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Mark F. O'Dwyer

University of Wollongong, markod@uow.edu.au

H. Linke

University of Oregon, USA

E. Hoffmann

University of Oregon, USA

T. E. Humphrey

University of Geneva, Switzerland

R. A. Lewis

University of Wollongong, roger@uow.edu.au

See next page for additional authors

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Authors

Mark F. O'Dwyer, H. Linke, E. Hoffmann, T. E. Humphrey, R. A. Lewis, and C. Zhang

Power generation with nanowire resonant tunneling thermoelectrics

M. F. O'Dwyer¹, H. Linke², E. Hoffmann², T. E. Humphrey³, R. A. Lewis¹ and C. Zhang¹

¹ *School of Engineering Physics and Institute for Superconducting and Electronic Materials
University of Wollongong, Wollongong NSW 2522, Australia*

² *Materials Science Institute and Physics Department, University of Oregon, Eugene, OR 97403-1274, U.S.A.*

³ *Département de Physique Théorique, University of Geneva, CH – 1211, Geneva, Switzerland*

Abstract

Nanowires have been predicted to yield significantly improved thermoelectric figures of merit. Here we describe the electron energy spectrum of a resonant tunneling heterostructure nanowire in detail and show how it may be used to realize energy filtering for thermoelectric electronic efficiencies approaching the Carnot limit. A proof-of-principle experiment is described that seeks to demonstrate such idealized electronic properties.

Introduction

Whereas low efficiencies limit the practical application of current thermoelectric devices to niche applications, a breakthrough in thermoelectric technology allowing higher efficiencies would have substantial economic impact. Recent theory predicts that the use of nanowires in thermoelectric devices could have significant advantages. Hicks and Dresselhaus predicted considerably higher thermoelectric figures of merit for Bi₂Te₃ based nanowires compared to superlattice or bulk devices primarily due to changes in the electronic density of states [1]. Of particular interest here is the prediction that low-dimensional conductors in which mobile electrons are restricted to a very narrow range can achieve electronic energy-conversion efficiencies approaching the Carnot limit [2,3].

Here, we discuss in detail the requirements for a nanowire thermoelectric device to realize efficiency approaching the Carnot limit and develop specific structural parameters for an InAs/InP nanowire heterostructure to achieve these. The device described is a wire with a single embedded quantum dot, through which electrons tunnel via a resonant transmission energy between hot and cold electron reservoirs. Such a device might be used in a proof-of-principle experiment demonstrating that electron energy filtering in 1D conductors can significantly increase the efficiency of thermoelectric energy conversion.

Nanowires overview

Lithographic methods have traditionally been used to make quantum devices, however, such methods have drawbacks [4]. Semiconductor whiskers were first grown and characterized in the 1960s with diameters in the order of a hundred nanometers or more [5]. Although different growth mechanisms exist, all have been described using the vapor-liquid-solid mechanism [5]. Here a metal cluster, such as Au, acts as a catalyst under which the whisker grows [6].

In the 1990s whiskers with diameters in the order of tens of nanometers were grown, providing quantum confinement for new devices [7]. Since then rapid progress has occurred both in nanowire growth and the development of nanowire devices. Nanowires have been grown in many different

materials including GaAs [7-11], InAs [6,7], InP [10], InAs [11,12], GaP [10], Si [13] and AlGaAs [11,14]. Techniques have been developed that allow the precise control of the size, shape and position of nanowires grown on the substrate with an accuracy of nanometers [9]. Furthermore, the nanowires may be grown with uniform diameters over the length of the wire, which is important for quantum confinement properties. Nanowire heterostructures are formed by switching the growth materials [15]. Various heterostructures have been grown including Si/SiGe [16], GaAs/GaP [17] and InP/InAs [15]. It has been demonstrated that devices with high quality dislocation-free material interfaces may be grown in InP/InAs systems [18]. This is achieved through a very slow growth process. The uniformity of nanowire diameter and defect free interfaces make the development of novel devices possible.

To fabricate devices, nanowires are removed from the growth substrate and placed on a SiO₂ capped Si wafer [6]. Lithography is then used to fabricate contacts to wires.

Modulation doping has been demonstrated allowing nanowire p-n junctions [19] and light-emitting diodes [20, 21], photo-detectors [21], transistors [22], inverters [22] and biological nano-sensors [23] to be demonstrated. Resonant tunneling diodes [24], single-electron transistors [25] and few-electron quantum dots [26] have been demonstrated using nanowire heterostructures.

Measurements on nanowire composites [27, 28], nanowire arrays [29] and individual nanowires [30] have been performed investigating their thermoelectric properties. No measurements of the thermoelectric properties of nanowire heterostructures have been conducted.

Background

The figure of merit in bulk thermoelectrics has been relatively stagnant over the last forty years with $ZT \sim 1$ and efficiencies in commercial devices of about 10% of the Carnot limit [31]. Hicks and Dresselhaus proposed that the reduced dimensionality of nanowires could be utilized to enhance the electronic density of states in energy ranges advantageous to thermoelectric power generation [1]. They predicted $ZT \approx 6$ for Bi₂Te₃ nanowires compared to 2.5 and 0.5 for superlattice and bulk systems respectively.

Thermal-to-electric energy conversion with efficiency near the Carnot limit would require negligible lattice heat conduction and reversible electron transport between the hot and cold reservoirs, that is, current flow without entropy production. We recently showed [3] that the latter conditions can indeed be achieved in principle if the only electrons that can travel between the reservoirs are those that have a specific energy given by

$$E_0 = \frac{\mu_C T_H - \mu_H T_C}{T_H - T_C} \quad (1)$$

where $T_{H/C}$ and $\mu_{H/C}$ are the hot/cold reservoir temperatures and chemical potentials respectively. Electrons at this energy are said to be in ‘energy-specific equilibrium’ [3] because they can move reversibly between the two reservoirs. If electrons are transmitted at an energy infinitesimally close to E_0 , the efficiency of energy conversion will approach the Carnot value.

We propose a resonant tunneling double barrier heterostructure nanowire device, as shown in Figs. 1 and 2, which filters electrons such that only those within a narrow range around E_0 are transmitted. The potential of the system may be varied in two ways, either by applying a source-drain bias or a gate voltage which varies the global potential of the device. Specific structural parameters will be proposed for an InP/InAs system. Due to a large lattice mismatch, bulk InP/InAs heterostructures may not be grown. It is possible to grow nanowire heterostructures using the two materials because of strain relaxation due to the small size of the crystal [6].

The InAs/InP conduction band offset has been estimated through thermionic emission experiments to be around 0.57 eV [18]. This value is used in calculations. The effective masses used are $0.08m_e$ and $0.023m_e$ for InP and InAs respectively [32]. Calculations are performed using a Landauer equation based method detailed elsewhere [33].

Figure 1: An illustration of quantum dot embedded resonant tunneling nanowire heterostructure on a SiO₂ insulated Si wafer with contacts.

Practical requirements for near-Carnot efficiency

There are a number of requirements our system must meet in order to achieve an efficiency approaching the Carnot value.

First, the filtering of electron energies for transmission must occur according to their *total* energy. This is not possible in conventional 3D superlattices which filter electrons according to their energy in the direction of transport only, allowing energies in the transverse spatial dimensions to take on random values [34]. In a nanowire, electron energies are quantized in the transverse dimensions.

Figure 2: Band diagram showing the double barrier structure and key system parameters used in the model. $\mu_{H/C}$ are the chemical potentials of the hot/cold reservoirs, $T_{H/C}$ are the temperatures of the hot/cold reservoirs, E_{res} is the resonant transmission energy and has energy width δE_{res} , ΔE is the energy gap between the first and second resonance (if any), ϕ is the conduction band offset, V_{bias} is the bias voltage on the system applied between the source and drain, and b_S , b_D and w are the source barrier, drain barrier and well widths, respectively.

Second, the double barrier needs to be designed such that the longitudinal electron energies are restricted to a narrow range. Efficiency is predicted to be higher for smaller δE_{res} [35], which can be tuned by adjusting the barrier widths.

Third, one of the net resultant energy levels in the device must dominate electronic transport. Should the energy levels be sufficiently spaced relative to the thermal energy, $k_B T$ (~ 1 meV at 10 K), transport in the nanowire attached to the double barrier will be restricted to a single level.

Fourth, heat leaked by the lattice must be very low if high efficiency is to be achieved. This is particularly important when δE_{res} is small because then the electron current and the power of the device will be very low.

Fifth, the overall width of the double barrier structure should be less than the electron mean free path so that electrons are not scattered, but travel ballistically between the reservoirs.

As shall be demonstrated, a resonant tunneling quantum dot embedded nanowire system is capable of meeting these requirements.

Energy levels in nanowires

We will now analyze in detail the energy levels in a resonant tunneling nanowire heterostructure and discuss how the device must be structured in order to meet the stated requirements for near-Carnot efficiency. In a resonant tunneling nanowire device, there is an interplay between three effects that will determine the net energy level spacing. These are: (a) the transverse quantization due to the width of the

nanowire, (b) the longitudinal quantization due to the levels in the potential well/quantum dot and (c) the charging energy caused by the capacitance of the quantum dot.

Transverse energy levels

The cross-sectional shape and diameter of the nanowire determine the transverse quantization energies in the y and z directions. InAs/InP nanowires have either a hexagonal or square cross section when grown in the $\langle 111 \rangle$ and $\langle 001 \rangle$ directions respectively [26]. Since the potential barrier due to the vacuum and SiO_2 is high, it is accurate to consider the nanowire bounded by an infinite potential. The energy levels for hexagonal nanowires may be obtained through a numerical solution of the Schrödinger equation. Energy level solutions in the y and z directions for the square cross section are given by the standard infinite square well model; $E_{y/z} = \pi^2 \hbar^2 n_{y/z}^2 / 2m^* a_{y/z}^2$. The high vacuum/ SiO_2 potential also means that we may accurately assume that the transverse energy levels are infinitely sharp. Fig. 3(a) shows the energy levels in one transverse dimension, for a square cross section nanowire of width 55 nm. Two electrons may occupy each of these levels due to spin degeneracy. The *total transverse* energy is given by $E_y + E_z$, giving the energy level structure shown in Fig. 3(b). Four electrons are allowed to occupy some levels due to spin degeneracy combined with the symmetry of the square potential. The low effective mass of InAs gives large spacing between the energy levels. The transverse energy levels are closer for thinner nanowires. Although the details vary, the energy level structure is generally similar in form for nanowires with different cross-sectional profiles.

Longitudinal energy levels

Longitudinal energies, in the direction of the wire, x , are quantized due to the double barrier resonant tunneling structure. Transmission through the double barrier is allowed at certain longitudinal energies corresponding to the bound states of the quantum dot. Electrons with energies above the barrier height will generally be transmitted unobstructed through the dot. The contribution of such electrons to the current should be negligible, however, due to the low occupation of states at such high energies, particularly at low temperatures.

The energy levels of the dot may be determined by numerically solving the Schrödinger equation for the finite width/finite potential barrier system. Fig. 4 shows the longitudinal energy levels calculated for devices with dot widths of 7 nm and 100 nm. The narrower the dot is, the larger the spacing between longitudinal energy levels.

Net quantum energy levels

The net quantum energy levels in the dot are the results of the transverse confinement in the y and z directions by the width of the nanowire and the longitudinal confinement in the x direction due to the width of the dot. Electrons will therefore be selected according to their *total* energy as required. The energy spread of electrons transmitted at any level may be restricted by increasing the width of the barriers

Figure 3: (a) The energy levels in one transverse dimension for a square cross section nanowire of width 55 nm. (b) The resultant total transverse energy levels for the same nanowire when those in the y and z direction are combined. Circles indicate where two levels have the same energy.

Figure 4: The longitudinal energy levels for a quantum dot of width (a) 7 nm and (b) 100 nm with barrier widths of 7 nm.

defining the dot [33]. For each longitudinal energy (shown in Fig. 4) electrons may occupy any of the transverse energy levels (shown in Fig. 3). This gives the net quantum energy level structure shown in Fig. 5.

Capacitance and charging energy

Measurements on quantum-dot embedded nanowires show small capacitance and Coulomb blockade effects [6, 24-26]. This means that the spacing of the electron energy levels is increased by $\Delta E_C = e^2 / C$ where C is the system capacitance [36]. The origin of this additional energy gap is the electrostatic repulsion an electron in the nanowire reservoir feels due to the presence of an electron on the dot. Energy levels that previously allowed two or four electrons will therefore be split into distinct levels separated by ΔE_C . Odd energy level gaps will always be equal to ΔE_C . Every second or fourth energy gap will be given by $\Delta E_C + \Delta E_N$ where ΔE_N is the quantum spacing between the N th and $(N-1)$ th energy levels.

Figure 5: The net quantum energy levels for systems with nanowire width of 55 nm, barrier widths of 10 nm and dot width of (a) 7 nm and (b) 100 nm. Circles indicate two levels with the same energy.

Typically reported experimental values for ΔE_C range from 4 meV to 6 meV depending on system dimensions [26]. The total system capacitance, C , is given by the sum of the source, drain and gate capacitances. For any quantum dot embedded nanowire device, the charging energy and system capacitances may be determined in a relatively straight forward manner from its stability diagram. A stability diagram is a two dimensional plot of differential conductance, dI/dV , versus source drain voltage and gate voltage. The charging energies and capacitances are determined from the dimensions of the diamonds [26]. It has been shown that the plate capacitor formula, $C_p = \epsilon_r \epsilon_0 A/t$, gives a reasonable estimate of the capacitances [25] and that the gate capacitance scales with dot width as this equation predicts [26]. To estimate the capacitance of nanowires with different configurations we will therefore scale the reported experimental values [25,26] according to the plate capacitor formula

$$C = 1aF \frac{w}{10nm} \frac{d}{55nm} + 13aF \frac{d^2}{(55nm)^2} 5nm \left(\frac{1}{b_s} + \frac{1}{b_d} \right) \quad (2)$$

where d is the diameter of the nanowire. Fig. 6 shows the final energy level spacing for the resonant tunneling nanowire device, with charging energies included. The spacing is much more regular than that of the net quantum levels. The charging energy for the smaller 7 nm dot is larger due to its lower capacitance. The smallest energy gap between transmission energies in such a Coulomb blockaded system will always be ΔE_C .

Device structure for an energy-selective thermoelectric

It is now possible to discuss how the nanowire device should be structured in order to achieve an electron energy spectrum that meets the requirements described for near-Carnot efficiency. There are two ways the required energy

Figure 6: The net energy levels with charging effects for a device with dot width (a) 7 nm and (b) 100 nm.

filtering could be achieved. The first is to have a very low charging energy, $\Delta E_C \ll k_B T$. In this limit, we would effectively have no splitting of the net quantum energy levels relative to the thermal energy. In this case, the quantum energy gap between the levels would need to be at least a few $k_B T$ to ensure a single transmission energy dominated transport. Realizing this limit requires very high capacitance, $C > 6000$ aF at 10 K. Based on Eq. 2, the capacitance can be increased by decreasing the barrier widths, increasing the dot width and increasing the wire diameter, none of which is desirable. Decreasing the barrier width increases the width of the electron energy spectrum reducing electronic efficiency. Increasing the dot width and wire diameter decrease the energy gap between the quantum energy levels that we require to be large in this instance.

The second way to achieve the required energy filtering is to utilize the charging energy to provide the energy level spacing. In this case, we require $\Delta E_C \gg k_B T$ and a small capacitance, the opposite to the previous case. Since $k_B T \sim 1$ meV at 10 K, $\Delta E_C > 5$ meV is desirable. This is equivalent to a system capacitance of less than 30 aF. This may be easily achieved with the InAs/InP nanowires discussed and the suitability of different configurations estimated using Eq. 2. In fact, this means that any nanowire with a strong Coulomb blockade effect might make a suitable candidate for the energy filtering of interest here.

Barriers of width 7 nm or larger should provide a sufficiently narrow electron energy spectrum. Since the system potential may be varied via the gate voltage, the magnitude of the energy level utilized is not critical and a dot of any width may be used so long as the charging energy is sufficient. It might be desirable in a particular experiment to use a narrow dot with strong quantum confinement, or conversely, a wide dot so that the energy level used is close to the Fermi level in the nanowire reservoirs. In any case, the gate voltage should be tuned such that suitable current is achieved through the desired energy level.

Proof-of-principle experiment

Performing a proof-of-principle experiment to measure thermoelectric effects in energy filtering nanowires at low temperature ($T < 10$ K) has a number of advantages. At low temperatures a lower charging energy is required and less efficiency reducing ‘thermal smearing’ of the electron energy spectrum occurs. Electron-phonon coupling is also very weak below 10 K [37]. In this case one can assume electron-electron interactions establish a quasi-equilibrium electron temperature that is independent of the phonon temperature. One electron reservoir can be heated using a heat current without phonon-mediated heat flow to the cold electron reservoir. Thus, high electronic efficiencies should be possible.

Determining the efficiency of the nanowire device requires measurements of the heat flow through the device, which could be difficult. It has been shown that with ideal electron energy filtering, the Seebeck coefficient approaches a theoretical maximum value given by $S_0 = (E_{res} - \mu_H)/eT_H$. The Seebeck coefficient of the nanowire device may be determined more easily than efficiency, by simply measuring the temperature and electrical properties of the system. How close the measured Seebeck coefficient is to the S_0 will provide an indication as to whether or not the device is filtering the electron energy spectrum as desired. Fig. 7 shows that calculated electronic efficiency approaches the Carnot value and that as the width of the spectrum is decreased through widening the barriers, the Seebeck coefficient approaches S_0 .

Figure 7: The electronic efficiency relative to the Carnot value of the nanowire thermoelectric device with 7 nm dot versus μ_C (with bias voltage tuned for maximum efficiency). Inset: the Seebeck coefficient, S , as a function of μ_C for different barrier widths as labeled. The maximum possible Seebeck coefficient, which is associated with reversibility, S_0 , is also included.

Although phonon heat backflow would dominate, an experiment demonstrating idealized electron transport at room temperatures could also be performed. This would require

very low capacitance, in the order of 1 aF, to provide the required separation between levels. Using a barrier width of 10 nm (barrier widths beyond this will result in very small currents) and evaluating Eq. 2 suggests that nanowires with diameters less than 15 nm would be required. In such a device, one would expect to observe Seebeck coefficients approaching S_0 at room temperature.

When performing an experiment, one should be aware that there will be a Seebeck coefficient associated with the contact between the three dimensional leads and the one dimensional wire. There will also be a resistance associated with this. Device currents will be very small, requiring precise calibration and measurement techniques.

Conclusions

We have discussed the requirements for a nanowire thermoelectric device to filter the electron energy spectrum such that high efficiencies approaching the Carnot value might be realized. An InP/InAs resonant tunneling heterostructure nanowire is capable of realizing these. A detailed analysis of the energy level structure in nanowires reveals that the device should be designed with capacitance lower than ~ 30 aF so that Coulomb blockade effects provide the required electron energy filtering. Finally, a proof-of-principle experiment was described, which it is hoped will measure a Seebeck coefficient revealing near-ideal electron energy filtering.

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