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Quasi-one-dimensional intermittent flux behavior in superconducting films

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Quasi-one-dimensional intermittent flux behavior in superconducting films

Abstract
Intermittent filamentary dynamics of the vortex matter in superconductors is found in films of \( \text{YBa}_2\text{Cu}_3\text{O}_{7-\delta} \) deposited on tilted substrates. Deposition of this material on such substrates creates parallel channels of easy flux penetration when a magnetic field is applied perpendicular to the film. As the applied field is gradually increased, magneto-optical imaging reveals that flux penetrates via numerous quasi-one-dimensional jumps. The distribution of flux avalanche sizes follows a power law, and data collapse is obtained by finite-size scaling, with the depth of the flux front used as crossover length. The intermittent behavior shows no threshold value in the applied field, in contrast to conventional flux jumping. The results strongly suggest that the quasi-one-dimensional flux jumps are of a different nature than the thermomagnetic dendritic (branching) avalanches that are commonly found in superconducting films.

Keywords
quasi, behavior, flux, intermittent, dimensional, films, one, superconducting

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Quasi-One-Dimensional Intermittent Flux Behavior in Superconducting Films

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Intermittent filamentary dynamics of the vortex matter in superconductors is found in films of YBa2Cu3O7–δ deposited on tilted substrates. Deposition of this material on such substrates creates parallel channels of easy flux penetration when a magnetic field is applied perpendicular to the film. As the applied field is gradually increased, magneto-optical imaging reveals that flux penetrates via numerous quasi-one-dimensional jumps. The distribution of flux avalanche sizes follows a power law, and data collapse is obtained by finite-size scaling, with the depth of the flux front used as crossover length. The intermittent behavior shows no threshold value in the applied field, in contrast to conventional flux jumping. The results strongly suggest that the quasi-one-dimensional flux jumps are of a different nature than the thermomagnetic dendritic (branching) avalanches that are commonly found in superconducting films.

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Since the prediction of a regular vortex lattice in type-II superconductors [1], a wide variety of vortex systems has been thoroughly investigated [2,3]. The pronounced dependencies of the range and strength of the vortex-vortex interaction on temperature and magnetic field make the vortex matter a unique, tunable model system for probing the statistical properties of interacting systems. The behavior of the vortex matter is to a large extent also determined by its interaction with quenched disorder in the material, i.e., with microscopic defects that pin the vortices and therefore serve as pinning centers in the superconductor. The interplay between the pinning forces and the driving Lorentz force leads to formation of a metastable critical state [4], where the current density has a critical magnitude, \( j_c \), which corresponds to the maximal nondissipative current density.

In films of YBa2Cu3O7–δ (YBCO) grown epitaxially, i.e., with proper matching of crystal lattice parameters, on a substrate slightly tilted from a major crystal plane (vicinal films), self-organized arrays of planar defects (antiphase boundaries) are formed with a typical period of 2–5 nm [5]. The terrace structure of the surface is characterized by steps that are a few Ångströms in height, and the steps provide well-oriented seeding sites for growth along the main axis (c axis) of the overlying YBCO film. Films grown on substrates with a tilt angle of \( \theta \) close to 10° have better grain alignment and improved current-carrying ability [5,6]. There has been considerable interest in such films due to their potential application in Josephson-junction design [7–9], in particular for highly sensitive detectors of electromagnetic radiation.

The growth of YBCO films on tilted substrates is also known to produce planar defects, which become channels for easy vortex motion [5,6,10]. These channels are separated by 5–10 \( \mu \)m and run parallel to the terrace structure, causing considerable anisotropy in both the flux penetration and the effective critical current. At low temperatures, where the anisotropy is most pronounced, the vortices are essentially confined inside the channels, and the flux penetration has a strong quasi-one-dimensional (quasi-1D) character. In this paper, we show, using magneto-optical imaging (MOI), that the quasi-1D flux dynamics is highly intermittent at low temperatures in samples with moderate tilt angles.

Intermittent flux motion is very harmful for electronic devices, so the source of intermittency should be identified and the behavior characterized. Until now, intermittent flux behavior in superconducting films has been observed in Nb, Pb, Nb3Sn, NbN, MgB2, and YNi2B2C [11–16], where, during slow ramping of the applied field, the flux avalanches take the form of large dendritic (branching) structures. These avalanches are believed to be caused by a thermomagnetic instability [17–20]. We find that, in YBCO on tilted substrates, the flux jumps are largely

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different from the thermomagnetic avalanches both in morphology and in size distribution, suggesting that the origin of the intermittency is of a different nature.

Superconducting films are prepared by laser ablation (vaporization by a laser beam and subsequent crystallization) of YBa$_2$Cu$_3$O$_{7-δ}$ ceramic targets on NdGaO$_3$ substrates with tilt angles $\theta$ of up to 33°. (See Ref. [9] for sample preparation details.) The films we investigate in the present work have thickness of $d = 200$ nm and a critical temperature of $T_c = 88$ K. They are shaped by optical lithography into long strips of width $2w = 0.9$ mm. Low-temperature MOI is performed using an in-plane magnetized ferrite-garnet film as the Faraday rotating sensor [21,22]. The measurement configuration is illustrated in Fig. 1.

Figure 2(a) shows a magneto-optical image of the flux penetration in a $\theta = 14^\circ$ film where the surface steps are aligned vertically in the picture. The sample is initially cooled to $T = 4$ K at zero field, and then a perpendicular applied magnetic field is slowly increased at a rate of 0.2 mT/s. The image is recorded at $B_a = 16.2$ mT. The flux penetrates the sample from the two long edges, seen in the figure as bright horizontal lines, in a distinctly filamentary manner, where the filaments are aligned with the underlying terrace steps. From the short edge, however, the flux penetration is essentially blocked by the strong pinning associated with vortex motion transverse to the terrace structure. The full flux dynamics during such a field ramp is seen in Video 1.

From the real-time observation, it is evident that the penetration is strongly intermittent, where the flux enters from both long edges via discrete quasi-1D avalanches. This penetration is also documented in panel (b) of Fig. 2.

FIG. 1. Mounting in the cryogenic MOI setup of the YBCO film on a NdGaO substrate with a terrace-structured surface. Also shown is the orientation of the crystallographic axes specified by Miller indices, as well as the tilt angle $\theta$. On top of the superconductor is the Faraday rotating ferrite-garnet film (FGF), grown on a gadolinium-gallium-garnet (GGG) substrate, which allows realtime visualization of the flux density across the film area.

FIG. 2. (a) Direct and (b) differential magneto-optical images of flux penetration in a YBCO film on a $\theta = 14^\circ$-tilted substrate. The applied magnetic field is $B_a = 16.2$ mT, and the sample temperature is $T = 4$ K. The image brightness represents the distribution of flux density. In (b), the linear streaks show the avalanches taking place during $\Delta B_a = 42.5$ μT. The white scale bars at the bottom of each panel are 200 μm long.

VIDEO 1. The intermittent flux penetration in the YBCO film shown in Figure 2. Needlelike flux avalanches are seen as abrupt events as the magnetic field $B_a$ is increased from zero to 17 mT in steps of $\Delta B_a = 42.5$ μT. The sample temperature is $T = 8$ K.
which shows the result of subtracting two subsequently recorded images. The bright streaks show the abrupt arrival of the flux entering either (i) from the edge where new vortices nucleate, or (ii) from an internal vortex rearrangement [23]. The red ovals in the figure mark examples of internal avalanches, whereas the dark streaks are the regions from which the flux escaped. All this dynamics takes place within a field interval of only $\Delta B_a = 42.5 \mu T$. A differential movie of the flux dynamics is included as Video 2. Analyzing the sequence of avalanches from such movies, we find no correlation between flux jumps in adjacent channels. Thus, the overall flux-penetration process can be considered as a sequence of independent avalanche events.

More insight into the phenomenon is obtained by determining whether the avalanches are reproducible or not. The well-known dendritic flux avalanches caused by thermomagnetic instability have the characteristics of being irreproducible [15,24,25]. When a field sweep is repeated under the same experimental conditions, the flux patterns show essentially no overlap, suggesting that stochastic fluctuations play a main role. The present quasi-1D avalanches also display irreproducible behavior, although on a smaller scale. Figure 3 shows a superposition of three monochrome color-coded (red, green, and blue) differential images taken at the same applied field and temperature during three different consecutive experimental runs. In an image made in this way, repeatable features appear as a gradation of gray for repeatable features, whereas events that occur in only one run appear as red, green, or blue. The superposition is black in areas where no flux change occurs in any of the images. Evidently, there is no overlap in the three sets of flux avalanches [26]. The same irreproducibility has been found at all fields investigated.

All the quasi-1D avalanches are limited in length by the overall flux-penetration front as it advances toward the middle of the strip in response to the increasing applied magnetic field. The front is built up as an envelope of numerous flux needles formed by the avalanches penetrating the most deeply into the film. This result is strikingly different from the dendritic type of avalanches, where the size of the jumps can span the sample even with a small applied field, and the flux front in general attains a very complex shape. In our case, the flux front is far more well behaved.

To quantify the new type of intermittent flux dynamics, we record magneto-optical images while the applied field

![FIG. 3. Superposition of three magneto-optical differential images of flux penetration in a YBCO film on a $\theta = 14^\circ$-tilted substrate. The different monochrome image series are color coded in red, green, and blue, respectively. The presence of colored superpositions shows that the flux jumps are not reproducible. The sample temperature is $T = 4 \text{ K}$, the applied magnetic field is $B_a = 16.7 \text{ mT}$, and the field step is $\Delta B_a = 42.5 \mu \text{T}$. The scale is the same as for Fig. 2(a).](image)

![FIG. 4. Dependence of the maximum avalanche length, $\ell_{\text{max}}$, on the applied field (red dots). The solid blue curve shows the Bean-model flux penetration depth, $L$, given by Eq. (1).](image)

![VIDEO 2. The differential video obtained by subtracting subsequent frames in Video 1.](image)
is slowly ramped from zero to $B_a = 17$ mT. The sample becomes nearly fully penetrated by flux. Images are recorded every 42.5 μT. From all these images, a sequence of difference images is prepared, and, for every avalanche that occurs, its length $\ell$ is measured by using a pattern-recognition program. Figure 4 shows how $\ell_{\text{max}}$, the size of the longest avalanche within each field interval, varies with the applied field. The maximum length follows a smooth curve, which corresponds very well to the advancement of the overall flux front, i.e., at all fields, there are avalanches starting at the edges and ending at the flux front. Actually, the $\ell_{\text{max}}(B_a)$ behaves in full accord with the flux-penetration depth for a long thin superconducting strip in the critical state. For a strip in the Bean critical state, the flux front reaches a depth of $L$ given by [27]

$$L/w = 1 - \cosh^{-1}(B_a/B_d),$$

(1)

where $B_d = \mu_0 j_c d/\pi$. In Fig. 4, $L(B_a)$ is plotted to fit the experimental data using a critical current density of $j_c = 0.78 \times 10^{11} \text{ Am}^{-2}$ as the only fitting parameter. Based on the good agreement, we conclude that the overall flux front evolves with the applied field according to the conventional critical-state behavior, whereas the detailed dynamics is governed by quasi-1D flux avalanches of length up to the depth of the flux front.

Figure 5 shows the size distribution of all the detected avalanches of more than 10,000, as a normalized probability for the occurrence of an avalanche of length $\ell$. The data are grouped into equal field intervals of 1.7 mT. From the log-log plot, it is evident that the vast majority of the avalanches are distributed as a power law $P(\ell) \sim \ell^{-\tau}$. The avalanche distribution has a natural cutoff length at the overall flux-penetration depth $L(B_a)$. A fit to the linear part of the data gives $\tau = 1.3$ for the exponent. Applying finite-size scaling according to the relation

$$P(\ell, L) \propto \ell^{-\tau} f\left(\frac{\ell}{L}\right),$$

(2)

where $f$ is a scaling function, the plot in Fig. 6 shows that a good data collapse is obtained with $D = 1$.

To summarize the experimental results, we have found that, at small fields, the avalanches are also small, and, as the applied field becomes larger, the maximum avalanche size gradually increases. The envelope curve of the flux-penetration front is slightly ramified (split into branches) by the avalanche activity, but it still behaves essentially in full accord with the critical-state model. Analyzing avalanches that occur within a small field interval as the applied field increases, we find that the distribution of

![FIG. 5. Statistics of avalanche length, $\ell$, observed while the applied field is ramped from zero to $B_a = 17$ mT in steps of $\Delta B_a = 42.5$ μT. The curves correspond to the field intervals listed in the key (mT). The straight line with a slope of $-1.3$ is added as a guide to the eye.](image)

![FIG. 6. Collapse of the data in Fig. 5, showing finite-size scaling. The graphs correspond to the field intervals listed in the key (mT).](image)

![FIG. 7. Superposition of three magneto-optical images (red, green, and blue) taken at the same applied field, $B_a = 22$ mT at $T = 9.2$ K in three different experimental runs. The presence of colors shows that the dendritic avalanches are irreproducible. The sample is a $5 \times 5 \text{ mm}^2$, 300-nm-thick film of MgB$_2$ on Al$_2$O$_3$ (1102) substrate.](image)
Moreover, in contrast to the dendritic histograms of the avalanche sizes show a strongly peaked shapes, deep into the Meissner-state part of the film, and have substantial positional disorder and hence add a vortices, which sit at strong-pinning sites, certainly will pinning areas, thus forming a fence on both sides. These nells, some vortices will also penetrate into the strong-pinning surrounded by areas of strong pinning, thus providing quasi-1D confinement. As flux enters these chan-
tions of channeling, which is clearly seen in the current MOI experiments. The film has a large number of linear defects which form parallel narrow channels with low pinning surrounded by areas of strong pinning, thus providing quasi-1D confinement. As flux enters these channels, some vortices will also penetrate into the strong-pinning areas, thus forming a fence on both sides. These vortices, which sit at strong-pinning sites, certainly will have substantial positional disorder and hence add a considerable random component to the confinement. Thus, the channels will contain a sequence of random bottlenecks for the traffic of vortices. As the applied magnetic field increases, more and more vortices penetrate into the channels, and situations analogous to a traffic jam, or clogging, will occur. Whenever one of these blocked regions eventually breaks open, an avalanche of vortex motion takes place along the channel. Since these barriers can be arbitrarily small, there is no threshold applied field for the onset of this intermittent behavior. This picture is consistent with our experimental observations. Moreover, this mechanism allows avalanches to start not only from the sample edge, but also from inside the channels, which is also in accordance with our observations. Interestingly, this scenario resembles the flux motion found in artificially created mesoscopic flow channels. (See Ref. [29] and references therein.)

It is also worth discussing our results within the framework of self-organized criticality (SOC). Although the first dynamical system shown to display SOC, the Bak-Tang-Wiesenfeld sand pile [30], does not exhibit SOC in one dimension, several similar algorithms with different toppling rules and intrinsic randomness do [31–33]. These models were invented to study numerically a mechanical quasi-1D dynamical system, the Oslo rice pile [34], which for certain types of rice grains displays SOC behavior. The numerical simulations give power-law avalanche-size distributions with exponents in the range of 1.3–1.6, depending on the details of the model. Our measured avalanche exponent falls within this range.

In the SOC literature, various definitions are used for the size of an avalanche: the number of sites being toppled, the amount of dissipated energy, the spatial extent of an avalanche, etc. In the present work, we have also performed an alternative statistical analysis where the avalanche size is taken to be the amount of the flux being abruptly displaced in each event, rather than the length of the filamentary jumps. This alternative analysis also leads to good scaling and a power-law exponent that agrees within 0.1 of that reported in this paper. Aegerter et al. [35] have also reported power-law statistics of flux avalanches in YBCO thin films deposited on plain substrates. Using MOI, they find the exponent \( \tau \) close to ours. However, their observed avalanches are far from being one dimensional, having \( D = 1.89 \). Closer-to-one-dimensional motion has been observed in small bundles of vortices in superconductor films of tungsten by use of scanning microscopy [36]. However, the data were accumulated over periods of many minutes, showing very different time characteristics compared to our observations. Note that, in contrast to the previous flux-imaging experiments [35,36], the present MOI observations cover the avalanche activity of the entire flux pile, enabling us to perform finite-size scaling with the physical size of the pile \( L \), instead of analyzing a small viewing window.

Worth noting in Fig. 6 is the slight overshoot in the curves near the cutoff length, \( L \). Also, simulations

VIDEO 3. For comparison, a typical set of flux avalanches in a MgB\(_2\) film. Notice the different morphology between these avalanches spanning the sample in complex dendritic patterns, and those seen in Video 1.
[31–33] show this feature, i.e., a small increase in the probability of having avalanches of maximum size, which is interpreted as a finite-size effect [31]. To our knowledge, this effect has not been observed experimentally before in vortex systems.

Since inertia can destroy SOC in mechanical systems [37], superconducting vortices, commonly considered as massless, indeed represent a very favorable candidate for SOC behavior with scaling and power-law distributions, reported on the topic [38–41]. In particular, the simulations [37], superconducting vortices, commonly considered as massless, indeed represent a very favorable candidate for SOC behavior with scaling and power-law distributions, including an overshoot similar to that in our data.

We also perform similar experiments on YBCO films using two other ramp rates: 0.12 mT/s and 0.02 mT/s. No significant qualitative or quantitative changes in the behavior are observed. Moreover, intermittent flux dynamics has also been observed in vicinal samples with tilt angles of $\theta = 8^\circ$, $10^\circ$, and $12^\circ$. However, in films with $\theta = 3^\circ$, $20^\circ$, $26^\circ$, and $33^\circ$, we find, not abrupt flux motion, but rather a smooth penetration into the channels. A reference sample with zero-degree tilt angle has shown neither flux jumps nor channeling. More work is required to clarify the relationship between the sample morphology and flux dynamics in superconductor films grown on vicinal-cut substrates.

In conclusion, we find that a gradual injection of the magnetic flux into a system of well-defined channels may trigger quasi-1D vortex avalanches, the sizes of which are distributed by a power law with the avalanche exponent $\tau = 1.3$. Introducing the depth of the flux front as a dynamic length scale makes the distributions invariant.

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For comparison, similar experiments were carried out on a quasi-one-dimensional intermittent flux with in-plane magnetization, Phys. Rev. Lett. 94, 037002 (2005).


For comparison, similar experiments were carried out on a sample with $\theta = 0^\circ$. Here, the flux dynamics always developed quite smoothly, and difference images similar to that in panel 2(b) showed just featureless noise from the CCD camera.


Notice the very faint colors along the edge, which are caused by the flux jumps perturbing the external field near the edge and are a result of the nonlocal electrodynamics of thin-film superconductors [19,27].


