they are often called geometrically necessary dislocations and related to the gradient of plastic shear strain in a material [63,64].

The most famous strain gradient plasticity model for nanoindentation was proposed by Nix and Gao [65] in 1998. It has been assumed that plastic deformation of the surface is accompanied by the generation of dislocation loops below the surface, which are contained in an approximately hemispherical volume below the region in contact, as shown schematically in Figure 24. The deformation is self-similar and the angle (\( \theta \)) between the conical indentation tip and indented surface remains constant.
There are different theories to explain ISE. The most popular theory is based on strain gradient plasticity which is a class of continuum theories aimed to bridge the gap between classical plasticity and the deformation resistance:

\[ \tau_{\text{h}} = \alpha \mu \sqrt{\rho_T} = \alpha \mu \sqrt{\rho_G + \rho_S} \]

where \( \tau \) is the resolved shear stress, \( \mu \) is the shear modulus, \( b \) is the Burgers vector and \( \alpha \) is a constant which is usually in the range 0.3–0.6 for FCC metals [66]. Here, they note that \( \rho_S \) does not depend on the depth of indentation. Rather it depends on the average strain in the indentation, which is related to the shape of the indenter (\( \tan(\theta) \)). They also assume that the von Mises flow rule applies and that Tabor’s factor of 3 can be used to convert the equivalent flow stress to hardness:

\[ \sigma = \sqrt{3} \tau, H = 3\sigma \]

According to these relations the hardness can be expressed by as:

\[ \frac{H}{H_0} = \sqrt{1 + \frac{h^*}{h}} \]

where

\[ H_0 = 3\sqrt{3} \alpha \mu b \sqrt{\rho_S} \]
is the macroscopic hardness from the statistically stored dislocations alone, in the absence of any geometrically necessary dislocations, and

\[
h^* = \frac{8}{3} b a^2 \tan^2 \theta (\frac{H}{H_0})^2
\]  

(14)

is a length scale for the depth dependence of hardness.

From Equation (12), it can be seen that the indentation hardness \( H \) is related only to indentation depth \( h \) as \( h^* \) and \( H_0 \) are material constants which can be obtained by fitting the experimental results.

After Nix and Gao [67], many other researchers continue to observe ISE through experiments and simulations. Most of them explained the size effect via the strain gradient theory (Ma and Clarke [68], Fleck et al. [48], Nix and Gao [65], Poole et al. [69], Stelmashenko et al. [70], Gao et al. [71,72], Acharya and Bassani [73], Huang et al. [74], and Gurtin [75]). They believed that ISE must have a relationship with the strain gradient as the geometrically necessary dislocation density \( \rho_G \) is usually related to an effective strain gradient \( \eta \) as

\[
\rho_G = \frac{2\eta}{b}
\]  

(15)

According to Equation (9), strain gradient was inversely proportional to the indentation depth \( h \), which meant strain gradient should be larger at the shallow depth.

However, Demir, Raabe and Zaafarani [76] expressed a different theory about ISE. They thought as \( \rho_G \) is the GND density that is required to accommodate a curvature \( \omega \), the crystallographic misorientation between two neighboring points can be used as an approximate measure for the GNDs as shown in the following equation:

\[
\rho_G = \frac{\omega}{b}
\]  

(16)

According to Equations (15) and (16), the size dependence of indentation hardness has been associated with strain gradients which exist in the lattice through GNDs. Thus, these researchers decided to directly measure lattice rotations below indents with the aim of quantifying the density of these defects. For this purpose they performed an experiment using a tomographic high-resolution electron backscatter diffraction orientation microscope in conjunction with a focused ion beam instrument to map the orientation distribution below four nanoindents of different depths. Unfortunately, the experimental result contradicted the commonly expected inverse relationship between the indentation depth and the density of the GNDs. In terms of GND-based strain gradient theories, larger GND densities should appear at shallow indentation depth, not at a deep one. But their experiment showed an opposite trend that the total GND density below the indents reduces with decreasing indentation depth. According to the experimental results, they concluded that the explanation size-dependent material strengthening effects by using average density measure for GNDs was not sufficient to understand the indentation size effect.

Kiener [57] investigated Nix-Gao model with the cross-sectional EBSD method and proposed that Nix-Gao model’s physical basis was still under debate, and its validity cannot be addressed alone with load versus displacement characteristics. There were two assumptions with respect to the Nix-Gao model, hemispherical plastic zone and self-similarity of the evolving deformation structure. However, according to the EBSD observation shown in Figure 17, it is clear that the true plastic deformed zone deviates from the assumption of a half-sphere. Other reports indicated that there were differently shaped deformation areas, depending on the indenter geometry [45,77,78]. Regarding the self-similarity, based on the Nix-Gao model, the strain gradient induced by the indenter should be determined solely by the indenter geometry. Therefore, it should be constant for self-similar indenter shapes, which means the observed misorientations should depend only on the indenter angle and not on the indent size. However, the observations for Vickers indents in copper and tungsten displayed that the maximum misorientation was along the indent flanks for different sizes, as shown in Figure 25.
Furthermore, Nix-Gao model assumed that GNDs would accommodate the impression geometry at very low indentation depth for metallic materials with no pre-existing defects, such as single-crystal metals without any deformation. Subsequently, it was generally accepted that ISE would not exist in materials with pre-existing high dislocation densities, such as ultrafine-grained materials [79] and amorphous materials. However, recently Smedskjare [80] and Liu et al. [81] found ISE existing in oxide glasses and photonic crystals, respectively. Obviously, all of these materials are not crystalline metallic materials. Therefore, it is concluded that ISE may commonly exist in natural materials, not only in crystalline materials.

![Image](image_url)

**Figure 25.** Maximum misorientation angle measured along the flanks of the indent for different sized Vickers indents into fcc copper (closed squares) and bcc tungsten (open squares) [82,83]. Reproduced with permission from D. Kiener et al., JOM; published by Springer, 2009.

Meyer’s law is another widely used method to describe ISE. For the indenters which have ideal geometry, the relationship between the test load and the resultant indentation diagonal length curve could be obtained from [67]

\[ P = C \cdot d^n \]  

(17)

where \( P \) is the load, \( d \) is the diagonal length of impression, \( C \) is the material/indenter constant and \( n \) is the Meyer index due to the curvature of the curve. Since \( d \) is proportional to the contact depth \( h_c \) which in turn is proportional to the indentation depth \( h \), Equation (17) could be expressed as follows:

\[ P = C' \cdot h^n \]  

(18)

where \( C' \) is constant and \( h \) is the indentation depth.

Fischer-Cripps [84] mentioned that if the plastic zone was fully developed (beyond elastic-plastic transition point), the load-displacement (\( P-h \)) curve of the loading section could be related to the square of the displacement (\( P = C h^2 \)). As for the loading stage of the \( P-h \) curve in the elastic-plastic field, Sakai [85] stated that the load is proportional to the square of the indentation depth. According to Equation (17), if \( n = 2 \), the materials shows no ISE. But if \( n < 2 \), the materials shows ISE and this case was confirmed by different materials [86,87].

Considering aforementioned facts, Ebisu and Horibe [67] analyzed the relationship between the \( P-h \) curve and ISE behaviour in their experiments by differentiating the \( P-h \) curves of the three samples. They found that for single 8Y-FSZ (8 mol %Y\(_2\)O\(_3\)-ZrO\(_2\) single crystal) in the load range of 200–1900 mN, the index \( n \) calculated from the \( P-h \) curve was 1.873, which suggests that single 8Y-FSZ showed ISE behaviour. They also found this ISE result agreed well with the experimental results of another report [88] in which the hardness decreased as the indentation increased between the load range of 100–2000 mN. The same procedure was conducted in the 12Ce-TZP \( P-h \) curve and they found \( n = 1.808 \) within the load range 200–1900 mN. It also was consistent with the results (ISE behaviour).
from zirconia ceramics [88,89]. However, for fused quartz, index \( n = 1.961 \) calculated from \( P-h \) curve in the load range of 200–1900 mN meant that this material showed almost no ISE behaviour [67]. This agreed with Oliver and Pharr’s report [18] which stated that quartz showed very little indentation size effect.

Kolemen [90] conducted the same experiments with superconductors, which showed a apparent ISE. He then concluded that for hard materials like brittle ceramics at low indentation loads, \( n \) is significantly less than 2. According to Onitsch [82], \( n \) lied between 1 and 1.6 for hard materials and higher than 1.6 for soft materials.

However, Peng et al. [91] pointed out the correlation between \( n \) and \( C \) seemed to be of little significance for understanding the ISE, as their previous study has showed that the best-fit value of the Meyer’s law coefficient \( C \) depended on the unit system used for recording the experimental data and completely different trends of \( n \) versus \( C \) may be observed in different unit systems [92] as shown in Figure 26.

![Figure 26. Variation of Meyer’s law coefficient C with Meyer’s exponent n. Note that completely different trends are observed when different unit systems were used for recording the experimental data [92]. Reproduced with permission from JianghongGong et al., Proceedings of Journal of the European Ceramic Society; published by Elsevier, 2000.](image)

The first unit system used is \( P \) in Newton (N) and \( d \) in millimeter (mm) and the second is \( P \) in gram (g) and \( d \) in micrometer (mm). As can be seen from Figure 26, completely different trends of \( n \) versus \( A \) were observed in different unit systems. Similar conclusions were reported by Li and Bradt [93] when they analyzed the experimental data on single crystals. Therefore, they concluded that a particular care should be taken when analyzing the microstructural effects on the measured hardness based on Meyer’s power law.

It should be noted that only \( n \) plays an important role in determining ISE in Meyer’s law and it is not necessary to consider the variation of Meyer’s law coefficient \( C \). Although numerous researchers used Meyer’s law to analyse ISE, all of them just fit the whole \( P-h \) curve. In fact, the \( P-h \) curve can be fitted separately from the ISE-boundary which is shown as in Figure 27. In the left side of ISE-boundary an \( n \)-value smaller than 2 can be obtained, while an \( n \)-value of about 2 can be achieved in the right side.
Some other factors may influence the ISE, which include: inadequate measurement capabilities of extremely small indents [94], presence of oxides or chemical contamination on the surface [95], indenter-sample friction [96], and increased dominance of edge effects with shallow indents [68].

Elmustafa and Stone [97] proposed a vast number of hypotheses to explain the ISE, including: friction, and lack of measurement capabilities, and surface layers, oxides, chemical contamination and dislocation mechanisms. To calculate the hardness for the nanoindentation measurements, indents were imaged in calibrated optical and scanning electron microscopes. However, because of the inaccuracies inherent to “optical” method, they did not just rely on them alone. In addition, they used contact stiffness as a method to determine indirectly the projected contact area. Interestingly, the two methods agreed very well.

Elmustafa et al. [97] conducted experiments using alpha brass and aluminium as samples. It has been found that the oxide on a fresh surface of alpha brass is less than 5 nm thick, while the oxide thickness on an aluminium surface is only 1–3 nm [98]. For Elmustafa et al.’s experiment, the smallest indents were approximately 0.3 um across or 60 times larger in lateral dimensions than the oxide thickness. Therefore, the oxide layer would not greatly affect the hardness.

The indenter piling-up or sinking-in was also seen as a factor that influences ISE. McElhaney et al. [99] did numerous experiments and found that the indenter piling up and sinking in had a huge effect on the micro-indentation hardness. However, after very careful examination, they found the indentation hardness still displayed strong dependence on the penetration depth. This observation displayed that the indenter piling up and sinking in cannot explain the depth-dependent indentation hardness alone.

Loading rate was raised as another influence factor for ISE because usually materials tended to display larger a plastic work hardening at a large strain rate (loading rate) [100]. The strain rate in the indented material should be proportional to the ratio \( \frac{h}{h_{\text{ref}}} \), where \( h \) is the rate of change of the indentation depth and \( h_{\text{ref}} \) is the indentation depth. It is not hard to understand that for a constant rate of indentation depth \( (h = \text{constant}) \), the strain rate should be very huge at the initial penetration. However, Lilleodden [101] performed indentation test at a constant ratio \( \frac{h}{h_{\text{ref}}} \) and still observed the phenomenon of ISE.

Indenter tip radius was regarded as another factor which affected ISE. However, McElhaney et al. [99] and Huang et al. [102] found that the sharp indenter tip radius less than 100 nm had definitely no influence on the micron and sub-micron scale indentation, which indicated that indenter tip radius cannot be used to explain the ISE observed in the indentation test with sharp indenters.
5. Simulations of Mechanical Behaviours of Materials Undergoing Nanoindentation

5.1. Conventional Finite Element Method (FEM) Simulations

Lee and Kobayashi’s work [103] was the first to conduct the finite element simulation (FEM) of indentation in 1969. Plane strain and axisymmetric flat punch indentation was simulated to study the development of the plastic zone, the load-displacement relationships, and the stress and strain distributions during continued loading, taking into account the changes of the punch friction and sample dimensions. However, problems such as the accuracy of the solutions and the efficiency of the computation still existed. Then three years later, Lee and his colleagues [83] performed another finite element simulation of indentation using ball indenter, and compared all the results with their own experiments for heat-treated SAE4340 steel. It was found that the simulated load-displacement curve, plastic zone development and indentation pressure were in good agreement with the experimental observations. In addition, by calculating the mean effective strains with FEM, the representative strains defined by Tabor were found to be equal to the mean effective strains of the plastic zone under the indenters shown in Figure 28.

Bhattacharya and Nix [104] performed elastoplastic FEM simulations of nanoindentation using conical indenter to study the elastic and plastic properties of materials on a sub-micro scale under the conditions of frictionless and completely adhesive contact. The simulated load-displacement curves for nickel and silicon were compared with experimental results as shown in Figures 29 and 30, respectively. It was concluded that the FEM is suitable to simulate nanoindentation behaviour at a sub-micro scale for different types of materials. Bhattacharya and Nix [105] then investigated the relationship between Young’s modulus and yield strength, and concluded from FEM simulation that the shapes of the plastic zones for an elastic-plastic bulk material under a conical indenter depend strongly on the ratio $E/\sigma_y$ (Young’s modulus/yield stress) with a fixed indenter angle as shown in Figure 31.

Figure 28. Strain contours and elastic-plastic boundaries under the load of (a) 978 kg; (b) 1423 kg; (c) 2224 kg and (d) 3000 kg (—FEM; —-experiment) [83]. Reproduced with permission from C.H. Lee et al., International Journal of Mechanical Sciences; published by Elsevier, 1972.

Figure 29. Comparison between the results from the present Finite Element Method (FEM) analysis and those from Pethica et al. [106] on indentation of nickel [104].
was validated using "pseudo-experimental" (computer generated) data with and without noise.

Chen et al. [126] proposed two alternative indentation techniques to effectively distinguish elastoplastic material parameters via FEM indentation simulation, and their proposed methodology has been well understood. This work must be done through the crystal plasticity based simulation.

5.2. Crystal Plasticity FEM Simulation

Most of the researchers thought the conventional plasticity theory cannot be used to explain ISE because its constitutive models possess no intrinsic internal material lengths. However, Storakers et al. [106] did observe the reversed ISE through simulation by using a parabola-shaped indenter. Furthermore, recently Maier et al. [123–125] proposed an inverse analysis method to identify the elastoplastic properties of the mystical materials which have distinct elastoplastic properties yet they yield almost identical indentation behaviors, even when the indenter angle is varied in a large range. The evolution of crystallographic texture and grain lattice rotation under the indentation has not been well understood. This work must be done through the crystal plasticity based simulation.

Subsequently, FEM nanoindentation simulation of thin films [107–110], stress distribution [111–113], hardness [114–116], friction effects [109,117], brittle cracking behaviour [118–120] and coatings [121,122] were extensively developed.

Figure 29. Comparison between the results from the present Finite Element Method (FEM) analysis and those from Pethica et al. [106] on indentation of nickel [104]. Reproduced with permission from A.K. Bhattacharya et al., International Journal of Solids and Structures; published by Elsevier, 1988.

Figure 30. Comparison between the results from the present FEM analysis and those from Pethica et al. [106] on indentation of silicon [104]. Reproduced with permission from A.K. Bhattacharya et al., International Journal of Solids and Structures; published by Elsevier, 1988.

Figure 31. Comparison of the yield zones at a particular indenter angle of 136° for various $\frac{E}{\sigma_y}$ ratios for a depth of indentation of 203 nm [105]. Reproduced with permission from A.K. Bhattacharya et al., International Journal of Solids and Structures; published by Elsevier, 1991.

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properties of the mystical materials which have distinct elastoplastic properties yet they yield almost identical indentation behaviors, even when the indenter angle is varied in a large range.

Most of the researchers thought the conventional plasticity theory cannot be used to explain ISE because its constitutive models possess no intrinsic (internal) material lengths. However, Storakers et al. [127] did observe the reversed ISE through simulation by using a parabola-shaped indenter.

5.2. Crystal Plasticity FEM Simulation

The evolution of crystallographic texture and grain lattice rotation under the indentation has not been well understood. This work must be done through the crystal plasticity based simulation.

Casals and Forest [128] investigated the anisotropy in the contact response of FCC and HCP (hexagonal closest-packed) single crystal via simulating spherical indentation experiments of bulk single crystals and thin films on hard substrates. Their simulations predicted that the plastic zone beneath the indenter preferentially grew along the slip system directions as shown in Figures 32 and 33. Consequently, in coated thin film systems, a prominent localization of plastic deformation occurred at those specific regions where slip system directions intersected the substrate. Meanwhile, these specific areas were prone to crack nucleation in terms of accumulative plastic damage. Therefore, the identification of these areas was meaningful for the prediction of potential delamination and failure of the coatings. Casals et al. [129] also used three-dimensional crystal plasticity finite element simulations to examine Vickers and Berkovich indentation experiments of strain-hardened copper. The results showed that the simulation was in a good agreement with experimental observations with respect to hardness, load-displacement curves, material piling up and sinking in development at the contact boundary.

![Figure 32](image-url)

**Figure 32.** Details of the indentation-induced plastic zone in the simulations concerning face centered cubic (FCC) copper crystals. (a,c,e) correspond to the (001), (011) and (111) indented planes of bulk crystals. (b,d,f) correspond to their thin film counterparts. Plastic zone is assessed by considering the total accumulated plastic strain variable. White arrows point to the specific locations where high plastic strain localization occurs within the coating-substrate interface. Penetration depth in the figures is $h_s = 3.5 \, \mu m$ [128]. Reproduced with permission from O. Casals et al., Computational Materials Science; published by Elsevier, 2009.
was governed by the crystallography of FCC crystals on the indented surface. Plasticity finite element simulation by recourse to the Bassani and Wu hardening model for pure FCC crystals. The anisotropic nature of the surface topographies around the imprints four-fold symmetric piling-up patterns were observed on (011), (111), and (100) oriented surface with micro level to the macro level as shown in Figure 35. They also investigated the orientation effects in simulation approach for determining meso-plastic model parameters works reasonably well from in the hardening model was determined by fitting the simulated load-displacement curves to the experimental observations with respect to hardness, load-displacement curves, material piling up strain localization occurs within the coating-substrate interface. Penetration depth in the figures is $h = 3.5 \mu m$ [128]. Reproduced with permission from O. Casals et al., Computational Materials Science; published by Elsevier, 2009.

Alcala et al. [130] analysed Vickers and Berkovich indentation behaviour via extensive crystal plasticity finite element simulation by recourse to the Bassani and Wu hardening model for pure FCC crystals. The simulated results have been used to illustrate the impact of the crystallographic orientation, as shown in Figure 34. It was clear that the irregular appearance of pyramidal indentations was governed by the crystallography of FCC crystals on the indented surface.

Figure 33. Details of the indentation-induced plastic zone in the simulations concerning hexagonal closest-packed (HCP) zinc crystals. (a,c) correspond to the basal and prismatic indented planes of bulk crystals. (b,d) correspond to their thin film counterparts. White arrows point to the specific locations where high plastic strain localization occurs within the coating-substrate interface. Penetration depth in the figures is $h = 3.5 \mu m$ [128]. Reproduced with permission from O. Casals et al., Computational Materials Science; published by Elsevier, 2009.

Figure 34. Imprint morphologies for Vickers indentation in the (001) plane for different orientations (rotations) of the tip. (a) The slip directions at the surface coincide with the edges of the indenter (arrows indicate development of pincushion effects); (b) The slip directions coincide with the sides of the indenter; (c) Intermediate orientation to those described in (a,b) [130]. Reproduced with permission from J. Alcala et al., Journal of the Mechanics and Physics of Solids; published by Elsevier, 2008.
Liu et al. [131] implemented crystal plasticity constitutive model initially developed by Peirce et al. [132] in a finite element code ABAQUS/Explicit to study the material behaviour of nanoindentation on (001) oriented surface of single crystal copper. All of the appropriate meso-plastic parameters used in the hardening model was determined by fitting the simulated load-displacement curves to the experimental data. Their studies demonstrated that the combined nanoindentation/CPFEM simulation approach for determining meso-plastic model parameters works reasonably well from micro level to the macro level as shown in Figure 35. They also investigated the orientation effects in nanoindentation of single crystal copper [133]. Simulated load-displacement curves were found to be in agreement with those from experimental tests as shown in Figure 36. Meanwhile, two-, three-, and four-fold symmetric piling-up patterns were observed on (011), (111), and (100) oriented surface with respect to CPFEM simulation. The anisotropic nature of the surface topographies around the imprints in different crystallographic orientations of the single crystal copper samples then were related to the active slip systems and local texture variations. Wang et al. [40] had similar observations while performing a 3D elastic-viscoplastic crystal plasticity finite element method simulation to study the dependence of nanoindentation piling-up patterns. Their simulation showed that the piling-up patterns on the surface of (001)-, (011)- and (111)-oriented single crystal copper had four-, two-, and sixfold symmetry, respectively. All the simulated piling-up patterns were in agreement with those from the experiments. The explanations of the anisotropic surface profiles were also related to the active slip systems and local texture variations.

Figure 35. (a) Results of FEM simulations showing the variation of the indentation force, F with indent diameter, 2a for different indenter radii, R; (b) Results of indentation experiments showing the variation of the indentation force, F with indent diameter, 2a for different indenter radii, R [131]. Reproduced with permission from Y. Liu et al., Journal of the Mechanics and Physics of Solids; published by Elsevier, 2005.
from the experiments. The explanations of the anisotropic surface profiles were also related to the active slip systems and local texture variations.

**Figure 35.**
(a) Results of FEM simulations showing the variation of the indentation force, $F$ with indent diameter, $2a$ for different indenter radii, $R$; (b) Results of indentation experiments showing the variation of the indentation force, $F$ with indent diameter, $2a$ for different indenter radii, $R$ [131].

**Figure 36.** Comparisons between numerical and experimental load-displacement curves on copper samples of different crystallographic orientations made with a spherical indenter (tip radius $3.4 \mu m$): (a) (100) plane; (b) (011) plane and (c) (111) plane [133]. Reproduced with permission from Y. Liu et al., International Journal of Plasticity; published by Elsevier, 2008.

Zaafarani et al. [45] carried out the 3D elastic-viscoplastic crystal plasticity finite element simulations with the same geometry of indenter and boundary conditions as those from experiments. Their CPFEM simulations predicted a similar pattern for the absolute orientation changes as the experiments as shown in Figure 37. However, it was found that the simulations over-emphasized the magnitude of the rotation field tangent to the indenter relative to that directly below the indenter tip. The reason was then found to be due to edge effects at the contact zone and milling-induced curvature caused by ion beam so that no complete EBSD mapping could be made up to the actual contact interface [134].
Figure 37. Rotation maps for a set of successive (11\(\text{2}_{\text{a}}\)) sections perpendicular to the (111) indentation plane (surface plane perpendicular to the plane presented) with different spacing to the actual indent [45]. The images on the left-hand side (a–h) were obtained from viscoplastic crystal plasticity simulations. The corresponding maps on the right-hand side (i–p) were determined via EBSD measurements in succeeding planes prepared by serial FIB sectioning. The color code shows the magnitude of the orientation change relative to the initial crystal orientation without indicating the rotation axis or rotation direction. Scaling is identical for all diagrams. Reproduced with permission from N. Zaafarani et al., Acta Materialia; published by Elsevier, 2006.

Eidel [135] simulated pyramidal micro-indentation on the (001) surface of Ni-base superalloy single crystal with three different azimuthal orientations of the pyramidal indenter. The numerical piling-up patterns were compared with the experimental results. It was found that the resultant material piling-up was insensitive to different azimuthal orientations of the pyramidal indenter as shown in Figure 38. The reason could be due to the piling-up formation determined by crystallographic processes rather than by the stress distribution pattern, induced under the non-isotropic pyramidal indenter. He then also found that the piling-up was independent of the indenter shape (sphere or pyramid) and the elastic anisotropy, which further confirmed that only the geometry of the slip systems in the (001) oriented crystal governed piling-up, whereas stress concentrations introduced by different indenter shapes, by the azimuthal orientation of a pyramidal indenter and also by the characteristics of the elasticity law, had no significant influence.

Liu et al. [136] simulated indentation process of single-crystal aluminium with three different initial orientations via using three-sided Berkovich indenter, and all the numerical load-displacement curves and pile-up patterns from CPFEM have been validated by experimental observations, as shown in Figures 39–41. CPFEM simulation was also used to explain the anisotropic feature of pile-up patterns for different single crystals in details [137,138]. Recently, indentation on severely deformed materials [139] and bicrystalline ones [139] were also investigated via CPFEM modelling.
Figure 38. Pyramidal indentation experiments into (001) FCC CMSX-4. Left: experiment (SEM); right: simulation with isolines of height, uz (µm), for azimuthal orientation angle θ = 0°, 22.5°, 45° in row 1–3. In the coordinate system, X-, Y-, Z-axes each represent h001i directions. The white stains in the experimental indentation craters are debris from sputtering [135]. Reproduced with permission from Y. Liu et al., International Journal of Plasticity; published by Elsevier, 2008.
Figure 39. Comparisons between numerical and experimental load-displacement curves for single-crystal Al samples: (a) (001); (b) (101) and (c) (111) surfaces [136].

Figure 40. Atomic-force microscopy (AFM) images of the indent impressions made on a single-crystal Al workpiece with a Berkovich indenter (tip radius 200 nm) at different crystallographic orientations: (a) (001), (b) (101) and (c) (111) surfaces [136].
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Figure 41. Simulated images of the indent impressions on a single-crystal Al workpiece with a Berkovich indenter (tip radius 200 nm) at different crystallographic orientations: (a) (001); (b) (101) and (c) (111) surfaces [136].

6. Conclusions

Nanoindentation is the most popular method to investigate the mechanical properties of materials at micro- and nanoscale. The key advantage of this technology is its convenience and applicability on a very small sample where normal tensile test cannot be applied. A vast number of experiments have been conducted to investigate different characters during indentation deformation, including hardness, Young's modulus, load-displacement curve, ISE, piling up and sinking in, cracks, texture evolution and lattice rotation and so on. Meanwhile, a wide range of materials were studied, such as metals, ceramics, rubbers, human bones, coatings, etc.

Indentation size effect has been extensively studied by numerous researchers. Among all of these researchers, Nix and Gao has proposed a strain gradient model which was believed to be the best way to simulate and explain ISE in the past. However, it has been found that the main assumptions for that model are in conflict with the experimental observations. Other potential influence factors, such as inadequate measurement capabilities of extremely small indents, presence of oxides or chemical contamination on the surface, indenter-sample friction, increased dominance of edge effects with shallow indents and tip radius have been eventually proven to be ineffective in determining the ISE. Therefore, the mechanism of ISE needs to be further investigated and discussed.
6. Conclusions

Nanoindentation is the most popular method to investigate the mechanical properties of materials at micro- and nanoscale. The key advantage of this technology is its convenience and applicability on a very small sample where normal tensile test cannot be applied. A vast number of experiments have been conducted to investigate different characters during indentation deformation, including hardness, Young’s modulus, load-displacement curve, ISE, piling up and sinking in, cracks, texture evolution and lattice rotation and so on. Meanwhile, a wide range of materials were studied, such as metals, ceramics, rubbers, human bones, coatings, etc.

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The conventional FEM has been used to study the indentation process on materials and to predict their hardness, stress distribution, friction effects, Young’s Modulus, load-displacement curves, and brittle cracking behaviour and so on. However, the anisotropic characters of materials could not be taken into account in the conventional FEM. Therefore, Crystal plasticity FEM (CPFEM) which considers the lattice rotation and the plastic slip as the key deformation mechanism has been used to simulate the texture evolution of materials during indentation deformation. All the numerical results can be accurately validated by comparing with experimental observations. In addition, CPFEM is also the best candidate to investigate the deformation mechanism of materials at smaller scale.

Acknowledgments: The authors acknowledge the financial support from an Australian Research Council Discovery Grant (DP0773329) and from UPA and IPTA scholarships from the University of Wollongong and from Japan Society for the Promotion of Science (JSPS).

Conflicts of Interest: The authors declare no conflicts of interest.

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