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Abstract
For image database applications it is desirable that functions such as searching, browsing and partial recall be done without the need to totally decompress the image. This has the advantage of alleviating possible burden and degradation that the network may suffer. Edge images derived from wavelet-compressed images are considered as index that can be queried by example. Zernike moment invariants are used as descriptors for the index edge image and the query sketch image. The descriptions are compared for the purpose of database searching. The query images were allowed to undergo translation, rotation, scaling and some deformation. Simulation results gave 90% recognition rate.

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SIMILARITY MEASURES FOR COMPRESSED IMAGE DATABASES

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ABSTRACT

For image database applications it is desirable that functions such as searching, browsing and partial recall be done without the need to totally decompress the image. This has the advantage of alleviating possible burden and degradation that the network may suffer. Edge images derived from wavelet-compressed images are considered as index that can be queried by example. Zernike moment invariants are used as descriptors for the index edge image and the query sketch image. The descriptions are compared for the purpose of database searching. The query images were allowed to undergo translation, rotation, scaling and some deformation. Simulation results gave 90% recognition rate.

1. INTRODUCTION

The popularity of the Internet and the vast amount of available multimedia data is bound to pose some problems for multimedia resource discovery. These problems will be exacerbated by the fact that a lot of users will access the network via a low bit-rate communication link for some time to come. Image is one of the resources that have a huge storage requirement in a multimedia database application; browsing a full resolution image over the network may degrade the total network response time. The search time of image databases depends largely on the file format used in the storage and the search methods employed. Generally, the storage mechanism employed should support image database functionalities such as partial image recall and incremental image recall [1] in addition to efficient compression. It is desirable that the image compression method used allows the aforementioned functionalities without a need for full image reconstruction; such a method is described in [2].

The method described in [2] encodes an image using the wavelet transform and uses an edge image derived from the detail sub-bands of the image decomposition as the index. With this approach there is no need for a separate index which might occupy a large storage space. Furthermore, this method allows the user to interact with the database using a "query by visual example" [3]. One would expect that this method of query along with other techniques based on salient features of the images would be used in a practical system.

Similarity measure is a key factor in any database application. This is more so for image databases where the content bears varying degree of importance to the multitude of users that may want to use the images. Furthermore, some users may pose a query to the database without necessarily having a full knowledge of the composition of the image of interest. Thus, similarity rather than an exact match is a more suitable search criterion for image databases. The unstructured nature of image data also makes conventional database search methods inappropriate. Indeed the search should be human intuitive and allow for the inexact way in which humans pose queries.

In a given scenario, a user query may lack entire knowledge of the target image and the search engine needs to cope with a low resolution query with possibly some scale change, rotation, translation, and some degree of deformity. To search an image effectively, the search engine should be robust and capable of a partial similarity measure. This paper proposes a similarity measure based on moment invariants and defined over features of the edge image derived from [2]. The proposed method is invariant to scale, rotation, and translation.

Section 2 of the paper describes image feature based on moment invariant and Section 3 briefly reviews similarity measure paradigms. Section 4 presents the simulation results and discussion. Concluding remarks are given in Section 5.

2. IMAGE FEATURES

Features extracted from an image (or object) uniquely identify the image (or object) in a specific dimension. For instance, colour histogram is an image descriptor in colour space and spatial relationship of objects in an image is a representation of the image in the spatial-relationship domain. The importance of "objective" image features is easily seen in the inadequacy of annotations generated by a human annotator; there are no generally accepted predefined words for all the contextual occurrence of objects in images. Thus, image representation is better defined through image features.

In the image database literature, some of the image features that have attracted attention include colour histogram [4][5], object shape [6][7][8], transform coefficient [9][10], texture [11], image edge [3], spatial relationship of objects in an image [12][13], moment invariant [14][15], and their combination [16]. These features are usually compared under a particular distance.
metric; the closer distance, the more similar are the images (or objects) represented.

In the application described in this paper, an edge image is generated from a compressed representation of the image and used as the index. An appropriate feature should not only account for the nature of the edge image but must take into consideration the nature of possible queries. The user will be required to draw a sketch of some object in the target image. Moment invariants are a good choice in describing both the image index and the sketch presented by the user.

2.1. Moment

Moment is an important image descriptor used in pattern recognition [17],[15] and computer vision [14]. In general, moment extracts features of an image with respect to a reference axis or frame as a numeric value and is defined as,

\[ m_{n} = \int \int x^p y^q f(x,y) dx dy \]

The centralized moments are given as,

\[ \mu_n = \int \int (x - \bar{x})^p (y - \bar{y})^q f(x,y) dx dy \]

where, \( \bar{x} = \frac{\int \int x f(x,y) dx dy}{\int \int f(x,y) dx dy} \) and \( \bar{y} = \frac{\int \int y f(x,y) dx dy}{\int \int f(x,y) dx dy} \).

For example, the center of mass of an image can be described by using the two first order moment. Hu [18] defined a set of seven algebraic moment invariants based on the centralized and normalized version of (1). Hu's algebraic functions are invariant under rotation, reflection, translation and scale change.

From definition, the regular moment has the form of projection onto monomials, \( x^p y^q \), that constitute a complete but non-orthogonal basis set. This property accounts for the information loss, suppression and redundancy reported in [19]. Moments based on orthogonal basis functions have been introduced by Teague [20] to overcome problems associated with regular moments. Zernike moments are the projection of an image function onto a set of Zernike complex polynomials [21] and they form a complete orthogonal set over the interior of the unit circle. The Zernike moments of order \( n \) with repetition \( i \) for an image function \( f(x,y) \) can be defined in terms of the regular moments as

\[ A_{n} = \frac{1}{\pi} \sum_{i=0}^{n} \sum_{j=0}^{n} (-1)^{i+j} \frac{\binom{n}{i}\binom{n}{j}}{\binom{n}{r}} B_{n,i} B_{n,j} A_{(n-i,j)} \]

with \( r \| i \) selected as even and \( |i| \leq n \)

\[ B_{n} = (-1)^{n/2} \frac{\binom{n+k}{2}}{(n-k)/2!(k+1)/2!k/2!} \]

for \( (n-k) \) even

Because of orthogonal property of Zernike moments, image information is captured in a non-redundant manner by the various moment orders. For example, the zero-order moment represents mean intensity of an image function whereas the first order moments are related to centre of mass of an image. With appropriate normalization Zernike moments enjoy invariance to scale, rotation, and translation.

3. SIMILARITY MEASURE PARADIGMS

Numerical taxonomy, which allows the categorization of objects, is based on similarity functions. Similarity plays an important role in the theories of knowledge and behaviour [22]. The success of any feature set in discriminating or categorizing images depends to some extent on the use of an appropriate similarity function. Tversky [22] noted that it is not always appropriate to compute a metric distance between features, it might well be adequate to compare some features qualitatively. Similarity measures can be classified into 3 categories, namely, metric based models, set-theoretic based models and decision-theoretic based models. These will be briefly reviewed in the sequel.

3.1. Metric-based Models

A metric space is a set \( X \) with a distance function: \( d \) where \( X^2 \to \mathbb{R} \) such that \( \forall x, y, z \in X \) \( d \) satisfies the three axioms that define a metric [7]. The Minkowski r-metric, which generalizes a distance function, is defined as

\[ d_r(x, y) = \left( \sum_{i=1}^{n} |x_i - y_i|^r \right)^{1/r} \quad r \geq 1 \]

where \( x \) and \( y \) are two points in an \( n \)-dimensional space and \( i = 1, 2, \ldots, n \). The well-known Euclidean distance is a special case when \( r \) is equal to 2. The other cases of interest are when \( r \) is equal to 1 (city-block distance) or \( \infty \). When \( r \) is equal to \( \infty \), the distance can be defined as

\[ d_\infty(x, y) = \max(|x_i - y_i|) \]

The distance function can also be defined under a fuzzy set. Given two fuzzy sets, \( A \) and \( B \), the distance between them is defined as,

\[ d_\mu(A, B) = \left( \sum_{i=1}^{n} |\mu_A(x_i) - \mu_B(y_i)|^r \right)^{1/r} \quad r \geq 1 \]

where \( \mu_A \) and \( \mu_B \) are membership function.

Numerical features such as moment invariants lend themselves to comparison through these distance measures.

3.2. Set-theoretic based models

The set-theoretic model derived by Tversky are appropriate for feature comparison rather than distance computation and takes into consideration the fact that some features do not satisfy the symmetric property of metrics. For a set of features, \( A, B \) associated with images a, b, the Tversky defined a parametric family of similarity functions known as the contrast model,

\[ d(\theta, r, A, B) = \frac{\theta |A \cap B| - r |A - B| - \theta |B - A|}{\theta |A| + r |B|} \]

for some \( \theta, r, A, B \geq 0 \)

It is clear that this measure is more suitable for qualitative features.
3.3. Decision-theoretic based models

The basis of these models is that a set of \( p \) attributes are defined for a set of \( n \) images. A decision matrix \( X_{np} \) is a zero-one matrix indicating the possession or otherwise of each attribute by each of the \( n \) images. For two images \( i, j \), let \( n_i, n_j \) and \( q_{ij} \) represent the number of attributes they have (i) in common, (ii) missing and (iii) in disagreement respectively. Table 1 shows a list of commonly defined similarity measure based on these variables\cite{23}.

Table 1: Some commonly used decision-theoretic measures

<table>
<thead>
<tr>
<th>Measure</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>ANBERG</td>
<td>( S(i,j) = \frac{n_i}{n_i + 2q_{ij}} )</td>
</tr>
<tr>
<td>JACCARD</td>
<td>( S(i,j) = \frac{n_i}{n_i + q_{ij}} )</td>
</tr>
<tr>
<td>KULCYNZKI</td>
<td>( S(i,j) = \frac{n_i}{q_{ij}} )</td>
</tr>
<tr>
<td>SOKAL-SNEATH</td>
<td>( S(i,j) = (n_i + n_j)(n_i + q_{ij} + n_j) )</td>
</tr>
</tbody>
</table>

These measures are obviously suitable for qualitative features. They however suffer from the drawback that the features must be defined a priori for both images. This may be the case in specialised image databases but will rarely be useful in a "free form" image database. It should be noted that the set-theoretic measure of Tversky does not assume that features are predefined.

This paper uses Euclidean distance as a means of measuring similarity between two Zernike moment based features.

4. SIMULATION RESULTS AND DISCUSSION

The performance of the proposed scheme is tested by generating a database of ten edge images. These images are artificially generated so as to remove the bias from noise. The images labeled Tm1 through Tm10 consist of edge images of both geometrical and arbitrary shapes. Sketches of a car and a house are also included. The query images are formed from affine transformed versions of the original images. For example, the edge image Tm1r (see Figure 1) is a 90° rotated version of Tm1. A free-hand drawing of Tm1 (see Tm1d in Figure 1) is included as a realistic query that has suffered some deformation.

4.1. Simulation 1

Regular moment invariant and Zernike moments of two images namely, Tm1 and Tm3, are computed and compared against variation of Tm1 in terms of scale, rotation, and some degree of deformity. Figure 1 shows the image Tm1, Tm3, and variation of Tm1. The results are compared in Table 2 where the suffixes s (scale), r (rotation), d (deformation) signify the transformations to which the image has been subjected and the suffix t signifies truncation.

4.2. Simulation 2

This simulation is devised to test the performance of Zernike moment invariants in a database application. The ten edge images in the database were used; the query images were generated by transforming the images in the database. Three classes (P1, P2, P3) of query images corresponding to three sets of transformation on the images in the database are created. P1 consists of ten scaled images, P2 consists of 20 scaled and rotated (90°)
images and P3 consists of 30 scaled, and rotated (30° and 90°) images. No attempt has been made to ensure that the classes are disjoint. Zernike moment invariants up to order 12 (i.e. 47 features) were computed for each of the images in the query sets and compared to image database features. The rates of recognition are shown in Table 3.

### Table 3: Rate of recognition of scaled and rotated query images from the database (P1: scaling; P2: scaling & rotation (90°); P3: scaling & rotation (30° & 90°)).

<table>
<thead>
<tr>
<th>Transformation of the query image</th>
<th>P1</th>
<th>P2</th>
<th>P3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rate</td>
<td>90%</td>
<td>90%</td>
<td>72%</td>
</tr>
</tbody>
</table>

The recognition rate for transformation P3 is the lowest of the three classes. The reason for this performance is likely due to the artifacts introduced by the rotation through 30°. This may suggest that the proposed method will be sensitive to noise. In [17] the problem of noise was anticipated and an averaged feature vector of a set of training images was used as the representation in the database. This method was reported to have given a recognition rate up to 99% for alphabetic characters; their worst case being 86%

### 5. CONCLUSION

A method of describing the edge image derived from compressed images is proposed. An artificially generated image database was used to test it performance and the results obtained are indicative of it potential. Further work needs to be done in order to use the edge images derived directly from the compressed images.

### 6. ACKNOWLEDGEMENT

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### 7. REFERENCES


