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Behaviour of subballast reinforced with used tyre and potential application in rail tracks

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Abstract

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Behaviour of Subballast Reinforced with Used Tyre and Potential Application in Rail Tracks

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ABSTRACT

Rubber tyres have a three dimensional cylindrical structure, and as such could be used to stabilise foundations by increasing the bearing capacity and reducing settlement for transport infrastructure. It is therefore expected that in railroad engineering, a capping layer reinforced with rubber tyres could help to reduce the thickness of the granular layer (i.e. ballast), improve the track bearing capacity, and reduce the frequency of maintenance. However, there is a notable gap between the conceptual theories and real-life applications pertaining to the mechanisms of rubber tyre-reinforced foundations. In pavement engineering, the bearing capacity is closely linked to plate load tests. In this study, plate load tests were carried out on a single tyre filled with subballast material and subjected to a vertical load. This testing process was then modelled using the Finite Element software ABAQUS to study and quantify the interaction between the tyre and the granular medium. The experimental and numerical results reveal that the rubber tyre can significantly increase the modulus and ultimate bearing capacity of the granular layer. The numerical process was further extended to a finite element track model to demonstrate the expected response of a ballasted railway track with and without tyre reinforcement.

Key words: used tyre, reinforcement, gravel, rail track, Finite Element Modelling

1. INTRODUCTION

There is an ongoing demand in Australia and around the world to increase the speed and freight capacity of railroad transportation, but heavier axle loads and higher speeds could exert higher dynamic wheel loads on track structure with more repetitions; as a consequence, a soft subgrade may experience higher repeated stresses which may lead to progressive shear failure and excessive deformation (Li and Selig, 1998a). Moreover, under heavier dynamic loads the existing railway track may degrade further and faster due to unacceptable track deformation and the lateral spread of ballast, all of which leads to more frequent maintenance (Sun et al., 2016).

Over the past decades, geosynthetics such as geogrid and geocell have been used to improve the performance of embankments (Bathurst and Raymond, 1987; Göbel et al., 1994; Raymond, 2002; Shin et al., 2002; Raymond and Ismail, 2003; Brown et al., 2007; Fernandes et al., 2008; Indraratna et al., 2006; Webster and Alford, 1978). Several studies have already demonstrated that geogrid reinforcement reduces the settlement and degradation of ballast (Bathurst and Raymond, 1987; Brown et al., 2007; Indraratna and Salim, 2003; Indraratna et al., 2007; Qian et al., 2015). The main principle of geogrid reinforcement is to provide better grain interlocking that restricts the lateral movement of ballast. A layer of geogrid and geotextiles placed at the interface between ballast and subballast often gives encouraging results (Giroud and Han, 2004; Shin et al., 2002). Geocell arrangements could provide additional internal confining pressure and reinforcement to the gravel, which would then reduce the maintenance costs and enhance track serviceability. When a geogrid is installed between the layers of ballast and subballast, it interacts with the surrounding grains to carry the tensile loads imposed by repeated train loadings. However, this interaction depends primarily on the geometry, stiffness and cross-sectional shape of the rib, and its strength at the junctions (Shukla and Yin, 2006; Brown et al., 2007; Palmeria,

2009). Railway organizations do not usually use geocells to confine the upper ballast because it may lead to problems with track maintenance when machinery is used to replace the ballast; but despite this problem, reinforcing the underlying subballast with geocells is an economic and feasible alternative (Indraratna et al, 2015). During loading, additional confinement is mobilised in the geocell which helps to stop the granular mass of subballast from spreading laterally, and by increasing the rigidity of the infill, geocells also improve the load-carrying capacity (Zhang et al., 2010; Leshchinsky and Ling, 2012; Sitharam and Hegde, 2013), which in turn improves track performance. Past studies have shown that cellular confinement significantly improves the strength and stiffness of a granular material, even though a lack of generic design methodology has inhibited its implementation (Han et al., 2008).

Scrap tyres are a major source of pollution and pose a serious threat to public health through releasing chemicals and pollutants into the environment. It is estimated that in Australia there are approximately 50 million tyre equivalent passenger units entering the waste stream annually, and this is a major issue for the use of landfill, stockpiles, and illegal dumping. The current reuse of waste tyres for infrastructure is limited because there is no rigorous scientific approach to innovative design and/or to quantify performance through comprehensive field studies, and furthermore, the need to design rail tracks upon which trains could travel at higher speeds is an enormous challenge to the stability and load bearing capacity of present track substructure.

This study will examine the performance of a subballast capping layer reinforced with rubber tyres used to minimise track deformation and improve its bearing capacity. The test system involves a tyre where one sidewall is removed and the tyre is then filled with gravel; a geotextile might then be placed between the rubber tyre and the ground. This concept and application of a tyre-reinforced granular system has three primary engineering benefits: (i) the confinement

provided by the tyre cell would help to increase the stiffness of the contained aggregate, which then reduces vertical strains within the capping and ballast layers; (ii) prevents any lateral movement of the capping material, which would then reduce the deformation of the overlying ballast; and (iii) improves the flexural stiffness of the capping layer which distributes the traffic loads and reduces the maximum vertical stress on the subgrade. The technology proposed in this research is for subballast application, which is a continuous geo-mattress that supports the ballast layer rather than simply placing whole tyres in individual locations within the top ballast layer as possibly trialled elsewhere (but no published scholarly papers found by the authors). Placing tyres in the ballast layer will create practical problems in view of maintenance requirements plus the need to adhere to stringent constitutionalised standards of ballast placement and compaction in some countries such as Australia. The proposed applications in this study are designed to ensure that track construction and subsequent maintenance efforts are not hampered by interference with the tyre cells.

In this study, plate load tests were carried out to investigate the load transfer mechanisms between infill and tyre, and then a finite element model was established to simulate this plate loading procedure. Subsequently, the numerical predictions were compared with experimental results to validate the numerical procedure. Having calibrated the FEM model with a single tyre unit, a plane strain section of half a ballasted substructure was simulated to examine how the foundation would react under load, with or without being reinforced by tyres. The behaviour observed during the numerical simulation included vertical track settlement, the lateral displacement and the deviator stress of the subgrade which represents the combined influence of both vertical and confining stresses.

2. EXPERIMENTAL STUDY

2.1. Material Properties

The subballast (crushed basalt) used in this study came from a local quarry near Wollongong, NSW Australia. The particle size distribution (PSD) for the subballast was within the range specified by the rail industry, as shown in Fig. 1. Direct shear tests were carried out at lower normal stresses to represent the test conditions. The direct shear tests produced a peak friction angle of 39° for this material at 70% relative density (Biabani and Indraratna, 2015).

A rubber tyre (one side wall removed) with an outside diameter of 560 mm, a rim diameter of 330 mm, a width of 150 mm was used to reinforce the subballast. The tensile stress and strain relationships of the rubber were determined by tensile tests conducted in accordance with ASTM D4885-01(2011) at a strain rate of 10%/min, and are shown in Fig. 2. The mean tensile stresses at strains of 2% and 5% were 6.1 and 15.2 MPa respectively, and the mean ultimate tensile strength was around 19.45 MPa. The average thickness of the rubber tyre was around 10 mm, and its tensile stiffness was based on the tensile stress and strain relationship.

In this study, a 80 kN woven geotextile of 2 mm thickness was placed under the rubber tyre for testing purposes; it was manufactured from durable, high-modulus polypropylene yarns woven into a robust, dimensionally stable geotextile. Physical characteristics and technical specification of subballast, subgrade, tyre and geocell used for the study are shown in Table 1.

2.2. Test Setup and Procedures

Six plate load tests were carried out in a test box (i.e. 800 mm long, 600 mm wide and 400 mm high) to investigate the load transfer mechanisms between the infill and rubber tyre, and the 200

mm diameter loading plate set up is shown in Fig. 3. The sample was prepared (in a dry condition) by placing a 50 mm thick layer of compacted clayey sand into the test box to simulate the subgrade soil under the track. The subballast layers were 150 mm and 350 mm thick, and they were compacted to a density of 2100 kN/m^3 in two and four layers, respectively. Compaction was carried out using a vibratory hammer. In the cases where the subballast was reinforced with a rubber tyre, the tyre unit was placed within the test box and then backfilled with gravel. The subballast was both inside and outside the tyre, but a woven geotextile was also placed beneath the tyre to prevent the dissimilar soils from mixing and to allow each soil layer in the test to function as intended. The high tensile strength and low elongation properties of woven geotextiles added further reinforcement to the test sample. With the 350 mm thick subballast, the samples with and without geotextiles were tested and compared. Two 30mm long strain gauges were attached to the interior wall of the tyre to measure the axial and circumferential strains. The surface of the tyre was brushed lightly with a cleaner and degreaser, and an industrial adhesive was applied before mounting the strain gauge. A stainless steel pressure cell (thickness=10 mm, diameter=50 mm, range=500 kPa, accuracy=99.7%) was installed at the interface between the subballast and subgrade to measure the vertical pressure transmitted to the subgrade, as shown in Fig. 3. Another test was designed to evaluate the bearing capacity of a unit cell of rubber tyre and gravel composite; in this test the loading plate was 560 mm and the subballast was placed inside the tyre. Lateral spreading of the tyre was recorded by a linear voltage differential transformer (LVDT).

After the subballast was in place, the loading plate was placed on top of the test sample subjected to a vertical load. The centre of the plate coincided with the centre of the rubber tyre. Controlled displacement tests were carried out at a rate of 0.2 mm/min. The vertical load, axial and lateral

displacement, and the strain that developed inside the tyre were recorded every second during the test.

2.3. Test Results

The results of six plate load tests on unreinforced and reinforced subballast are shown in Fig. 4. In Fig. 4(a & b) for a load of 600 kPa, the vertical stress at the centre of the tyre, and at the interface between the subballast and subgrade was 470 kPa and 264 kPa for Test 1 without reinforcement and Test 2 with reinforcement, respectively. The inclusion of a rubber tyre and geotextile reinforcement reduced the stress transmitted to the subgrade, unlike the subgrade without reinforcement. Similarly, for a 600 kPa load, the stress decreased from 470 kPa to 82 kPa as the subballast increased in thickness from 150 mm to 350 mm in Test 1 and Test 3, respectively (Fig. 4a & c). As expected, the increment of subballast thickness reduced the stress at the interface between the subballast and subgrade. This implies that the rubber tyre and geotextile reinforcement can effectively reduce the thickness of gravel required for real-life track design. The apparent vertical stiffness of the sample, as represented by the initial and linear portion of the load-displacement curve (at 2% strain), could be calculated from the test data in Fig. 4(c&d). In Test 3, without reinforcement, the apparent stiffness was approximately 51.9 kPa/mm, but in Test 4 with tyre and geotextile reinforcement, the approximate stiffness was 78.4 kPa/mm. This result indicated that with reinforcement, Test 4 showed a 51% gain in stiffness compared to Test 3 without reinforcement. When Test 4 (Fig. 4d) in which geotextile was used, is compared to Test 5 (Fig. 4e), the results indicate that the geotextile provides further reinforcement effect. This is more beneficial in the case of thicker layer of subballast.

The strain gauges attached to the inner surface of the tyre confirmed that the strain in the tyre was very small; with circumferential tensile strains of 0.015%, 0.061% and 0.060% under vertical loads of 940, 1610 and 1600 kPa for Tests 2, 4, and 5 respectively, as shown in Fig. 5 (a, b & c). The axial compressive strains for the tyre were 0.0051%, 0.0085% and 0.0027%, respectively. It is very convincing that the tyre could confine the infill materials and maintain its original shape, unlike geocell reinforcement which deforms substantially under testing.

Without doubt the main parameter impacted by utilizing a tyre reinforcement unit is the bearing capacity of the soil, because, the cylindrical structure of the tyre confines the infill material, minimises lateral displacement, and increases its rigidity. Test 6 was carried out on a sample of subballast reinforced with a single tyre, as shown in Fig. 4(f). Here the vertical load reached 6500 kPa with 19.2% axial and 3.3% lateral strains. The strains measured from the inner surface of the tyre are shown in Fig. 5(d), and although the circumferential tensile strain is small (=1.2% in the end of the test), it will induce an additional confining stress $\Delta\sigma_3$ from the rubber tyre to the subballast. In the sample reinforced with a rubber tyre, any further confining stress can be generated through the hoop stress. By assuming that the internal friction angle of gravel for the reinforced sample remained constant, Bathurst and Karpurapu (1993) proposed using the apparent cohesion c_r to account for the increasing strength of the geocell. The apparent cohesion c_r was a result of the increased confining stress $\Delta\sigma_3$ provided by the geocell onto the infill soil where $c_r = \Delta\sigma_3/2 \cdot \tan(\pi/4 + \phi/2)$, and $\phi(=39^\circ)$ is the friction angle of the subballast. The increased stress $\Delta\sigma_3$, as suggested by Bathurst and Karpurapu (1993), can be estimated by the following equation: $\Delta\sigma_3 = 2M/d \cdot [1 - (1 - \epsilon_a)^{0.5}] / (1 - \epsilon_a)$, where $M(=1325000 \text{ N/m})$ is the tensile stiffness of the rubber tyre, $d(=0.56 \text{ m})$ is the initial diameter of the rubber tyre pocket, and ϵ_a is the axial strain of the sample.

Fig. 4(f) shows that as the load increased, displacement increased in the axial and lateral directions, and as a consequence, further confining stress was induced from the tyre to the subballast by the lateral expansion. The variation of additional confinement $\Delta\sigma_3$ and apparent cohesion c_r of the sample is shown in Fig. 6. Here, an increase in the applied stress generally increased $\Delta\sigma_3$ and c_r . There was a sharp increase of $\Delta\sigma_3$ when the load was relatively small (i.e. less than 500 kPa). As the applied load continued, the additional confining stress ($\Delta\sigma_3$) increased at a decreasing rate, but for applied stress greater than 4000 kPa, $\Delta\sigma_3$ increased at a higher rate.

3. NUMERICAL MODELLING OF THE TYRE-SUBBALLAST UNIT

3.1. Models and Material Properties

The commercially available FE software ABAQUS (Hibbitt, Karlsson and Sorensen Inc. 2014), was used in this analysis. To investigate the interaction between the rubber tyre and the subballast, Tests (3&5) with and without tyre reinforcement respectively, were modelled and analysed. The mesh for the reinforced case is shown in Fig. 7(a) as an example, and there was no tyre in the model used for the unreinforced test.

To correctly characterize the tested materials and to attain acceptable results in the Finite Element analysis, reliable testing procedures and correct material data must be adopted. Both subballast and subgrade, in this paper, are represented with a standard Mohr-Coulomb model (linear elastic-perfectly plastic), which has been commonly used to simulate granular materials in transport infrastructure in past well-known studies too (Indraratna and Nimbalkar, 2013; Sayeed and Shahin, 2016). The material parameters for the MC model can be determined using well-established laboratory methods (consolidation and shear).

The relevant deformation and strength properties were obtained from direct shear tests (Biabani and Indraratna, 2015) and large scale cubical triaxial tests (Indraratna et al., 2015). The MC model involves five basic parameters (i.e., Young's modulus E , Poisson's ratio ν , effective cohesion c' , effective friction angle ϕ , and dilation angle ψ). In this study, a subballast with the following properties: $E=2$ MPa, $\nu=0.3$, $\phi=39^\circ$ and $\psi=15^\circ$ has been considered. A small cohesion value of 1 kPa was assigned to the subballast to improve numerical stability and to avoid modelling difficulties such as strain localisation issues at or near sharp singularities (rate of convergence). The rubber tyre was modelled discretely as an elastic material because there was no evidence of plastic damage encountered during the tests. Contact between the rubber tyre and the gravel was modelled as a 'hard normal contact' (i.e. cannot penetrate rubber), and the tangential coefficient of friction was specified by the tangent of two thirds of the internal angle of friction (i.e. 0.45), as is commonly used for soil-reinforcement interaction (Leshchinsky and Ling, 2012). Table 2 summarises the material properties used in this analysis.

The test box was modelled in such a way where the vertical movement was fixed at the bottom boundary and the horizontal movement was fixed along the four side boundaries. Vertical movement was allowed on the top 200 mm diameter surface to simulate the vertical load applied by a rigid plate. The actual experimental and Finite Element simulation were run under displacement-control conditions. Throughout these simulations the vertical displacement and stress under the loading plate, as well as the pressure transmitted to the surface between subballast and subgrade, were compared with the actual test results.

The tyre cell used in this study has an aspect ratio (height/diameter) of 0.27. Thus the conventional aspect ratio of 2 used in testing of earthen materials cannot be used when testing soil confined in a single tyre cell. It is known that aspect ratio influences the shear strength of

soil measured in triaxial compression (Bishop and Green, 1965). The authors agree that the test results in this study may not replicate the exact field data because of the inevitable boundary conditions of the test setup. While recognizing this as a limitation, the observed results still indicate the benefits of the rubber tyre reinforcement albeit not being able to directly translate the magnitudes of experimental measurements to the field.

However, in order to study the implications of boundary and dimensional effects, a sensitivity analysis was carried out for a reinforced model with varying dimensions. Maximum lateral displacements of the tyre reinforced subballast obtained from the models were compared at a load displacement of 40 mm (Figure 7b). The results show that when the model (mesh) dimension is increased, the maximum lateral displacement decreases, and when the maximum dimension is greater than 3m, the corresponding decrease in lateral displacement becomes insignificant. Based on these preliminary observations, it can be concluded that the effect of boundary conditions may only be marginal when the mesh dimension is at least 5 times that of the tyre diameter.

3.2. Numerical Results and Analyses for Laboratory Testing

As Fig. 4(c & e) shows, the load-deformation relationships for reinforced and unreinforced tests agreed reasonably well with the experimental and FEM analysis results, and moreover, the vertical displacements decreased by the inclusion of a rubber tyre for the same load magnitude, which agrees with the experimental results. The main benefit of a rubber tyre is to confine the subballast, as shown by the tests results in Fig. 6, while Fig. 8 shows the patterns of vertical and lateral displacement for the unreinforced and reinforced test simulations. Fig. 8 (a & b) also shows that the patterns for the two cases were similar, i.e. compression under the load plate, but

276 vertical displacement for the unreinforced subballast was greater than the reinforced subballast,
277 albeit under the same vertical load.

278 Fig. 8(c & d) show the contours of lateral displacement for the unreinforced and reinforced cases,
279 and they show that the largest lateral displacement developed under the edge of the load plate.
280 The comparisons in Fig. 8(c & d) show that the maximum lateral displacement for unreinforced
281 subballast was approximately 1.8 times more than the reinforced subballast under the same load.
282 Clearly, this reduction in horizontal displacement of the reinforced set up has resulted due to the
283 confinement provided by the rubber tyre.

284 Lateral deformation along the x-direction of the tyre is shown in Fig. 9. Here the numerical
285 simulation indicates that the rubber tyre expanded outwards as shown in Fig. 4(f). As the applied
286 pressure increased from 50 kPa to 1500 kPa the maximum displacement of the rubber tyre
287 increased from 0.077 mm to 2.44 mm, but when the load is relatively small (i.e. 50 kPa),
288 maximum displacement occurred around the mid-height of the tyre. When the load increased to
289 1500 kPa, the maximum displacement moved towards the bottom of the tyre while the top edge
290 moved inwards, as shown in Fig. 9.

291 Fig. 10 shows the forces in the tyre at 1500 kPa; there is compression near the top edge of the
292 tyre which corresponds to an inward movement of the top edge as shown in Fig. 9. Moreover,
293 tension developed in the tyre in the lateral direction (Fig. 10) where it was highest approaching
294 the bottom edge of the tyre. This result is consistent with the distribution of displacement shown
295 in Fig. 9. The shear stresses at the interface between the tyre and subballast are presented in Fig.
296 11 (a & b), where the highest interface shear stresses developed near the bottom and close to the
297 edge of the tyre.

4. PRACTICAL APPLICATION WITH A LAYER OF REINFORCED SUBBALLAST

Validation through numerical modelling adds credibility when simulating a practical application of a tyre-reinforced railway track. Hence, a finite element 3D analysis was conducted to model the behavior of the capping layer composed of infilled rubber tyres.

4.1. Track System Geometry

As with a traditional railway track system, the steel rails in this study are supported on reinforced concrete sleepers spaced at 0.60 m centres. The rail head is 0.075 m wide, the web is 0.018 m wide, and the base 0.15 m wide. The concrete sleepers were embedded into a layer of coarse granular aggregate (ballast). For a standard gauge track, a sleeper of 2.50 m in width was bevelled to a maximum height of 0.20 m at the ends and 0.15 m at the centre. The ballast layer was 4 m wide at the base, 3 m wide at the crest, and 0.35 m high, with a slope of 1:1. The layer of subballast confined by rubber tyres was 6 m wide at the base and was 0.25 m thick. A typical passenger car tyre was simulated as being 0.15 m wide, 0.56 m in diameter, and 0.01 m thick. The simulated geometry of the track is shown in Fig. 12.

4.2. Loading

The analysis was based on a typical modern freight car used by Australian railways to transport heavy bulk materials such as coal, construction materials, and aggregates. Traditionally, these have an axle load of 25 tonnes, which corresponds to a static wheel load of 122.5 kN. It is common practice to conduct a pseudo-static analysis in which the dynamic effects are considered by multiplying the static load by a dynamic amplification factor (DAF). In conventional practice, DAF is used as a function of static (wheel) load and train velocity to obtain the equivalent dynamic load (Li and Selig, 1998b). The American Railway Engineering Association (AREA)

recommends the expression for $DAF=1+0.0052V/D$, where V is the train velocity in kilometres per hour and D is wheel diameter in metres (AREA, 1996). A 25t axle load train moving at 100 km/h speed was simulated in this study.

4.3. Finite Element Model for Rail Track

A plane strain slice of the cross section of half a ballasted railway substructure was modelled by a finite element mesh refined to observe the track settlement, lateral displacement of the ballast slope, and the subgrade stress of the foundation with or without rubber tyres reinforcing the subballast layer. The ballast was modelled as linearly elastic-perfectly plastic material with a Mohr-Coulomb failure criterion. The material parameters for the subballast, subgrade, and rubber tyre were the same as the plate load test simulation (Table 2). The tyres were modelled as perfect cylinders, and the contact between the tyres was considered smooth for simplicity. The sleepers and rails were modelled as non-yielding linear elastic material, whose significantly greater stiffness compared to the ballast, foundation and rubber tyres, replicated a composite structure (Table 2).

To properly configure a railway structure requires a true three-dimensional (3D) Finite Element analysis, but the track width along the assumed plane strain direction could be established by considering the loading characteristics and boundary conditions. Selig and Waters (1994) suggested that based on track deflections, a set of three sleepers would be sufficient to represent track response in the longitudinal direction. The transverse width of the plane strain model was assumed to be 1.9 m, and by exploiting centreline symmetry, only half the track was modelled. The FEM mesh with the subballast reinforced with rubber tyres consisted of 22548 elements and 36761 nodes (Fig. 13), while the model with unreinforced (no tyres) subballast only consisted of

15050 elements and 24608 nodes. The ballasted track and foundation were meshed with hexahedral 8-noded elements with reduced integration points (C3D8R). Interaction between different layers of gravel was modelled with the same strategy used to simulate the unit cell. In order to simulate railway field conditions, plane strain condition was applied to the model where the strain in the longitudinal direction was considered insignificant compared to lateral transverse strain. By taking advantage of symmetry, only half of the embankment and foundation was modelled. The vertical planes along the outer edge of the foundation were constrained from lateral displacement in the x-direction, and the same constraint was affixed to the x-y planes to prevent lateral displacement in the z-direction. The base of the model was restricted from any displacement as conventionally required for a FEM mesh, i.e. non-displacement bottom boundary.

4.4. Numerical Predictions

In Railway engineering, the design is mainly based on limiting the traffic and load-induced deviator stress in the subgrade to levels that will protect the subgrade from progressive shear failure and excessive plastic deformation (Li and Selig, 1998a). In order to maintain the track profile, ballast displacement (vertical and lateral) should be controlled within certain limits. This section of the paper will demonstrate how the subgrade deviator stress and ballast displacement can be influenced by the use of rubber tyres as reinforcement, in contrast to the unreinforced case. The input parameters used for the Finite Element Method analysis are listed in Table 2; note that a set of three sleepers were considered sufficient for the analysis, and the deviator stress discussed was directly under the central sleeper.

Fig. 14(a) shows the effect that reinforcement offered by rubber tyres has on the deviator stress at the surface of the subgrade. As expected, the highest deviator stress occurs near the sleeper end and it decreases towards the central sleeper. This is consistent with the field observations where the largest subgrade depressions usually occur near the edges of the sleepers (Li and Selig, 1998a). With tyre-reinforcement, a train running with the same axle load (i.e. 25 ton) and speed (i.e. 100 km/h), experiences a maximum deviator stress of 46.2 kPa, which is almost a 12% reduction compared to that of an unreinforced section. Intuitively, the confining effect causes the tyres and gravel infill composite to act as a stiffer, flexible “mattress” which allows a reduced and more uniform stress to be transmitted to the subgrade. As shown in Fig. 14(a), the area that the traffic and load-induced subgrade stress was distributed to was wider than the area without tyre reinforcement.

Fig. 14(b) shows the effect that tyre reinforcement has on the distribution of deviator stress with the depth of subgrade. The deviator stress in the subgrade decreases with depth. Lateral deformation along the slope of the embankment also decreases considerably due to tyre reinforcement (Fig. 15). The contours of lateral displacement for the unreinforced and reinforced layers of subballast are also shown in Fig. 15, where the largest lateral movement of subballast developed beneath the edge of the sleeper in the reinforced subballast. These comparisons show that the maximum lateral displacement for unreinforced subballast (0.095 m) was considerably more than that of reinforced subballast (0.012 m) under the same load.

5. CONCLUSIONS

In this study, plate loading tests were carried out to investigate the load transfer mechanism between rubber tyre and infill material. The inclusion of rubber tyre and geotextile reinforcement

could help to reduce the stress transmitted to the subgrade, and increasing the thickness of the subballast could also reduce stress at the interface between the subballast and subgrade. In a practical sense, the inclusion of rubber tyres and geotextile reinforcement can effectively reduce the design thickness of ballast, while eliminating the need for having a capping layer composed of natural rock aggregates. The experimental results showed that the tyre reinforcement could provide more than 50% gain in stiffness of a subballast (capping) layer. Due to its cylindrical structure, rubber tyres can confine the infill material, minimise lateral displacement, and provide a rigid capping with a bearing capacity of up to 6500 kPa with substantial reduction in lateral strains. The measurements confirmed that the strain experienced by the rubber tyre was relatively small. An additional confining stress is generated by the hoop stress of the tyre, which can be as much as 500 kPa, at the maximum applied load of 6500 kPa.

A FEM study of plate loading test verified that the use of tyres could increase the elastic modulus of reinforced gravel by confinement. The maximum displacement and maximum tension inside the tyre were close to its bottom, and the highest interface shear stresses also developed near the bottom and close to the edge of the tyre. The load-deformation relationships for the reinforced and unreinforced cases agreed reasonably well in view of the experimental and FEM results.

The 3D Finite Element track model indicated that the highest deviator stress occurred near the edge of the sleeper, while the confining effect causes the tyre and gravel infill composite to act as a stiff but flexible “mattress” that can reduce the stress transmitted to the subgrade. This has significant implications on the stability of a soft subgrade that can prematurely yield unless the transmitted stress is reduced by a reinforced capping layer.

In this study, plate load tests were carried out on a single tyre filled with subballast to investigate the load-settlement behaviour of the gravels under static load. The data of these tests was also used to validate and calibrate the numerical model. Cyclic loads testing program is still in progress and is premature to discuss herein. The cyclic tests have been set up with all the rail track components (e.g. rail, sleeper, ballast, tyre confined capping layer & subgrade). Lateral deformation and settlement, time-dependent resilient modulus, damping and energy-based characteristics, particle degradation effects, as well as the axial and circumferential strains of the tyre cell upon cyclic loading will be presented and discussed in a future research paper.

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Fig. 1. Particle size distribution of subballast and subgrade used in the experiments

Fig. 2. Tensile strength results of the rubber tyre

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Fig. 3. Static load test setup: (a&b) schematic illustration of test box; (c) rubber tyre detail and (d) specimen assembled

Fig. 4. Results of plate load tests: (a) Test 1: 150 mm thick of subballast without reinforcement; (b) Test 2: 150 mm thick of subballast with tyre reinforcement; (c) Test 3: 350 mm thick of subballast without reinforcement; (d) Test 4: 350 mm thick of subballast with tyre and geotextile reinforcement; (e) Test 5: 350 mm thick of subballast with tyre reinforcement; and (f) Test 6:

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Fig. 5. Circumferential and axial strains of the tyre for the reinforced tests: (a) Test 2: 150 mm thick of subballast with tyre reinforcement; (b) Test 4: 350 mm thick of subballast with tyre and geotextile reinforcement; (c) Test 5: 350 mm thick of subballast with tyre reinforcement; and (d) Test 6: rubber tyre and subballast composite unit cell test

Fig. 6. Increment of additional confinement $\Delta\sigma_3$ and apparent cohesion c_r with stress

Fig. 7. (a) 3D ABAQUS mesh for the model with tyre reinforcement and (b) maximum lateral displacement predicted by FE model with different mesh dimension W

Fig. 8. (a) unreinforced vertical displacement at a vertical pressure of 1000 kPa; (b) reinforced vertical displacement at a vertical pressure of 1000 kPa; (c) unreinforced lateral displacement at a vertical pressure of 1000 kPa and (d) reinforced lateral displacement at a vertical pressure of 1000 kPa

(a)

(b)

Fig. 9. Displacement vectors of rubber tyre along x direction: (a) at a vertical pressure of 50 kPa and (b) at a vertical pressure of 1500 kPa

Fig. 10. Force distribution in rubber tyre at a vertical pressure of 1500 kPa

Fig. 11. Interface shear stress between tyre and subballast at a vertical pressure of 1500 kPa

Fig. 12. Track geometry with rubber tyres reinforced capping (subballast) layer

Fig. 13. FEM mesh of ballasted railway track and foundation reinforced with rubber tyres
in the subballast layer

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Fig. 14. (a) Subgrade stress distribution below reinforced and unreinforced track and (b) distribution of subgrade deviator stress with depth for reinforced and unreinforced track

Fig. 15. Lateral displacements for reinforced and unreinforced railway track with various train speed loadings

583 Table 1 Physical characteristics and technical specification of subballast, tyre and geocell used
584 for the study

Subballast (crushed basalt)	Properties	Values	Satandard
	$D_{\max}$ (mm)	19	--
	$D_{\min}$ (mm)	0.075	--
	C_u	16.3	--
	C_c	1.3	--
	γ_d (kN/m ³)	21	--
	Internal angle of friction, ϕ (degrees)	39	ASTM D4885-01(2011)
Subgrade (clayey sand)	$D_{\max}$ (mm)	4.75	--
	$D_{\min}$ (mm)	0.01	--
	C_u	2.4	--
	C_c	1.1	--
	γ_d (kN/m ³)	17	--
Tyre	Outside diameter (mm)	560	--
	Rim diameter (mm)	330	--
	Width (mm)	150	--
	Tensile stress at 2% strain (MPa)	6.1	ASTM D4885-01(2011)
	Tensile stress at 2% strain (MPa)	15.2	ASTM D4885-01(2011)
	Ultimate tensile strength (MPa)	19.45	ASTM D4885-01(2011)
Geotextile	Tensile strength (kN/m)	16.8	AS3706.2-12
	Tensile Elongation (%)	<24	AS3706.2-12
	Tensile Strength at 2% Strain (kN/m)	4	AS3706.2-12
	Tensile Strength at 5% Strain (kN/m)	8	AS3706.2-12
	G Rating	2800	Austrorads
	Flow rate at 100 mm head (l/m ² /s)	40	AS3706.9-12
	Permittivity (s ⁻¹)	0.4	AS3706.9-12

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587 Table 2 Track variable values used in the numerical analysis

Track variable	Value
Rail Properties	
Density (kg/m^3)	2000
Young's modulus E (MPa)	500000
Poisson's ratio, ν	0.3
Sleeper Properties	
Density (kg/m^3)	2000
Young's modulus E (MPa)	30000
Poisson's ratio, ν	0.25
Ballast Layer	
Density (kg/m^3)	1530
Young's modulus E (MPa)	2
Poisson's ratio, ν	0.3
Internal angle of friction, ϕ (degrees)	45
Angle of dilation, ψ (degrees)	15
Cohesion, c (kPa)	1
Thickness (m)	0.35
Subballast Layer	
Density (kg/m^3)	2100
Young's modulus E (MPa)	2
Poisson's ratio, ν	0.3
Internal angle of friction, ϕ (degrees)	39
Angle of dilation, ψ (degrees)	15
Cohesion, c (kPa)	1
Subgrade Layer	
Density (kg/m^3)	1700
Young's modulus E (MPa)	2
Poisson's ratio, ν	0.3
Internal angle of friction, ϕ (degrees)	40
Angle of dilation, ψ (degrees)	15
Cohesion, c (kPa)	5
Tyre Properties	
Density (kg/m^3)	1500
Young's modulus E (MPa)	750
Poisson's ratio, ν	0.35
Wheel Load	
Static wheel load (kN)	122.5
Train Speed (km/h)	100
Dynamic amplification factor (DAF)	1.54
Dynamic wheel load (kN)	188.2
Interface Elements	
Normal property	Hard
Tangential coefficient	0.45

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